$D^0 - ar{D}^0$ Mixing

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 - ... Different measurements; present data
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 - ... SU(3) analysis & OPE predictions for Δm and $\Delta \Gamma$
 - ... $\Delta\Gamma$ from SU(3) breaking in phase space
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see: A. Falk, Y. Grossman, Z.L., A. Petrov, PRD 65 (2002) 054034 [hep-ph/0110317]

S. Bergmann, Y. Grossman, Z.L., Y. Nir, A. Petrov, PLB 486 (2000) 418 [hep-ph/0005181]

Introduction

Dictionary: CPV = CP violation

SM = standard model

NP = new physics

CA = Cabibbo allowed

DCS = doubly Cabibbo suppressed

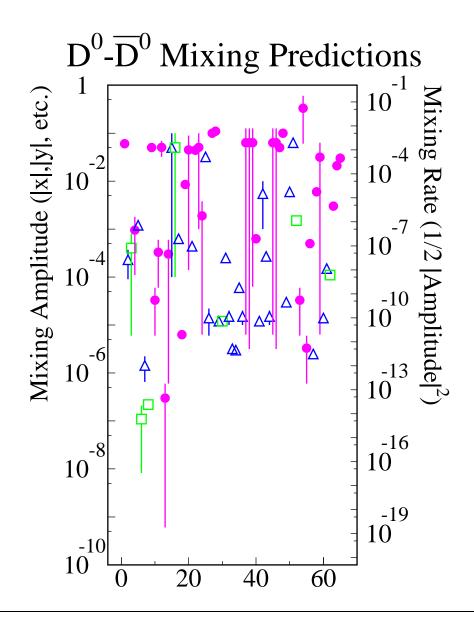
Why is $D - \bar{D}$ mixing important?

Of the neutral meson systems $D - \bar{D}$ mixing is unique in that:

- The only meson system where mixing has not been observed
- The only meson where the mixing is generated by the down type quarks
- Expected to be small in the SM: $\Delta M, \Delta \Gamma \lesssim \text{few} \times 10^{-3} \, \Gamma$, since it is DCS and vanishes in the flavor SU(3) symmetry limit
- It involves only the first two generations: If CPV $\gg 10^{-3}$ is observed unambiguously new physics
- Sensitive to new physics: NP can easily enhance ΔM but would not affect $\Delta \Gamma$ If D mixing is large: $\Delta \Gamma \gtrsim \Delta M$ probably large flavor SU(3) breaking $\Delta M \gg \Delta \Gamma$ probably new physics
- ullet There were two recent measurements with signals at the $\sim 2\sigma$ level



$oldsymbol{D}$ mixing predictions within and beyond the SM



(H. Nelson, hep-ex/9908021)

ullet : NP predictions for x

 \triangle : SM predictions for x

 \square : SM predictions for y

Definitions:
$$x\equiv \frac{\Delta M}{\Gamma}$$

$$y\equiv \frac{\Delta\Gamma}{2\Gamma}$$

$$|D_{L,S}\rangle=p\,|D^0\rangle\pm q\,|\bar{D}^0\rangle$$



Recent measurements of $D^0 - \bar{D}^0$ mixing (1)

• Measure D lifetime in decays to a CP eigenstate, e.g., K^+K^- , and a flavor eigenstate, e.g., π^+K^- , fitting exponential time-dependences:

$$y_{CP} = \frac{\Gamma(CP \text{ even}) - \Gamma(CP \text{ odd})}{\Gamma(CP \text{ even}) + \Gamma(CP \text{ odd})} = \frac{\hat{\tau}(D \to \pi^+ K^-)}{\hat{\tau}(D \to K^+ K^-)} - 1 = y \cos \phi - x \sin \phi \, \frac{A_m}{2}$$

 $A_m = |q/p|^2 - 1$ and $\phi = \arg(q/p)$ parameterize CPV in mixing – very small in SM

$$\mathbf{Data:} \quad y_{CP} = \begin{cases} 0.8 \pm 3.1\% & \text{(E791)} \\ 3.4 \pm 1.6\% & \text{(FOCUS)} \\ -1.1 \pm 2.9\% & \text{(CLEO)} \\ -0.5 \pm 1.3\% & \text{(BELLE)} \\ -1.0 \pm 2.8\% & \text{(BABAR)} \end{cases} \qquad \mathbf{World average:} \\ y_{CP} = 0.65 \pm 0.85\%$$

Large y_{CP} could be explained by large y or large x, A_m , and ϕ



Recent measurements of $D^0 - \bar{D}^0$ mixing (2)

Measure time dependence of "wrong sign" DCS decays, e.g.: $D^0(t) \to K^+\pi^-$ and $\bar{D}^0(t) \to K^-\pi^+$. Fit three terms: $e^{-\Gamma t} \big\{ (\text{dir-DCS}) + (\Gamma t)(\text{int-CS}) + (\Gamma t)^2(\text{mix-CA}) \big\} \quad \text{(CLEO)}$ $x' = (0.0 \pm 1.5) \times 10^{-2}$ $y' \cos \phi = (-2.5^{+1.4}_{-1.6}) \times 10^{-2}$ $R = (0.48 \pm 0.13) \times 10^{-2}$ $A_m = 0.23^{+0.63}_{-0.80}$ $A_$

Large -y' could be explained by $y \sim -10^{-2}$ and $\delta \ll 1$ or $x \sim 10^{-2}$ and $\delta \sim 1$

The central values of the FOCUS and CLEO data together implied last year that both y and δ would have to be large independent of x [in SU(3) limit $\delta = 0$]



Theoretical status

SU(3) analysis & OPE predictions for D mixing

Dependence of sensitivity to NP on y and x

Allowed range of y (and x) in the SM

SU(3) analysis of D mixing

• Want to study: $\langle \bar{D}^0|T\{H_w,H_w\}|D^0\rangle = \langle 0|D\,T\{H_w,H_w\}D|0\rangle$

the field operator $D\in 3$ creates a D^0 or annihilates a $\bar D^0$

$$H(\Delta C = -1) = (\bar{q}_i c)(\bar{q}_j q_k) \in 3 \times \overline{3} \times \overline{3} = \overline{15} + 6 + \overline{3} + \overline{3}$$

If 3rd generation is neglected, only $\overline{15}$ and 6 appear in H

SU(3) breaking is introduced by $\mathcal{M}_{j}^{i} = \operatorname{diag}(m_{u}, m_{d}, m_{s}) \sim \operatorname{diag}(0, 0, m_{s})$

A pair of D operators is symmetric, so $D_iD_j \in 6$

A pair of H's is symmetric, so $H_k^{ij}H_n^{lm}\in\left[(\overline{15}+6)\times(\overline{15}+6)\right]_S\to\overline{60}+42+15'$

- 0. Since there is no $\overline{6}$ in $H_wH_w \Rightarrow D^0$ mixing vanishes in SU(3) limit
- 1. $DD\mathcal{M} \in 6 \times 8 = 24 + \overline{15} + 6 + \overline{3} \Rightarrow \text{ no invariants with } H_wH_w \text{ at order } m_s$
- **2.** $DD\mathcal{MM} \in 6 \times (8 \times 8)_S = 6 \times (27 + 8 + 1) = 60 + \overline{24} + \overline{15'} + \dots$

 $\Rightarrow D^0 - ar{D}^0$ mixing only arises at order m_s^2



Operator product expansion for D mixing

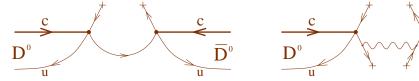
It is very hard to estimate x and y in the SM — they vanish in the SU(3) limit and are doubly Cabibbo suppressed: $x, y \sim \sin^2 \theta_C \epsilon_{SU(3)}^2$

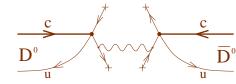
Short distance box diagram:
$$x \propto \frac{m_s^2}{m_W^2} \times \frac{m_s^2}{m_c^2} \to 10^{-5}$$

y has additional m_s^2/m_c^2 helicity suppression

Higher order terms in the OPE are suppressed by fewer powers of m_s : (Georgi '92)

	4-quark	6-quark	8-quark
$\frac{\Delta M}{\Delta M_{ m box}}$	1	$\frac{\Lambda^2}{m_s m_c}$	$\frac{\Lambda^4}{m_s^2 m_c^2} \frac{\alpha_s}{4\pi}$
$rac{\Delta\Gamma}{\Delta M}$	$\frac{m_s^2}{m_c^2}$	$\frac{\alpha_s}{4\pi}$	$\frac{\alpha_s}{4\pi}\beta_0$





(Bigi & Uraltsev '00 — argue that $x,y \propto m_s$ is possible; this is in conflict with our general proof from group theory)

With some assumptions about the matrix elements ($\Lambda \sim 4\pi f_{\pi}$): $x, y \lesssim 10^{-3}$

Long distance contributions to D mixing

• May be large, but extremely hard to estimate — SU(3) breaking has been argued to be $\mathcal{O}(1)$, based on $\mathcal{B}(D^0 \to K^+K^-)/\mathcal{B}(D^0 \to \pi^+\pi^-) \simeq 2.8$

Cancellations sensitively depend on poorly known strong phases and DCS rates:

$$y \approx \mathcal{B}(D \to \pi^+\pi^-) + \mathcal{B}(D \to K^+K^-) - 2\cos\delta\sqrt{\mathcal{B}(D \to K^-\pi^+)\mathcal{B}(D \to K^+\pi^-)}$$

Experimental central values yield: $y \approx (5.76 - 5.29 \cos \delta) \times 10^{-3}$

Assuming $\cos\delta \sim 1$ [the SU(3) limit] and that these intermediate states are representative, it is often stated that $x\lesssim y<\text{few}\times 10^{-3}$

- The most important long distance effect may be due to phase space:
 - Contrary to SU(3) breaking in matrix elements, this source of SU(3) violation is calculable model independently with only mild assumptions
 - Negligible for lightest PP final states; important for states with mass near m_D



What if $y\gg x$? The case of $|M_{12}/\Gamma_{12}|\ll 1$

• It is possible that the long distance contributions and SU(3) breaking are larger for y than for x, and could significantly enhance the OPE estimate of y

This may be unique, since in the K system $M_{12} \sim \Gamma_{12}$, in the B system $\Gamma_{12} \ll M_{12}$

New physics can significantly modify x, in particular, with new CPV phases

- It is very unlikely for NP to significantly modify y
- Observing $\phi \neq 0$ may be the best hope to find NP
- Solving the eigenvalue equation:
 - If $x\gg y$, the CPV phase can be LARGE: $\phi=\arg(M_{12})+\mathcal{O}(\Gamma_{12}^2/M_{12}^2)$
 - If $y\gg x$, the CPV phase is small: $\phi=\mathcal{O}(M_{12}^2/\Gamma_{12}^2) imes\sin[2\arg(M_{12}/\Gamma_{12})]$!
- If $y \gg x$ then even if new physics dominates M_{12} , the sensitivity of any physical observable to it is suppressed by x/y



$\Delta\Gamma$ from SU(3) breaking in phase space

• Phase space difference between final states containing fewer or more strange quarks is a calculable source of SU(3) breaking — these are "threshold effects"

• Let F_R denote final state F in representation R (e.g., PP can be in 8 or 27)

$$y_{F,R} = \frac{\sum_{n \in F_R} \langle D^0 | H_w | n \rangle \rho_n \langle n | H_w | D^0 \rangle}{\sum_{n \in F_R} \Gamma(D^0 \to n)}$$

the "would-be" value of y, if D only decayed to the states F in representation R

• If the decay rates to all representations are known, we can reconstruct the value of y from $y_{F,R}$:

$$y = \frac{1}{\Gamma} \sum_{F,R} y_{F,R} \left[\sum_{n \in F_R} \Gamma(D^0 \to n) \right]$$



Simplest example: $D^0 \rightarrow PP$

- PP must be in $(8 \times 8)_S = 27 + 8 + 1$ possible amplitudes:
 - PP in 27 and \mathcal{H}_w in $\overline{15}$: $A_{27} (PP_{27})_{ij}^{km} H_k^{ij} D_m$
 - $\begin{array}{l} \textbf{-} \ PP \ \text{in 8 and} \ \mathcal{H}_w \ \text{in} \ \overline{15} \hbox{:} \ A_8^{\overline{15}} \, (PP_8)_i^k \, H_k^{ij} \, D_j \\ \textbf{-} \ PP \ \text{in 8 and} \ \mathcal{H}_w \ \text{in 6:} \ A_8^6 \, (PP_8)_i^k \, H_k^{ij} \, D_j \end{array} \right\} \ \text{proportional to each other}$

So effectively there are only two amplitudes — for example, we obtain for $y_{PP,8}$:

$$s_1^2 \left[\frac{1}{2} \Phi(\eta, \eta) + \frac{1}{2} \Phi(\pi^0, \pi^0) + \frac{1}{3} \Phi(\eta, \pi^0) + \Phi(\pi^+, \pi^-) + \Phi(K^+, K^-) - \frac{1}{6} \Phi(\eta, K^0) - \frac{1}{6} \Phi(\eta, \bar{K}^0) - \Phi(K^+, \pi^-) - \Phi(K^-, \pi^+) - \frac{1}{2} \Phi(K^0, \pi^0) - \frac{1}{2} \Phi(\bar{K}^0, \pi^0) \right] \times \left[\frac{1}{6} \Phi(\eta, \bar{K}^0) + \Phi(K^-, \pi^+) + \frac{1}{2} \Phi(\bar{K}^0, \pi^0) + \mathcal{O}(s_1^2) \right]^{-1}$$

Result is explicitly proportional to $s_1^2 \equiv \sin^2 \theta_C$ and vanishes in SU(3) limit (as m_s^2)



Two-body final states

Final state repres	$y_{F,R}$ (%)	
$(PP)_{s-wave}$	8	-0.018
	27	-0.0034
$\overline{(PV)}$ p-wave	8_S	0.15
	8_A	0.15
	10	0.10
	$\overline{10}$	0.08
	27	0.19
$\overline{(VV)_{S}}$ -wave	8	-0.39
	27	-0.30
(VV)p-wave	8	-0.48
	27	-0.70
$(VV)_{\sf d}$ -wave	8	2.5
	27	2.8

Results for lightest multiplets, assuming no SU(3) breaking in matrix elements

Contribution of PP final states is "anomalously" small

Widths of vector mesons are important and taken into account (straightforward)

PV and VV channels effectively include resonant part of 3– and 4–body final states

Larger SU(3) breaking expected in heavier multiplets when some final states are not allowed at all



Multi-body final states

Final state representation		$y_{F,R}$ (%)	Consider simplest representations only
$\overline{(3P)_s}$ -wave	8	-2.3	Consular representations to all to sive
	27	-0.54	Smaller representations tend to give
$(3P)_p$ -wave	8	-5.5	larger effects
_	27	-0.36	Assuming a "form factor suppression" in
$^{(3P)}$ form-factor	8	-2.1	the matrix element, $\Pi_{i \neq j} (1 - m_{ij}^2/Q^2)^{-1}$,
	27	-0.64	where $m_{ij}^2=(p_i+p_j)^2$ and $Q=2{ m GeV}$,
4P	8	16	changes the results only moderately
	27	9.2	For $4P$, only consider fully symmetric
	27'	11	final state
			- III al Stato

• For many final state representations, especially those close to threshold, "large" effects are possible, i.e., $y_{F,R}$ at the percent level is not unusual



Conclusions from our analysis

• The 2–, 3–, and 4–body final states account for a large fraction of the D width Rounded to nearest 5%:

Final state	fraction
PP	5%
PV	10%
$\overline{(VV)_s}$ -wave	5%
$(VV)_d$ -wave	5%
3P	5%
4P	10%

There are other large rates near threshold, e.g.: $\mathcal{B}(D^0 \to K^- a_1^+) = (7.3 \pm 1.1)\%$

• Morals: There are final states that can contribute to y at the 1% level \Rightarrow It would require cancellations to suppress y_{CP} much below $\sim 1\%$



Conclusions

- For the first time there is a concrete calculation without ad hoc assumptions showing that $\Delta\Gamma/\Gamma$ can naturally be at the 1% level
 - Next: calculate ΔM from this source of SU(3) breaking using dispersion relation
- Standard Model predictions of Δm and $\Delta \Gamma$ remain uncertain \Rightarrow measurements of nonzero Δm or $\Delta \Gamma$ alone cannot be interpreted unambiguously as new phayics
- To disentangle New Physics from Standard Model contribution, it's crucial to try to
 - ... Improve measurements of both Δm and $\Delta \Gamma$
 - ... Extract strong phase simultaneously in $K^-\pi^+\pi^0$ Dalitz plot analysis
 - ... Look for CP violation, which remains a potentially robust signal of new physics

BaBar and Belle should be able to do this!

