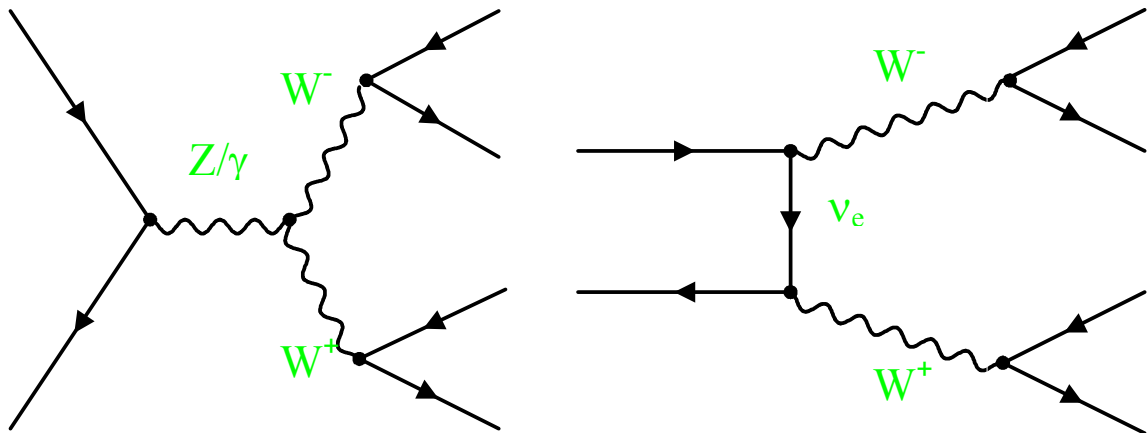


W mass and W^+W^- final state interactions



Nigel Watson
University of Birmingham

Outline

- W mass and width
 - \Rightarrow systematics
- Colour Reconnection
- Bose-Einstein Correlations
- Combined LEP Results
- Summary

W^+W^- final states

BR=45%

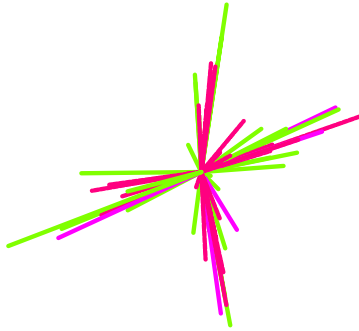
~ 87% efficiency

~ 20% impurity, mostly $Z \rightarrow qqg$

4 jets, fully observed

☹ jet-jet \leftrightarrow W ambiguity

☹ Final State Interactions

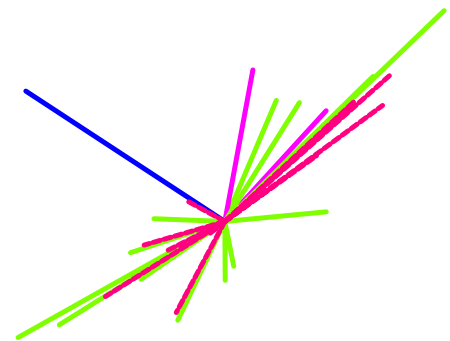


BR=44%

~ 85% efficiency

~ 10% impurity, mostly non-WW 4-f

2 jets, 1 charged lepton, $\geq 1 \nu$



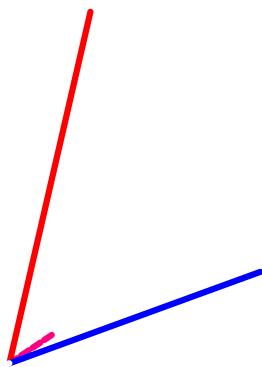
BR=11%

~ 80% efficiency

~ 10% impurity, mostly non-WW 4-f

☹ 2 charged leptons, $\geq 2 \nu$

minimal impact on M_W .



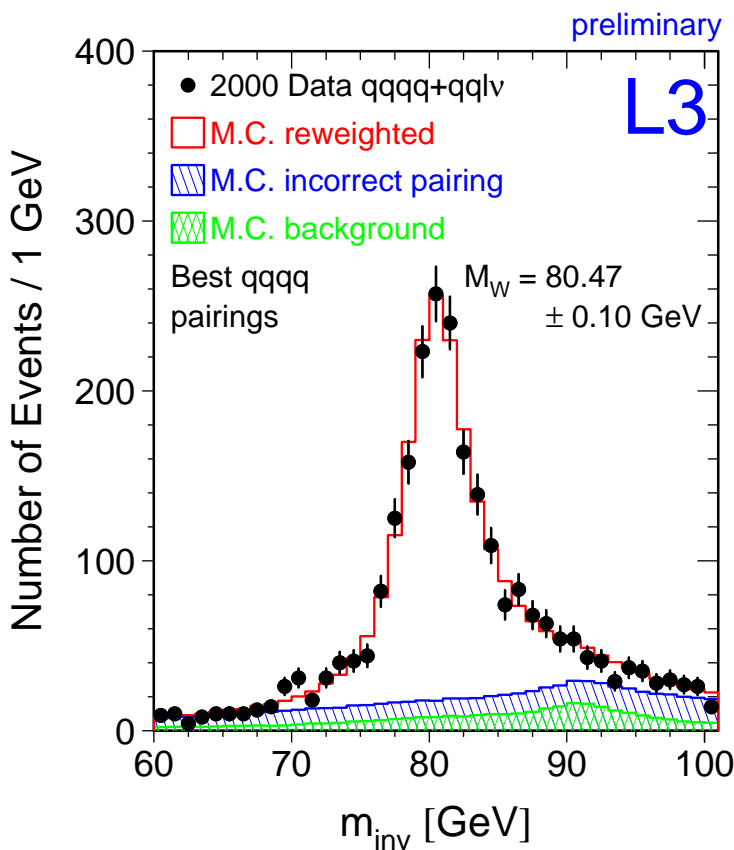
ADLO combined, $\sim 2\,300\text{ pb}^{-1}$ data for M_W measurement

$\Rightarrow 30\,000\ W^+W^-$

82% all LEP2 sample analysed (100% Aleph, L3)

Invariant Mass Reconstruction

Reconstruct jets (q, g) and charged leptons



Constraints

4 $\sum (E, \underline{p}) = (\sqrt{s}, \underline{0})$

1 $\text{mass } W^+ = \text{mass } W^-$

Jet energy measurement

poor cf. angles

Kinematic fit \rightarrow improved mass resolution

qq lv 1C, 2C fits for $l=e, \mu$

1C only for $l=\tau$ (τ energy unknown)

qq qq 4C, 5C fits 2 or 1 masses/event

Choose/weight jet pairing by: di-jet angles,

kin. fit probability, masses, CC03 matrix element

M_W Determination

3 methods

- Reweight “detector level” MC to arbitrary M_W [A,L,O]

- 1d fit to average mass, ≥1 bins of mass error

- 2d fit to 4C fit mass

- implicit MC correction

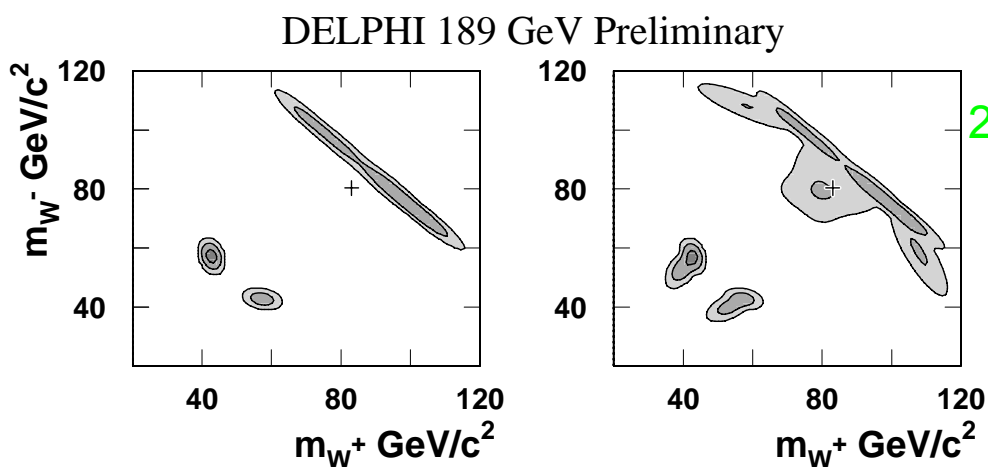
- Direct analytic fit [O]

- Asymmetric Breit-Wigner, explicit MC calibration

- Convolve Breit-Wigner with resolution, ISR [D,O]

- $L(M_W, m_{\text{rec}}) = p_w \cdot \text{BW}(M_W, m, s') \otimes \text{ISR}(s, s') \otimes R(m, m_{\text{rec}})$

- 1d or 2d



Systematic Effects

Important! > **combined statistical error = 26 MeV**

Errors either uncorrelated, or correlated:

- between **expts. and channels**
- between expts. in **single channel**

Source	Uncertainty on M_W (MeV)		
	qqlv	qqqq	Combined
ISR/FSR	8	8	7
Hadronisation	19	17	18
Detector	11	8	10
Beam energy	17	17	17
Colour	-	40	11
Reconnection	-		
Bose-Einstein	-	25	7
Other	4	5	3
Total systematic	29	54	30
Statistical	33	31	26
Total	44	63	40

- **BEC/CR uncertainty** \Rightarrow **qqqq net weight = 0.27**
- **With equal systematics, statistical uncertainty = 22 MeV**

ISR/FSR

- Compare ISR models, e.g. in KORALW/EXCALIBUR
- **Reweight** KORALW (LLA) $O(\alpha^3) \rightarrow O(\alpha^2), O(\alpha^1)$
 - **incomplete** at $O(\alpha)$, no $\text{ISR} \leftrightarrow \text{FSR}$, $W+\gamma$
 - \Rightarrow **Full** $O(\alpha)$, DPA of RACOONWW (unweighted)

Hadronisation

- Compare various models and parameter variation
- Reweight relevant variables MC/data, propagate $\rightarrow M_W$
- Mixed Lorentz Boosted Z^0 (MLBZ) (D)

Beam Energy

$$\Delta M_W = M_W \cdot \Delta E_{\text{beam}} / E_{\text{beam}}$$

- Resonant depolarisation, NMR probes/flux loop
- LEP Spectrometer

Final State Interactions

- **Colour Reconnection** (QCD vacuum properties)
- **Bose-Einstein Correlⁿ** (coherent particle production)

Colour Reconnection

Two colour singlets, may not hadronise independently

W^+W^- decay vertices ~ 0.1 fm

hadronic scale ~ 1 fm

} large spacetime overlap

Perturbative CR suppressed $\sim (\alpha_s/\pi)^2 \Gamma_W/N_c^2$

Non-perturbative CR, implemented in hadronisation models

- More reconnection (+background!) when hadronisation regions overlap
- spacetime picture of shower development important

“Observable” Effects

- Inclusive multiplicity, $\ln(1/x_p)$, soft or heavy particles
- Particle distribution relative to 4-jet topology
- Aim to control/calibrate systematic on M_W

Analysis Method

- Compare qq̄q̄q data with: models, no-CR and CR
MLBZ or qq̄lv data

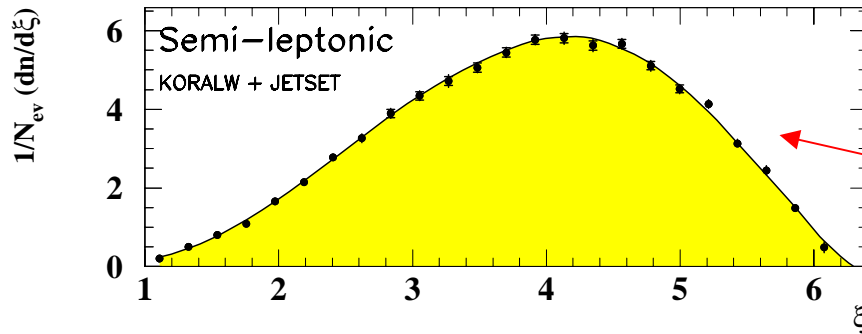
Inclusive Analyses

CR effects expected larger for soft particles, $p < \Gamma_W$

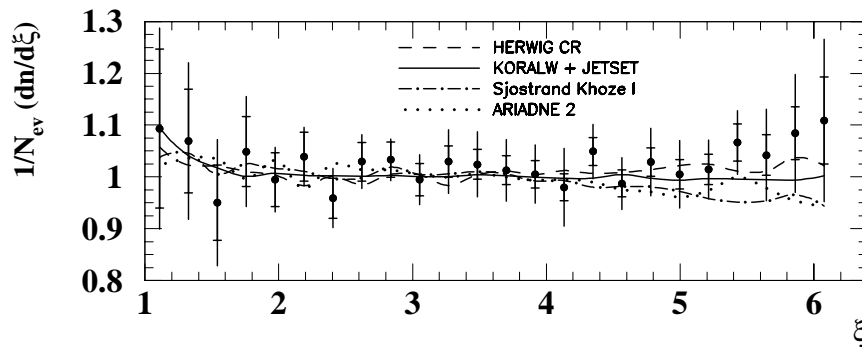
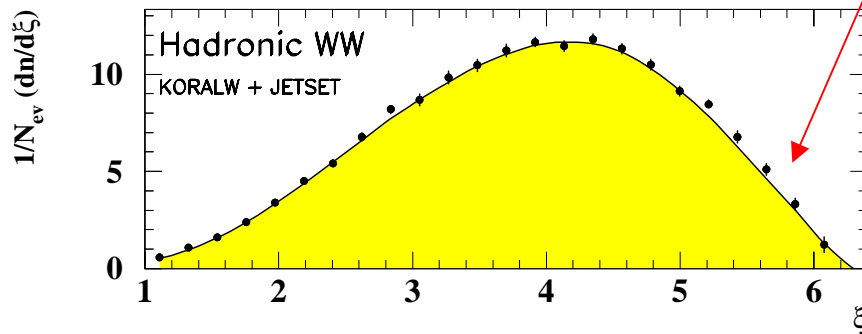
Look at observables with implicit scale, e.g. $\ln(1/x_p)$, p_T , y

$\ln(1/x_p)$

ALEPH preliminary combination 183-202GeV



data excess also seen in Z^0 events



EXCALIBUR vs. SK models is predicted CR effect

Uncorrected data, ratio $4q/qq\bar{v}$ not expected flat

Data consistent with CR and non-CR models

Integrate to obtain $\langle n_{ch} \rangle$

Charged Particle Multiplicity

Compilation of (mostly) preliminary results

Define $\Delta\langle n \rangle = \langle n^{4q} \rangle - 2 \langle n^{qq|v} \rangle$

All errors are stat. \oplus syst.

Expt.	$\langle n^{4q} \rangle$	$\langle n^{qq v} \rangle$	$\Delta\langle n \rangle$
ALEPH* 183–202 GeV	35.75 \pm 0.54	17.41 \pm 0.19	+0.98 \pm 0.43 [#]
DELPHI 183 GeV 189 GeV	38.11 \pm 0.72 39.12 \pm 0.49	19.78 \pm 0.65 19.49 \pm 0.41	See below
L3 183–202 GeV	37.90 \pm 0.43	19.09 \pm 0.24	-0.29 \pm 0.40
OPAL 183 GeV 189 GeV	39.4 \pm 0.8 38.31 \pm 0.44	19.3 \pm 0.4 19.23 \pm 0.27	+0.7 \pm 1.0 -0.15 \pm 0.58

* Not corrected for selection, # is $\Delta\langle n \rangle(\text{data}) - \Delta\langle n \rangle(\text{MC})$

DELPHI measure [Eur.Phys.J.C18(2000)203]

$$\langle n^{4q} \rangle / 2\langle n^{qq|v} \rangle = 0.981 \pm 0.027 \quad 0.1 < p < 1 \text{ GeV}$$

All models **except** ARIADNE 3, VNI consistent with data

Similarly for particle dispersion

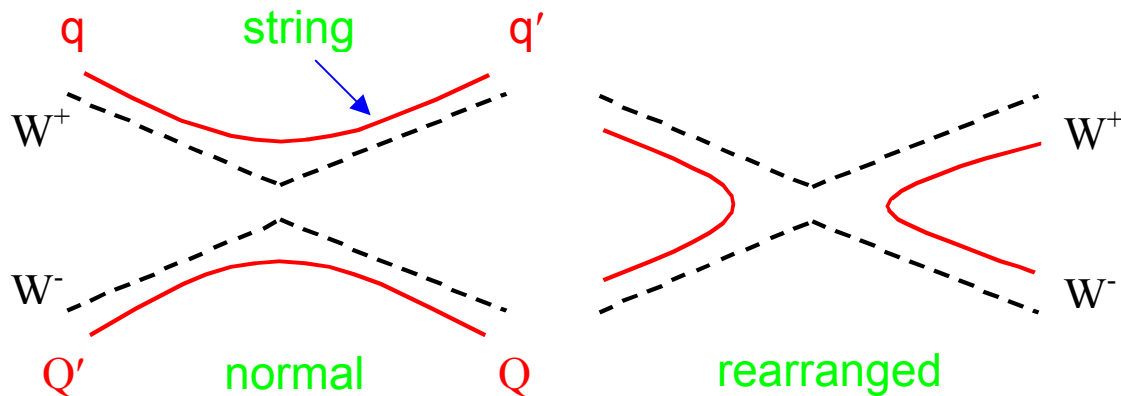
Systematic > **statistical uncertainty**

\Rightarrow combination requires proper treatment of correlations

“Heavy hadrons”, numerically larger effects, less sensitive

Interjet Analysis (L3)

Motivated by simple string picture of reconnection



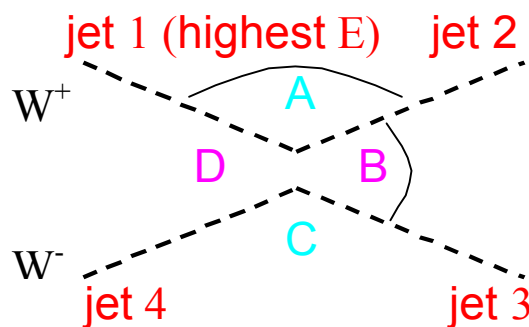
Non-standard qq̄q̄q selection, plus topological cuts:

2 larger jet-jet angles $100^\circ < A, C < 140^\circ$, +not adjacent

4 distinct jets

$y_{34} > 0.01$

(k_\perp scheme)

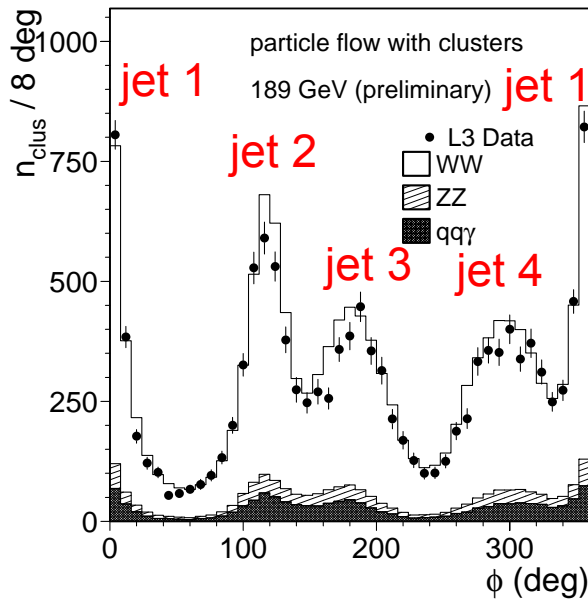


2 smaller jet-jet

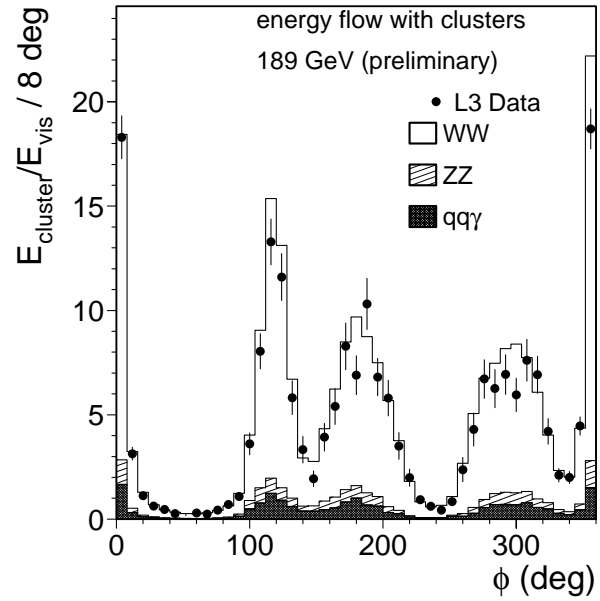
angles $B, D < 100^\circ$

- “strings” back-to-back, not crossing
- good jet-jet \Leftrightarrow W associations, 4 partons similar energy
- $WW \rightarrow qq\bar{q}\bar{q}$, efficiency=15%, purity=85%, 189 GeV MC
 - \Rightarrow 209 candidates at $\sqrt{s} \approx 189$ GeV
- Correct pairing+non-crossing topology in 87% events

- project particles onto jet 1-jet 2 plane
- follows earlier idea, “string effect” for 4-jets

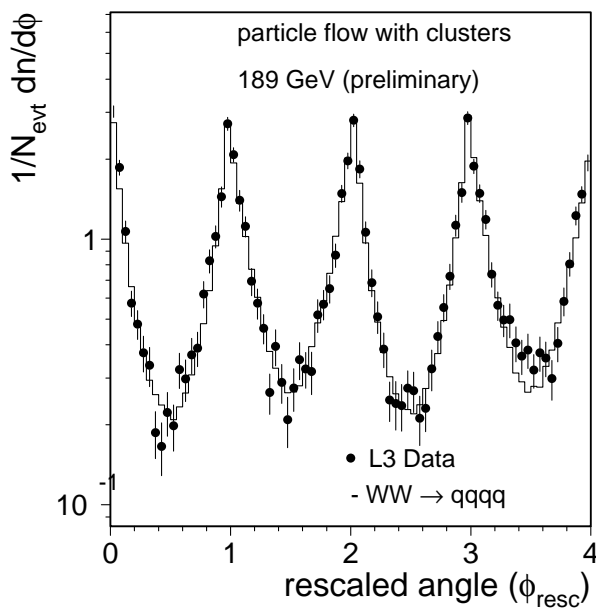


multiplicity flow

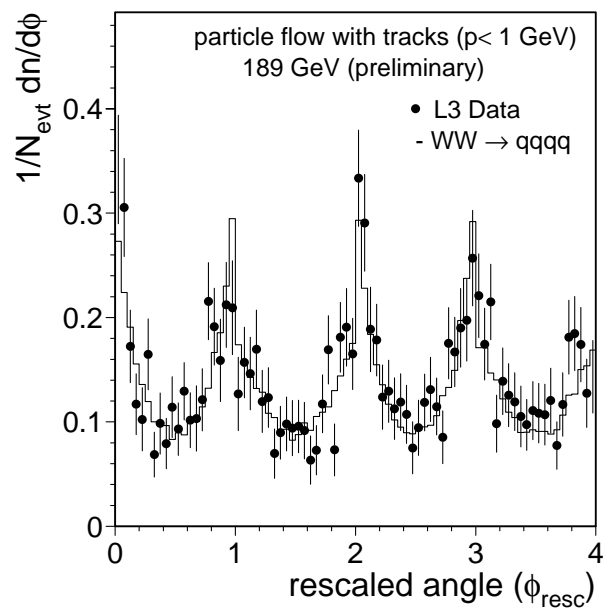


energy flow

- Normalise flow to jet-jet angles, subtract background, correct non-planarity of 4-jets

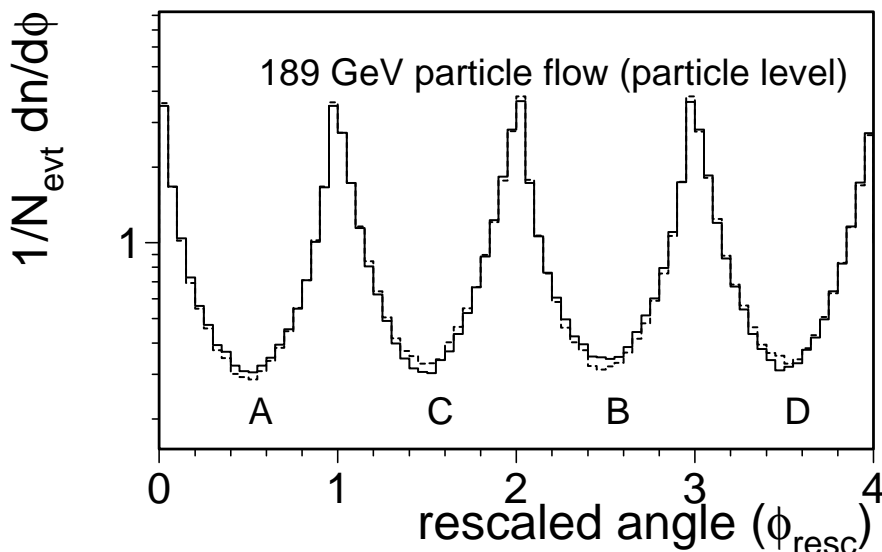


multiplicity flow

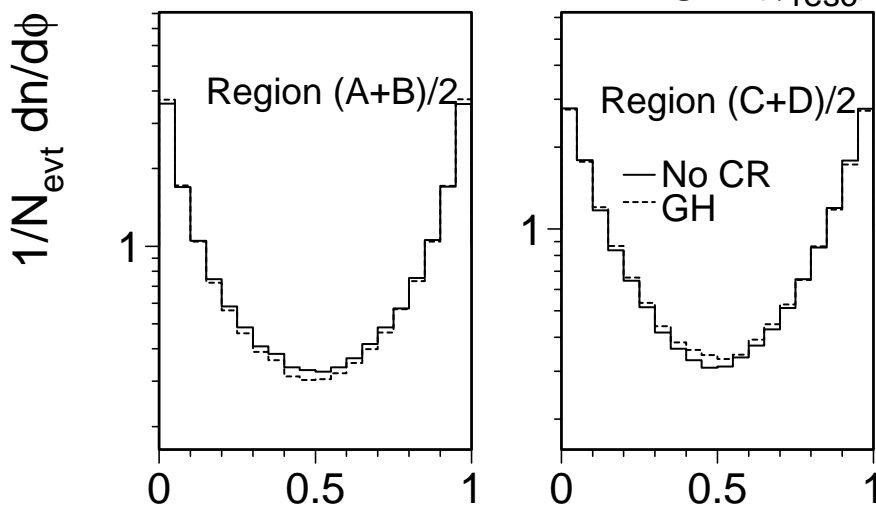


energy flow, $p < 1$ GeV

Model study without detector simulation



Predictions for
 $p > 0.1$ GeV



Depleted A,B

Enhanced C,D

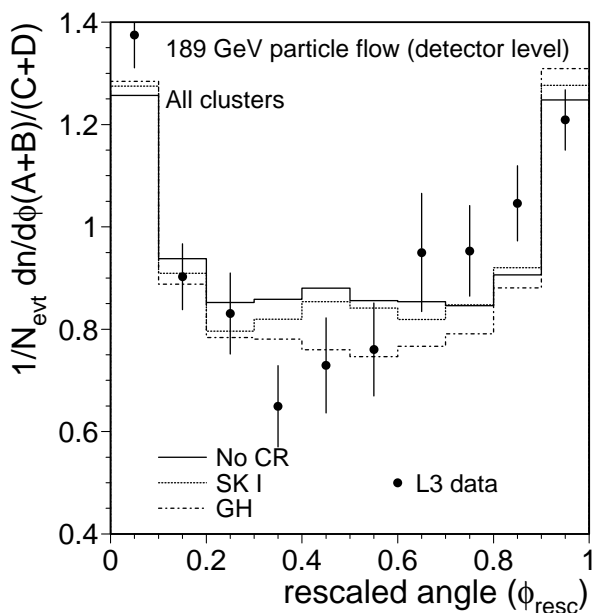
Improved comparison by averaging regions:

- between jets of different W s (C,D)
- between jets of same W (A, B)

Examine ratio (C+D) / (A+B)

- Quantify
$$\frac{\int \text{dn}/\text{d}\chi_R \text{ (inter-}W) \text{ d}\chi_R}{\int \text{dn}/\text{d}\chi_R \text{ (intra-}W) \text{ d}\chi_R}, \quad \chi_R = 0.2-0.8$$

Reduced angle flow in data



L3 189 GeV.

Sensitivity SK I (100%) = 3.2σ

SK I (32%) ~ 0.5

OPAL 189 GeV.

Looser cuts:

high efficiency 42%

same purity.

Jet pairing l'hood

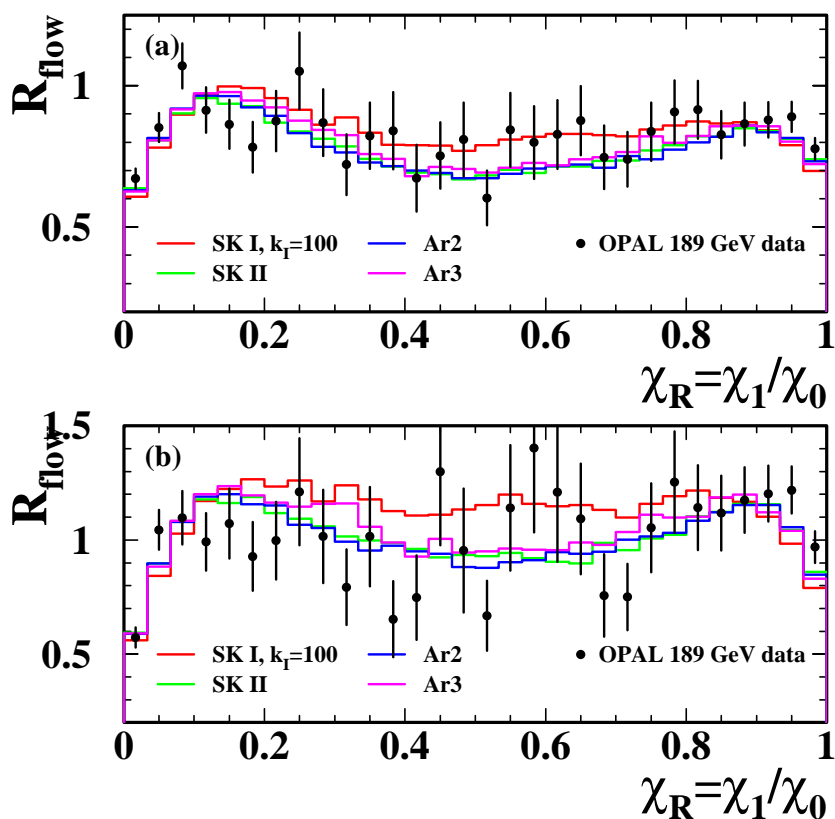
Kinematic fit axes

No double counting

Predicted sensitivity

improves slightly

OPAL Preliminary

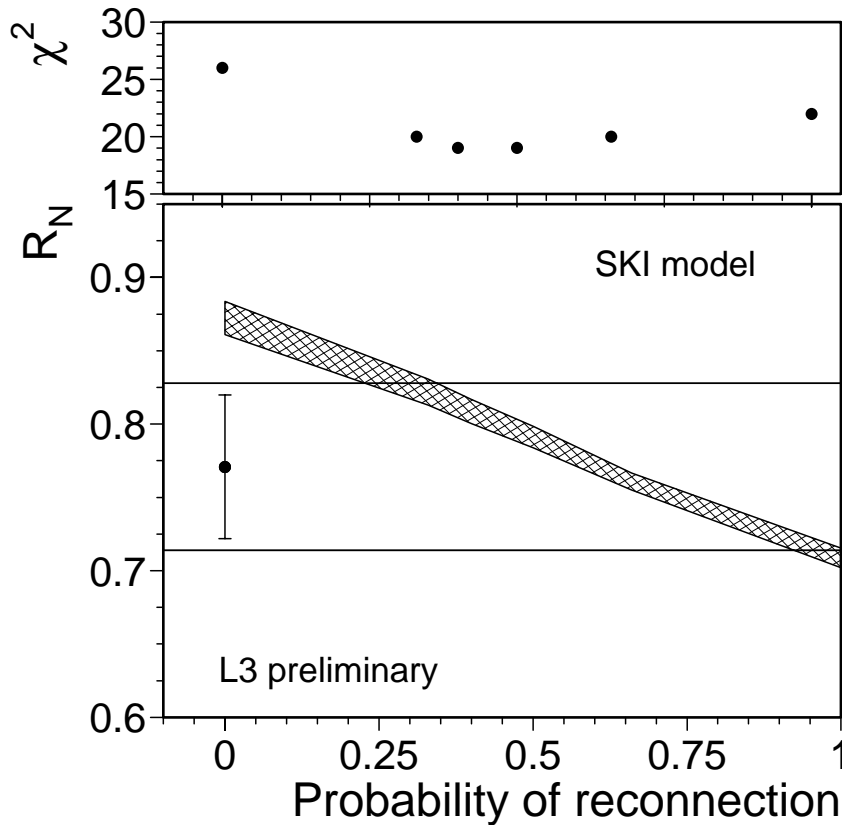


This analysis, favours SK I $\sim 65\%$ reconnected

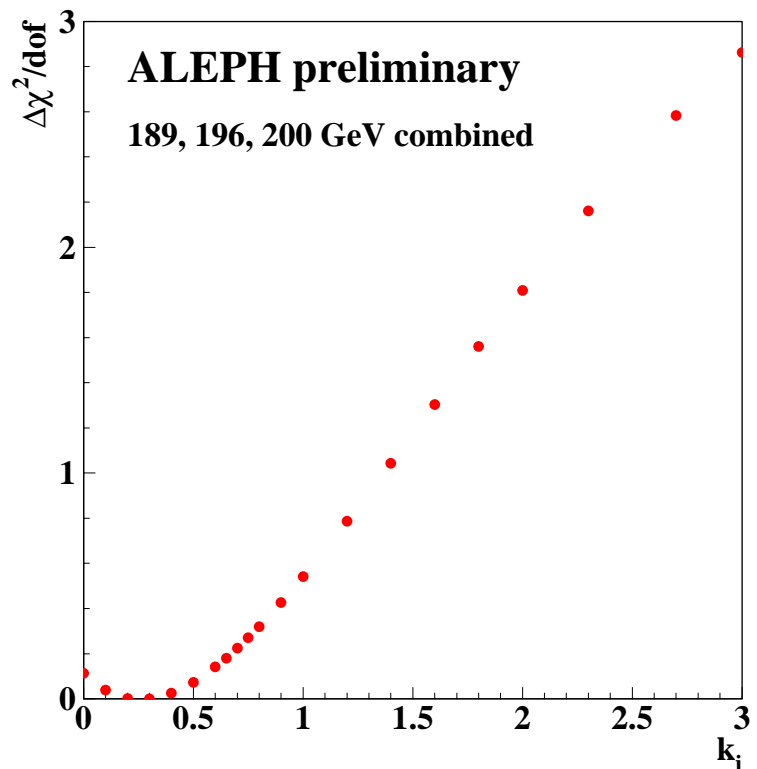
OPAL repeat of L3 analysis, best agreement with no-CR...

Towards mass biases

Estimate preferred P_{RECON} in models from data



L3 data prefer
 SK I prob. $\sim 40\%$
 1.7σ from no-CR



ALEPH data prefer
 SK I prob. $\sim 15\%$

Non-trivial differences in model predictions A/D/L/O

Bose-Einstein Correlations

Enhanced production of **identical** boson pairs ($\pi^+\pi^+$ or $\pi^-\pi^-$) at small 4-momentum difference, $Q^2 = -(p_1 - p_2)^2$

Firmly established phenomena, LEP1 and intra-W

Traditionally studied using 2-particle correlation function:

$$R(p_1, p_2) = \rho_2(p_1, p_2) / \rho_0(p_1, p_2)$$

Problem 1

Reference ρ_0 should be **identical** to ρ , but without BEC, so:

- **Unlike-sign data**, / ratio of same in MC (**resonances**)
- Like-sign MC without BEC (**MC modelling**)
- **Event mixing**

Many ways to study effect, all experiments differ!

Essential question: do BEC exist between W^+ and W^- ??

Problem 2

non-pQCD **amplitudes unknown**, resort to models

phenomenological parametrisation $R(Q) \sim 1 + \lambda \exp(-r^2 Q^2)$

BE strength

source radius

OPAL Analysis

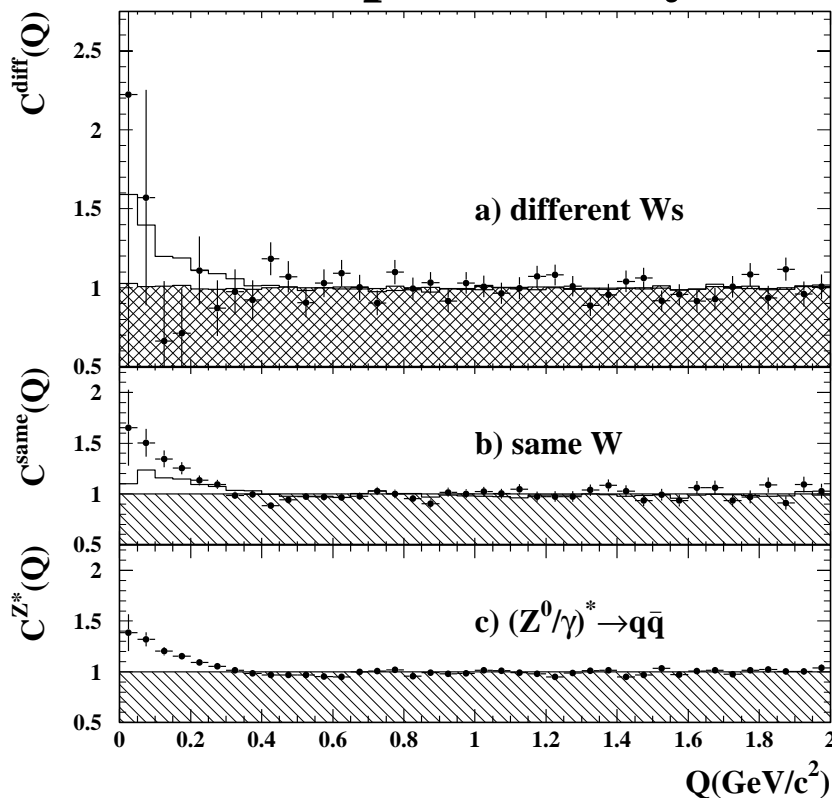
$C(Q) \sim \text{ratio (like-sign/unlike-sign)} \mid (\text{data})/(\text{no-BEC MC})$

3 event classes: $W^+W^- \rightarrow qqqq$, $W^+W^- \rightarrow qq\ell\nu$, $Z/\gamma \rightarrow qq$

Each class $C(Q) = \text{sum of pure contributions} \times \text{prob. (MC)}$

- $C^{\text{DIFF}}(Q)$ inter-W BEC
 - $C^{\text{SAME}}(Q)$ intra-W BEC
 - $C^{Z^*}(Q)$ non-radiative qq
- } simultaneous fit,
extract λ^{DIFF} for
various source size
hypotheses

OPAL preliminary



e.g.

$$R^{\text{DIFF}} = R^{\text{SAME}} = R^{Z^*}$$

$$\lambda^{\text{DIFF}} = -0.14 \pm 0.36$$

$$\lambda^{\text{SAME}} = 0.70 \pm 0.10$$

indep. R's

$$\lambda^{\text{DIFF}} = 2.9 \pm 1.7$$

$$\lambda^{\text{SAME}} = 0.62 \pm 0.10$$

Establishes intra-W BEC

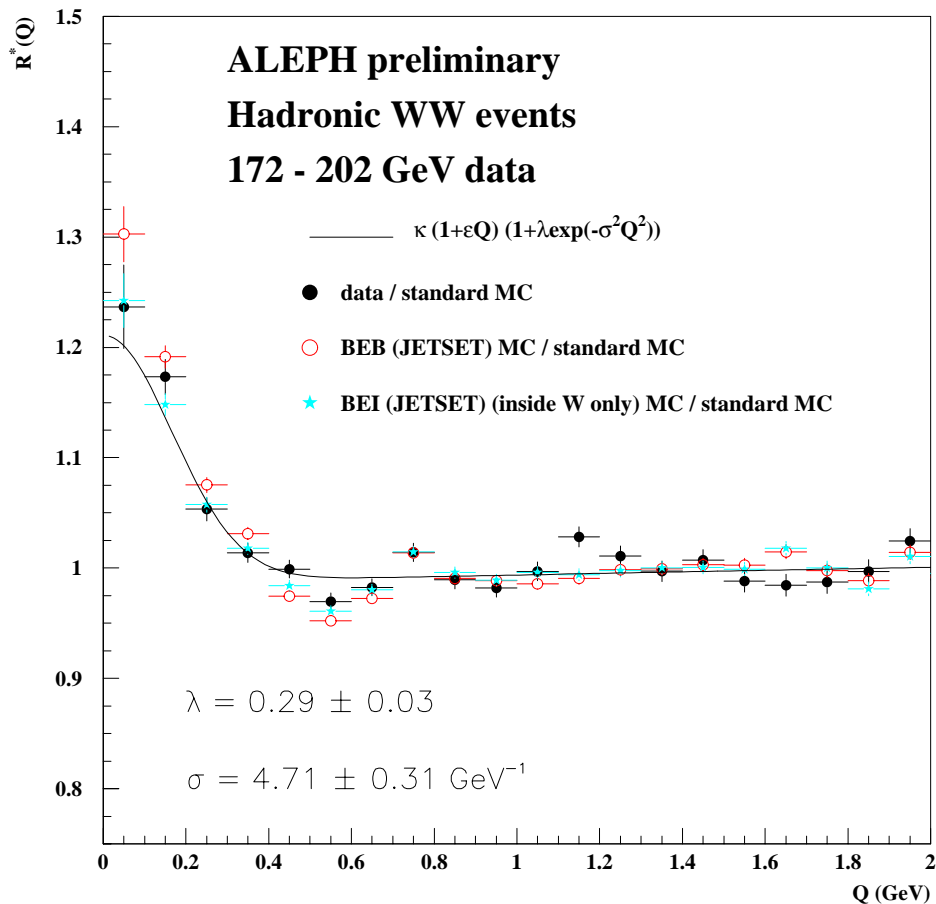
Unable to determine whether inter-W BEC exist

ALEPH Analyses

$R(Q) \sim \text{ratio (like-sign/unlike-sign) | (data)/(no-BEC MC)}$

Include $Z/\gamma \rightarrow qq$ background with BE_3

BE_3 model tuned with high statistics 91 GeV data



Disfavours inter-W BEC at 2.2σ

Compatible with intra-W BEC

Event mixing analysis

Also (qualitatively) disfavours inter-W BEC

L3 Analysis

Idea from Chekanov, De Wolf, Kittel, E.Phys.J. **C6**('99)403

If W^+ and W^- decays **uncorrelated**

$$\rho_2^{WW}(p_1, p_2) = \underbrace{\rho_2^{W^+}(p_1, p_2) + \rho_2^{W^-}(p_1, p_2)} + 2 \underbrace{\rho_1^{W^+}(p_1) \rho_1^{W^-}(p_2)}$$

Take $\rho_2^{W^+} = \rho_2^{W^-} = \rho_2^W$

Estimate from qqlv

$\rho_{MIX}^{WW}(p_1, p_2)$

mix 2 qqlv events,

$\Rightarrow \text{BEC} \equiv 0$

Remove background:

$$\rho_2 = 1/(\text{Purity} \cdot N_{EVENTS}) \cdot (dn/dQ - dn_{BACKGROUND}/dQ)$$

All **background samples** include BEC (BE₃₂ model)

Form ratio $D = \text{lhs}/\text{rhs}$

$$D' = D(\text{data}) / D(\text{MC, intra-W BEC})$$

remove

potential

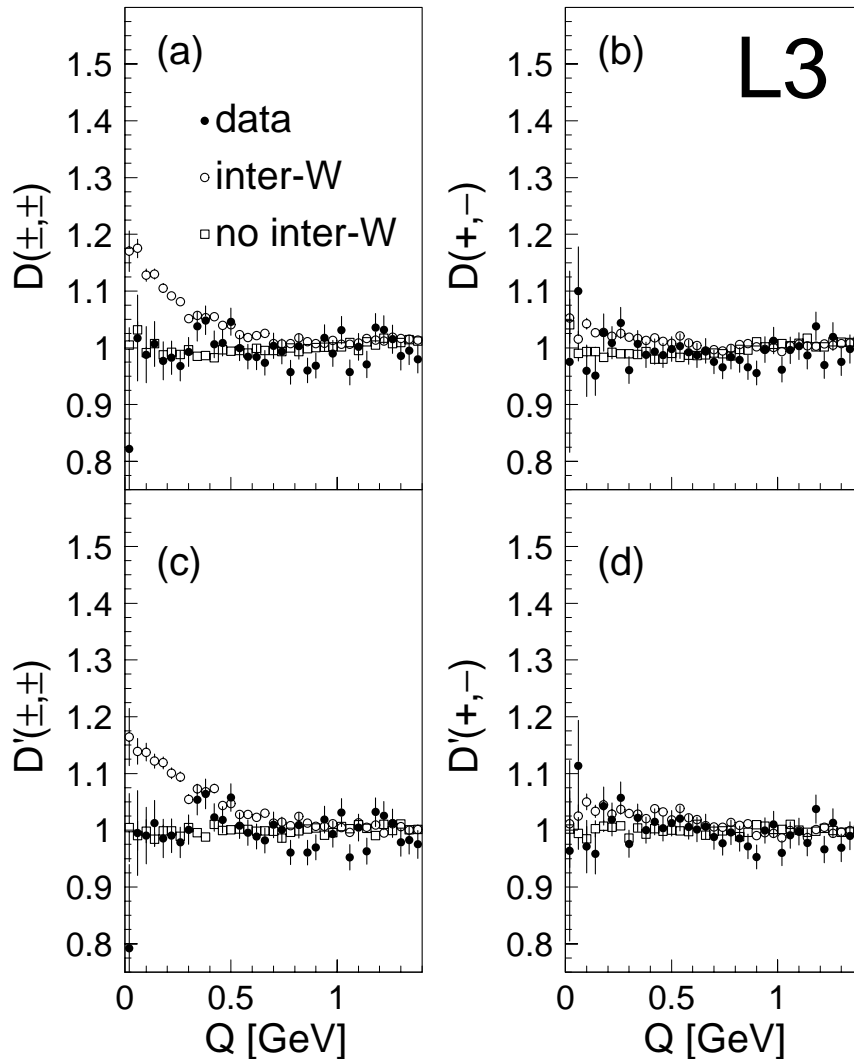
residual bias

$D \cong D' \neq 1 \Rightarrow$ non-independent W decays

\Rightarrow plausibly **inter-W BEC**

Using 1998–1999 data ~60% total L3 luminosity

PRELIMINARY 98+99 DATA



Single ratio

Double ratio
Data/MC

$$\text{Fit } D'(Q) = (1 + \epsilon Q)(1 + \Lambda \exp(-\kappa^2 Q^2))$$

No inter-W BEC $\Rightarrow \Lambda = 0$

$$\Lambda = 0.013 \pm 0.018 \text{ (stat.)} \pm 0.015 \text{ (syst.)}$$

Compare BE₃₂/Koralw $\Lambda = 0.126 \pm 0.006 \text{ (stat.)}$

Data disagree with inter-W BEC model by 4.7σ

Preliminary Combined LEP Results

Based on ~ 82% of all LEP2 data

$W^+W^- \rightarrow qqqq,$

172–208 GeV

$\chi^2=30.3/32$

ΔM_W (stat.)=31 MeV

ΔM_W (syst.)=54 MeV

LEP Preliminary : Winter 2001

ALEPH

80.507 ± 0.070

DELPHI

80.373 ± 0.091

L3

80.478 ± 0.093

OPAL

80.408 ± 0.120

LEP

80.460 ± 0.062

80.0

81.0

$M_W(qqqq)$ [GeV]

LEP Preliminary : Winter 2001

ALEPH

80.456 ± 0.060

DELPHI

80.381 ± 0.100

L3

80.314 ± 0.087

OPAL

80.510 ± 0.074

LEP

80.442 ± 0.044

$W^+W^- \rightarrow qq\bar{l}\nu$

172–208 GeV

$\chi^2=30.3/32$

ΔM_W (stat.)=34 MeV

ΔM_W (syst.)=28 MeV

80.0

81.0

$M_W(qq\bar{l}\nu)$ [GeV]

Preliminary Combined LEP Results

Based on ~ 82% of all LEP2 data

$W^+W^- \rightarrow qq\bar{q}\bar{q}, qq\bar{l}\bar{l}$

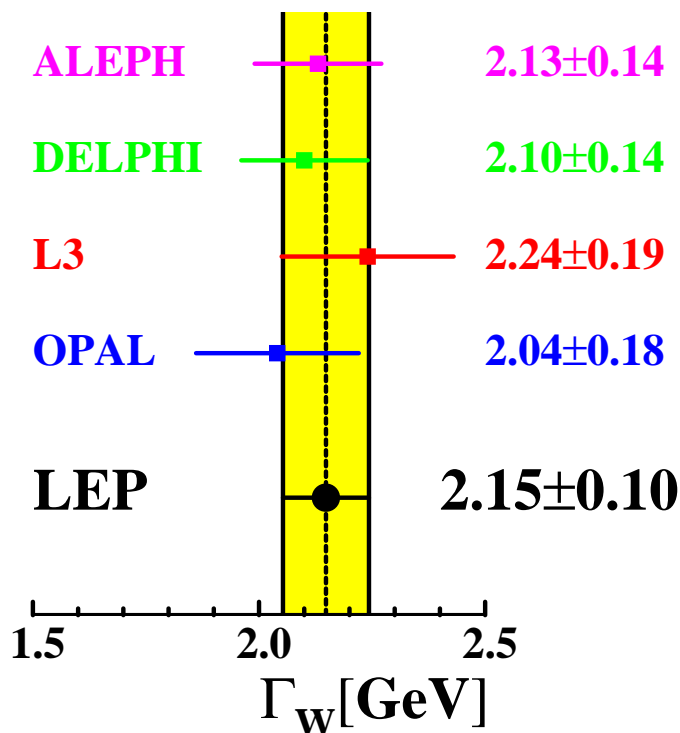
172–208 GeV

$\chi^2=17.7/21$

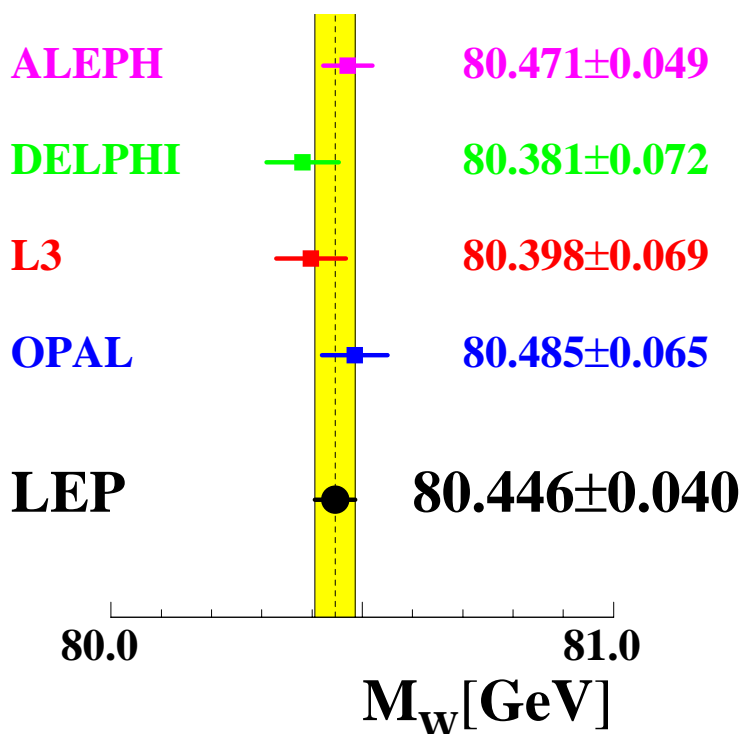
$\Delta\Gamma_W$ (stat.)=71 MeV

$\Delta\Gamma_W$ (syst.)=63 MeV

LEP Preliminary : Winter 2001



LEP Preliminary : Winter 2001



$W^+W^- \rightarrow$ all

161–208 GeV

$\chi^2=30.4/33$

ΔM_W (stat.)=26 MeV

ΔM_W (syst.)=30 MeV

Preliminary Combined LEP Results

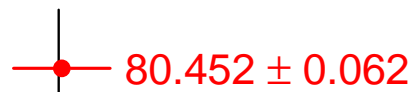
LEP M_W currently

world best direct measurement.

Use to probe M_{higgs}

W-Boson Mass [GeV]

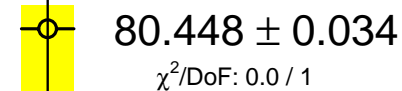
$p\bar{p}$ -colliders



LEP2



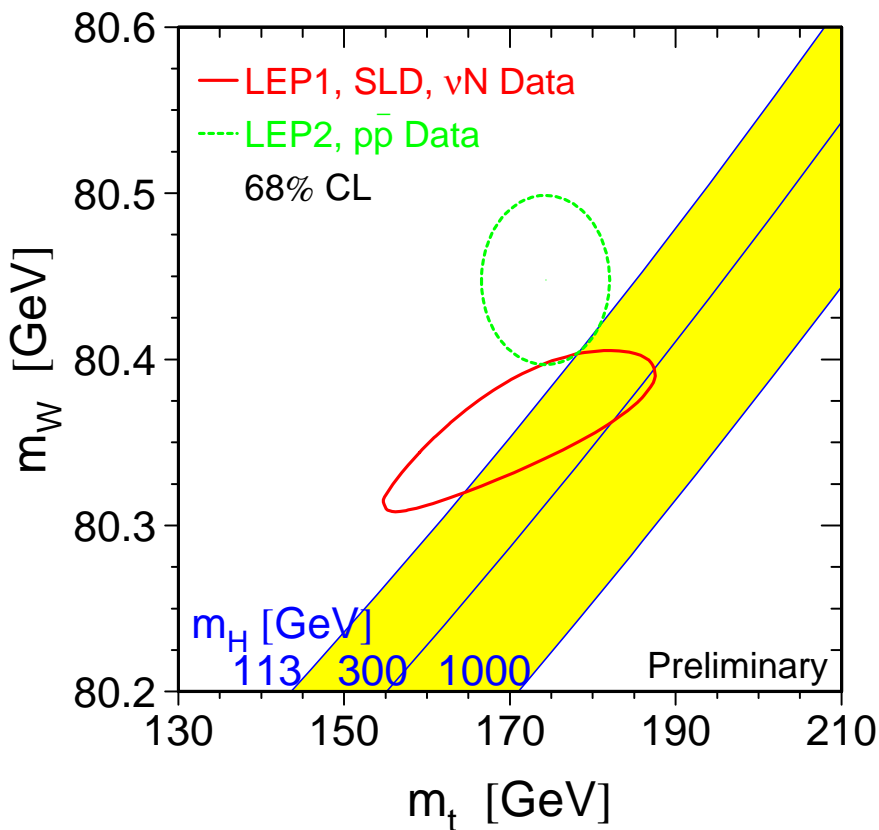
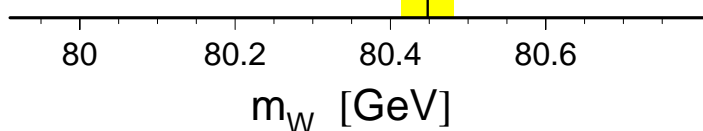
Average



NuTeV/CCFR



LEP1/SLD/vN/ m_t



Data seem to favour light Higgs

Summary

- 1996–2000, 2.8fb^{-1} accumulated, $\approx 82\%$ used in this M_W

- LEP combined $M_W = 80.446 \pm 0.026 \pm 0.030 \text{ GeV}$

[preliminary] $\Gamma_W = 2.148 \pm 0.071 \pm 0.063 \text{ GeV}$

$$\Delta M_W(\text{qqqq}-\text{qq}|\nu) = +18 \pm 46 \text{ MeV}$$

— Improved understanding of **systematics** to come

- **Colour Reconnection**, must combine results,

— e.g. **interjet multiplicity**

— need to understand **model differences** among ADLO

- Picture of **Bose-Einstein Correlations** becoming **more coherent** at LEP?