
Measurements of CP
Asymmetries and Branching
Fractions in $B^0 \rightarrow p^+ p^-, K^\pm p^\mp, K^+ K^-$

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BaBar Collaboration

Measuring CP Violation with Neutral B's

- CP violation arises from a **single phase** in CKM matrix:

Wolfenstein Parameterization

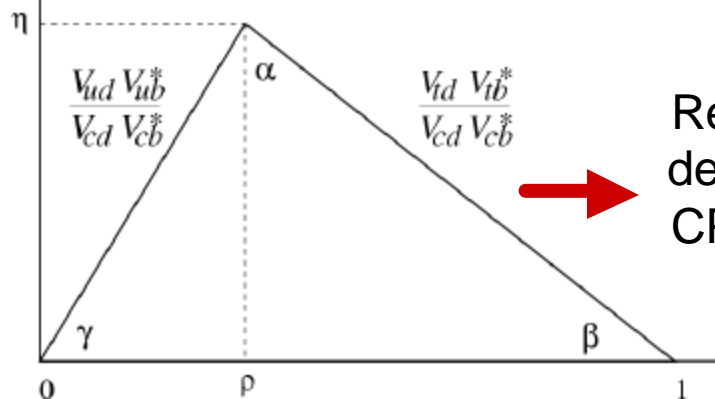
$$\mathbf{V} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{2} & A\lambda^3(r - ih) \\ -\frac{1}{\sqrt{2}} & \frac{1}{2} & A\lambda^2 \\ A\lambda^3(1 - r - ih) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

Complex Phase

Unitarity

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

Represented as triangle



Relate angles to decays of B's to CP Eigenstates

Measuring Angles with B⁰'s

$$A_{f_{CP}} = \frac{\Gamma(\bar{B}_{phys}^0(t) \rightarrow f_{CP}) - \Gamma(B_{phys}^0(t) \rightarrow f_{CP})}{\Gamma(\bar{B}_{phys}^0(t) \rightarrow f_{CP}) + \Gamma(B_{phys}^0(t) \rightarrow f_{CP})}$$

Look for time-dependent decay asymmetry

Oscillate w/ mixing freq

CP Eigenstate

$$= S_{f_{CP}} \sin \Delta m_d t - C_{f_{CP}} \cos \Delta m_d t$$

Amplitudes:

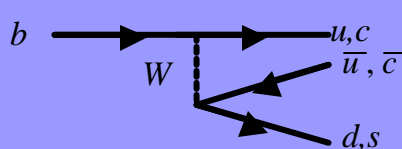
$$C_{f_{CP}} = \frac{1 - |?_{f_{CP}}|^2}{1 + |?_{f_{CP}}|^2}$$

$$S_{f_{CP}} = \frac{2 \text{Im } I_{f_{CP}}}{1 + |I_{f_{CP}}|^2}$$

Carry CPV Info

Decay amplitude ratio

$$?_{f_{CP}} = \frac{q}{p} \cdot \frac{A_{f_{CP}}}{A_{f_{CP}}}$$

Mode	? _{f_{CP}} Tree 	Im(? _{f_{CP}})
B ⁰ → J/ψ K _s	$-\frac{V_{td} V_{tb}^*}{V_{tb} V_{td}^*} \frac{V_{cb} V_{cs}^*}{V_{cs} V_{cb}^*} \frac{V_{cd} V_{cd}^*}{V_{cd} V_{cd}^*}$	sin 2b
B ⁰ → p ⁺ p ⁻	$\frac{V_{td} V_{tb}^*}{V_{tb} V_{td}^*} \frac{V_{ud} V_{ub}^*}{V_{ud} V_{ub}^*}$	sin 2a

Next Leading Diagram

Mode	Tree Amplitude (T)	Hadronic Penguin Amplitude (P)
$B^0 \rightarrow J/\psi K_s$	$\sim V_{cb} V_{cs}^* \approx ?^2$	$\sim ?^2 + O(?^4) e^{-i?}$
$B^0 \rightarrow p^+ p^-$	$\sim V_{ub} V_{ud}^* \approx ?^3 e^{-i?}$	$\sim V_{tb} V_{td}^* \approx ?^3 e^{i\beta}$
$B^0 \rightarrow K^+ p^-$	$\sim V_{ub} V_{us}^* \approx ?^4 e^{-i?}$	$\sim V_{tb} V_{ts}^* \approx ?^2$

- In the case of $B^0 \rightarrow J/\psi K_s$ Tree/Penguin carry **same** phase \rightarrow Measure $\sin 2\beta$
- $Br(B^0 \rightarrow K^+ \pi^-) \gg Br(B^0 \rightarrow \pi^+ \pi^-)$ \rightarrow Penguin contributions may be **large**
- But for $B^0 \rightarrow \pi^+ \pi^-$ Tree/Penguin may contribute w/ **different** phases

$$\Rightarrow ?_{pp} = e^{2ia} \frac{1 - \frac{P}{T} e^{i(d-a)}}{1 - \frac{P}{T} e^{i(d+a)}} \equiv |?_{pp}| e^{2ia_{\text{Eff}}} \leftarrow \text{“}\alpha \text{ Effective”}$$

■ Charmless 2-body B decays:

- $B^0 \rightarrow \pi^+ \pi^-$ sensitive to $\sin 2\alpha$
- $B^0 \rightarrow K^+ \pi^-$ may exhibit direct CP violation:

$$A_{Kp} = \frac{G(\bar{B}^0 \rightarrow K^- p^+) - G(B^0 \rightarrow K^+ p^-)}{G(\bar{B}^0 \rightarrow K^- p^+) + G(B^0 \rightarrow K^+ p^-)}$$

- The Branching Fractions may help $\alpha_{\text{Eff}} \rightarrow \alpha$ and $Br \rightarrow \gamma$

■ In ~60 Million B Decays (~55/fb) recorded w/ BaBar

- Extracted the Branching Fractions
- Measured asymmetry $A_{K\pi}$
- Measured the time dependent asymmetries $S_{\pi\pi}$ and $C_{\pi\pi}$

■ All results are preliminary

Analysis Issues

Looking for $B \rightarrow \pi\pi, K\pi, KK$ is very different than looking for $B \rightarrow J/\psi K_s$:

- Rare Decays: Br 's $\sim 10^{-5} - 10^{-6}$

→ Maximize efficiency: loose selection + global likelihood fit.

- Large background from

$$e^+e^- \rightarrow q\bar{q}, \quad (q = u, d, s, c)$$

→ Use multivariate techniques to discriminate against background.

- Must separate $B \rightarrow \pi^+\pi^-, K^+\pi^-, K^-\pi^+, K^+K^-$

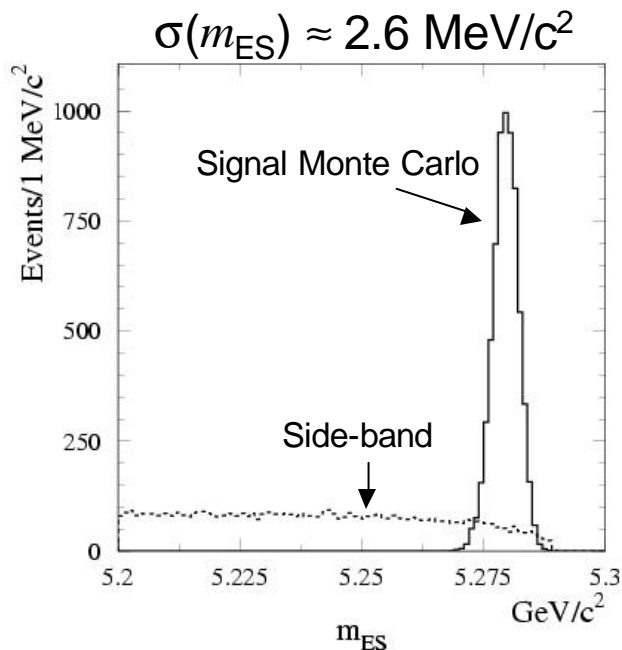
→ BaBar's Ring Imaging Cherenkov detector (DIRC)

Kinematics

$$m_{ES} = \sqrt{E_{\text{beam}}^{*2} - p_B^{*2}}$$

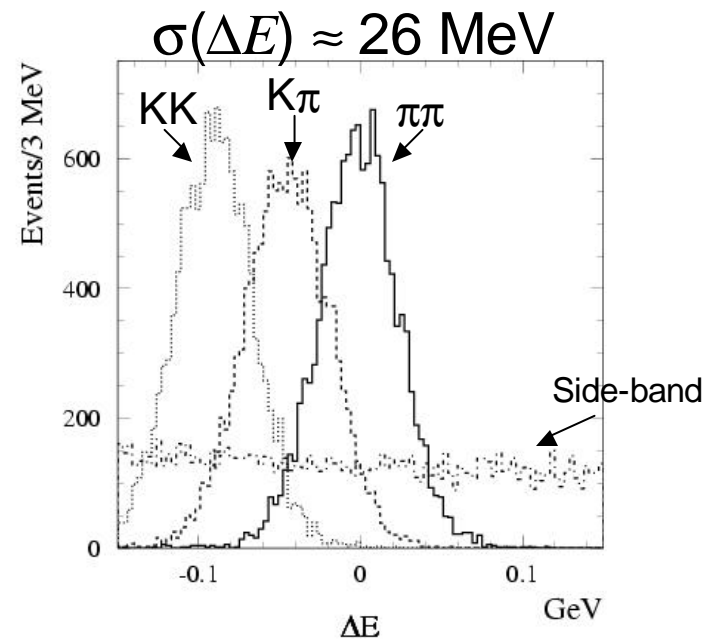
$\approx 325 \text{ MeV}$

- Resolution dominated by the small uncertainty in beam energy



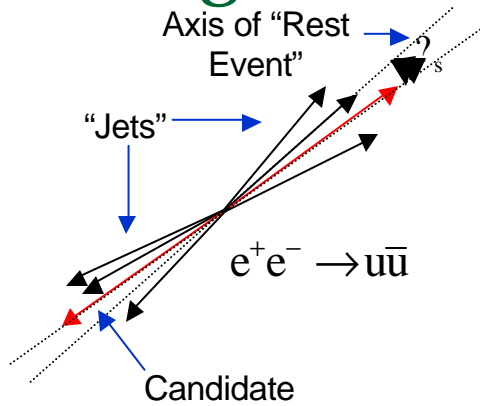
$$\Delta E = E_B^* - E_{\text{beam}}^*$$

- Dominated by tracking resolution
- Assume $\pi\pi$ mass
- Momentum dependent shift for $K\pi$ and KK

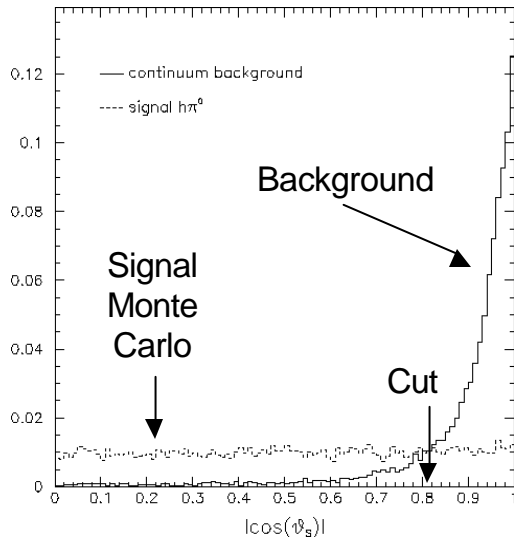
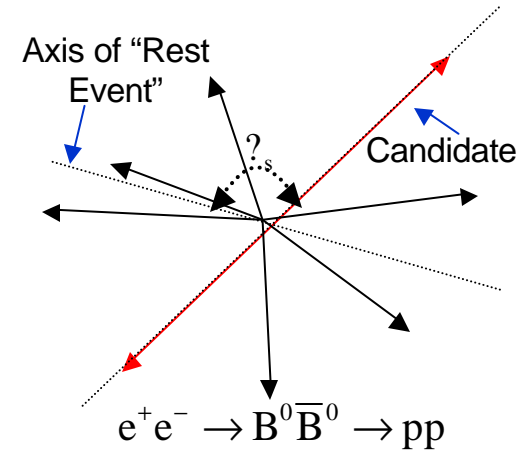


(All distributions are normalized to the same area)

Background Suppression

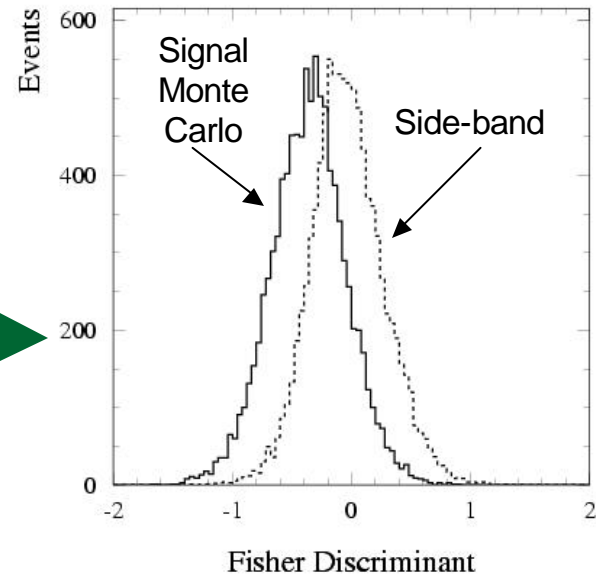


■ All background from $e^+e^- \rightarrow q\bar{q}$, ($q = u, d, s, c$) where picked 1 track from each fragmenting quark



← Angle btw candidate and "Rest of Event" axes. ($\cos \theta_s$)

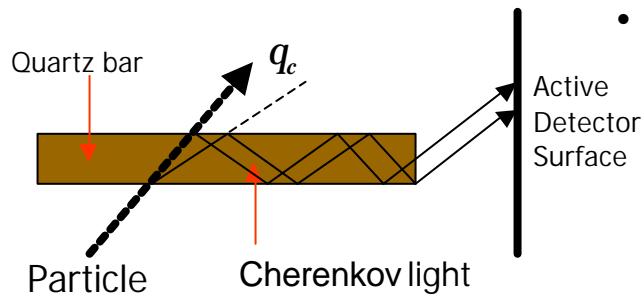
Optimized linear combination of energy flow into cones about candidate. (Fisher Discriminant)



(All distributions are normalized to the same area)

Particle Identification (DIRC)

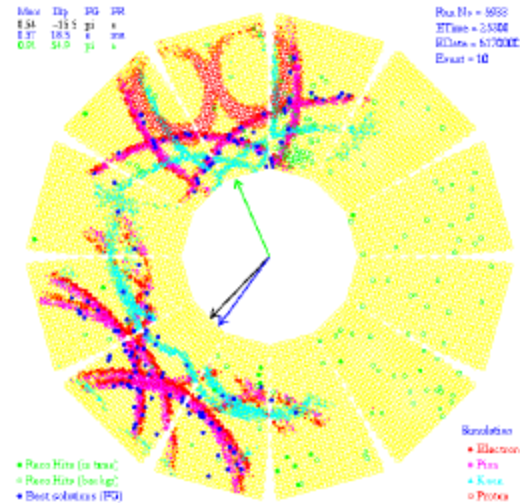
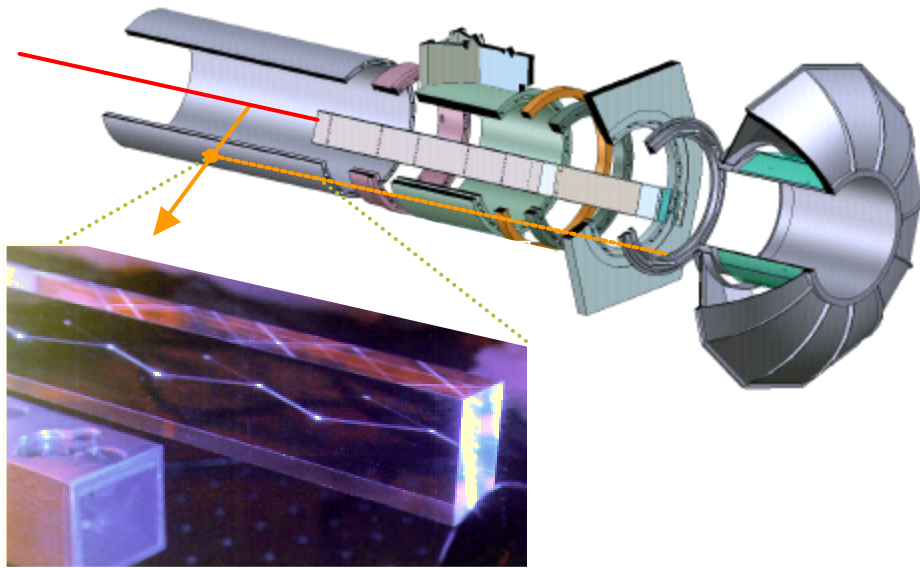
(Detector of Internally Reflected Cherenkov Light)



- Measure Angle of Cherenkov Cone in quartz

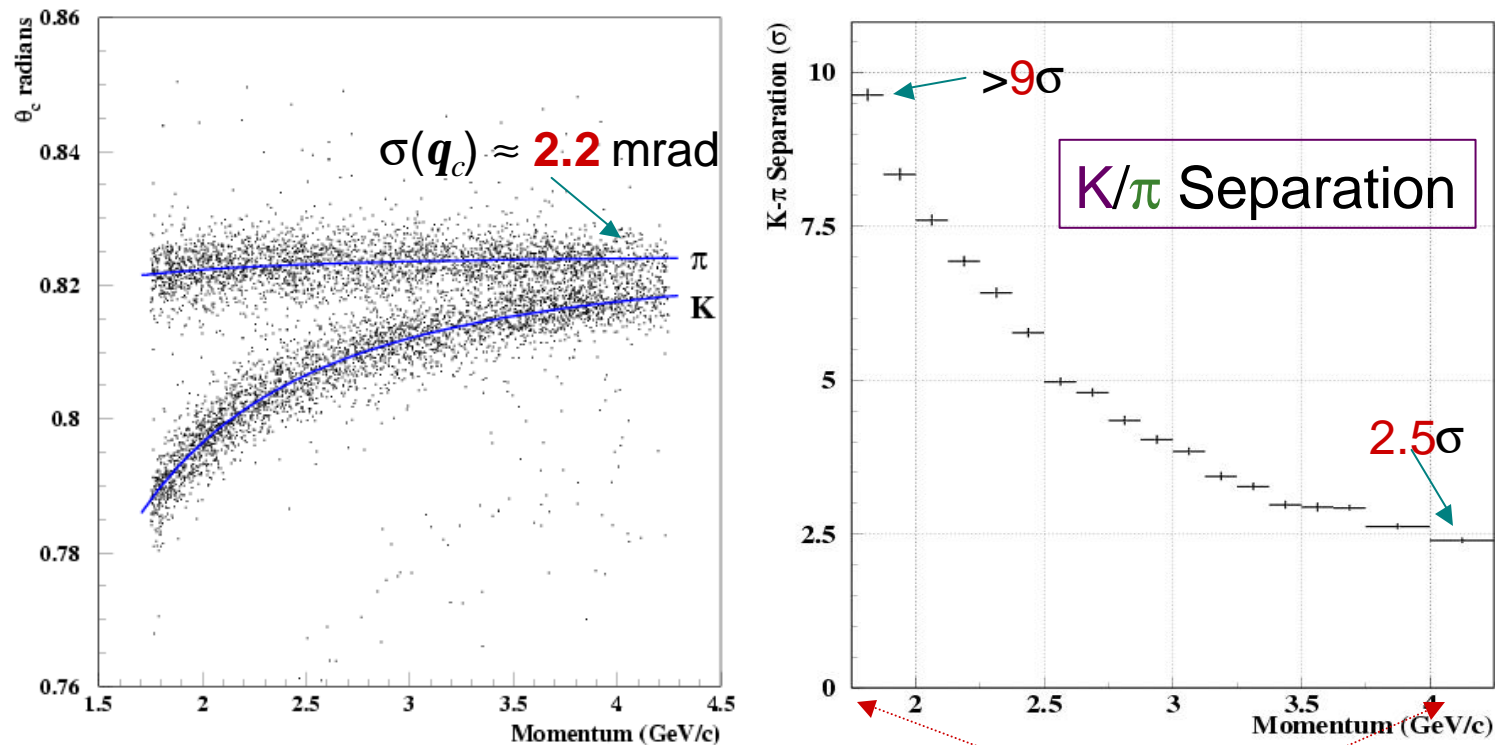
$$\cos \theta_c = \frac{1}{n\beta}, p = m\beta\gamma$$

- Transmitted by internal reflection
- Detected by PMTs



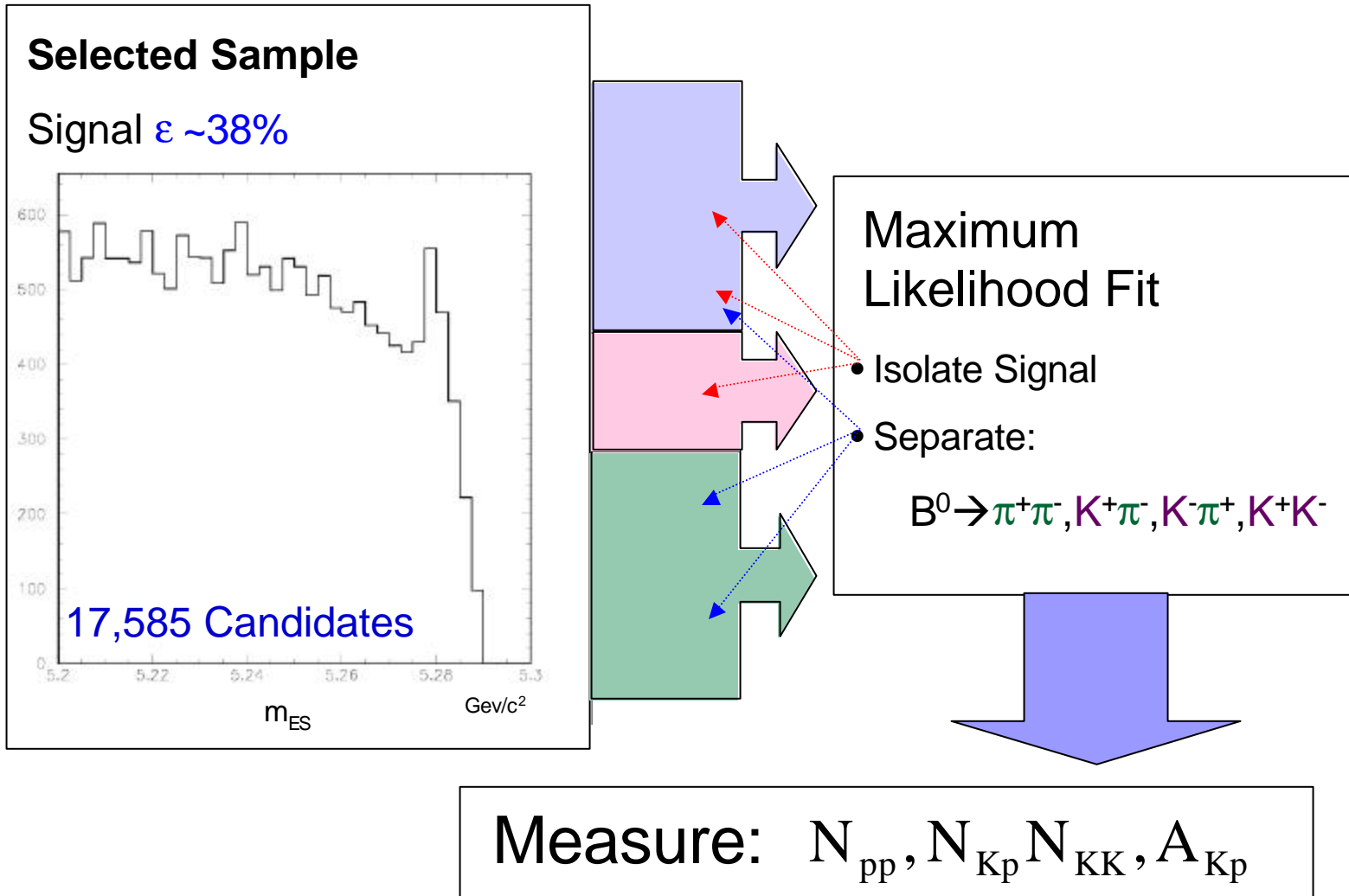
Particle Identification (DIRC) cont'.

- DIRC θ_c resolution and $K-\pi$ separation measured in data $\Rightarrow D^{*+} \rightarrow D^0 \pi^+ \rightarrow (K^- \pi^+) \pi^+$ decays



Momentum range of 2-body B Decays at BaBar

Extracting the Branching Fractions



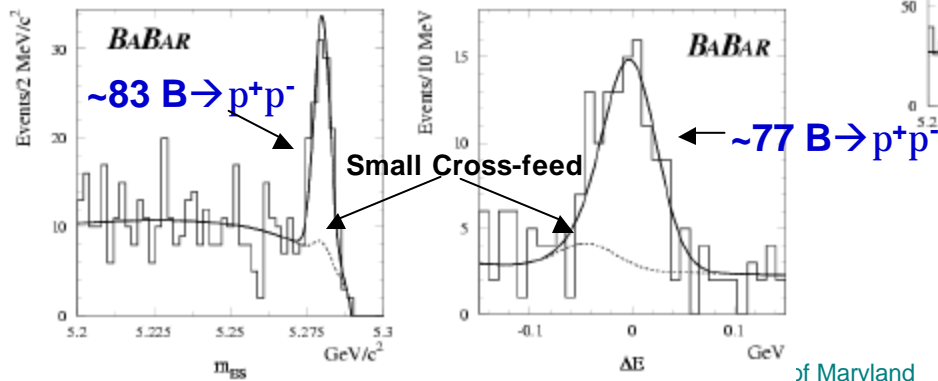
Branching Fraction Results

Mode	Yield	Branching Fraction (10 ⁻⁶)	K π Asymmetry ($A_{K\pi}$)
$B^0 \rightarrow p^+ p^-$	124^{+16}_{-15}	$5.4 \pm 0.7 \pm 0.4$	
$B^0 \rightarrow K^+ p^-$	402.7 ± 24	$17.8 \pm 1.1 \pm 0.8$	$-0.05 \pm 0.06 \pm 0.01$
$B^0 \rightarrow K^+ K^-$	0.6^{+8}_{-7}	< 1.1 (90% CL)	

Likelihood projections:

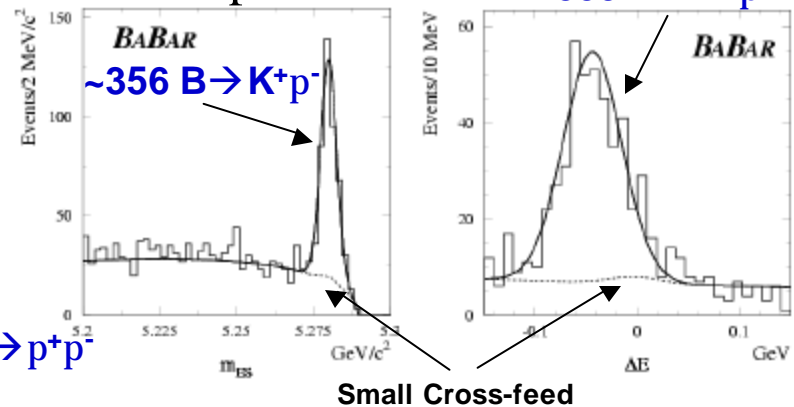
- Remove 1 variable from fit
- Cut on probabilities used in fit

$B^0 \rightarrow p^+ p^-$



Consistent with CLEO, Belle, and BaBar PRL

$B^0 \rightarrow K^+ p^-$

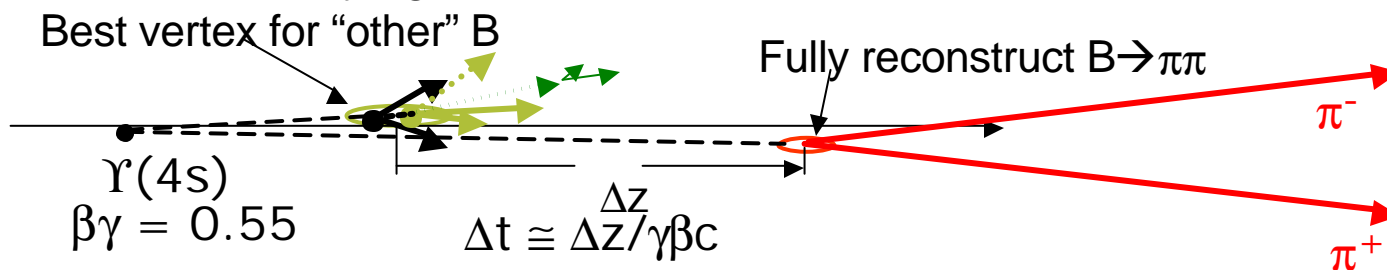


Measuring Time-dependent CP Violation

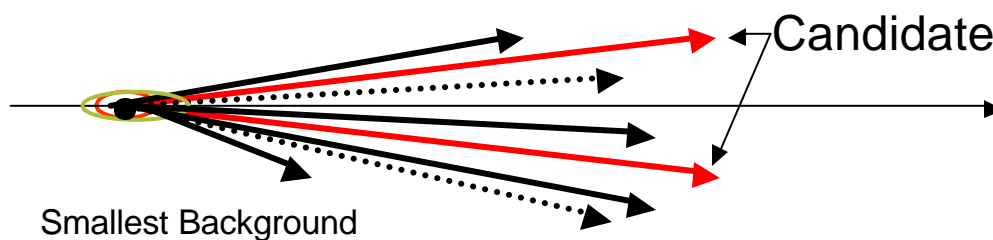
- Extend the Branching Fraction analysis to extract CP information
- Time-dependent analysis needs information on:
 - Time structure of the decays: Vertexing
 - Flavor content of the decays: Flavor tagging
- Use same techniques as BaBar's $\sin 2\beta$ analysis

Vertexing (Δt)

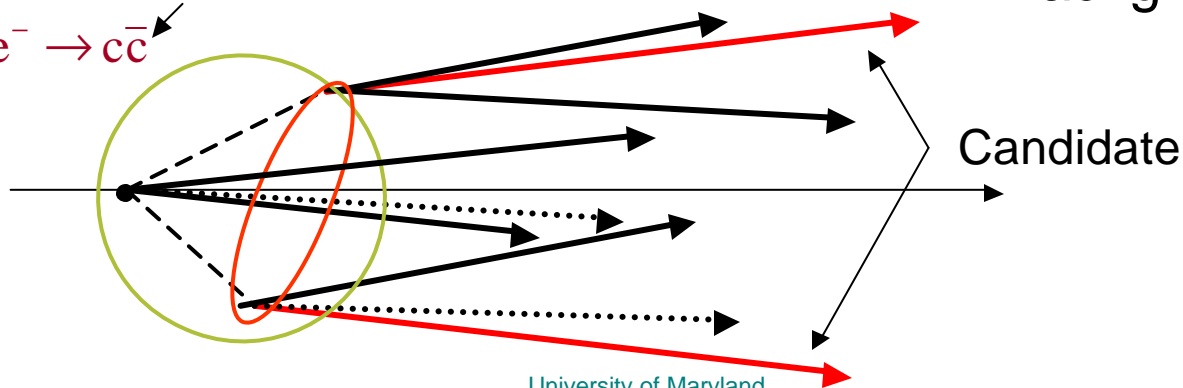
- **Signal**- We make flying B pairs



- $e^+e^- \rightarrow q\bar{q}$, ($q = u, d, s$)

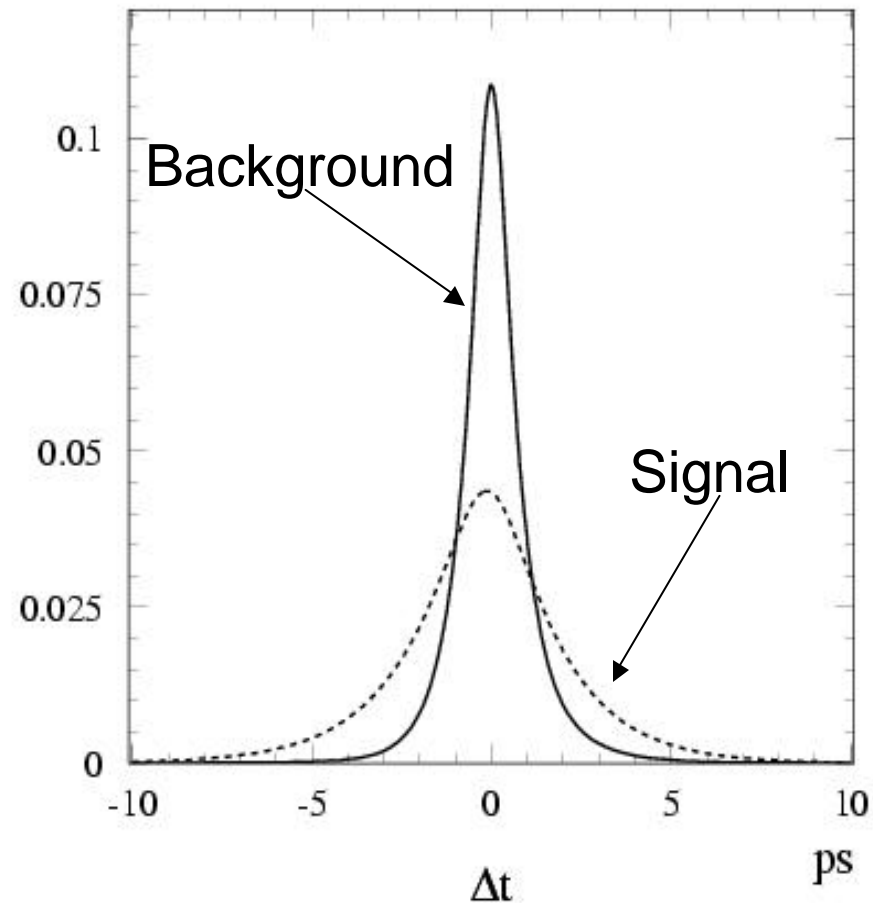


- $e^+e^- \rightarrow c\bar{c}$



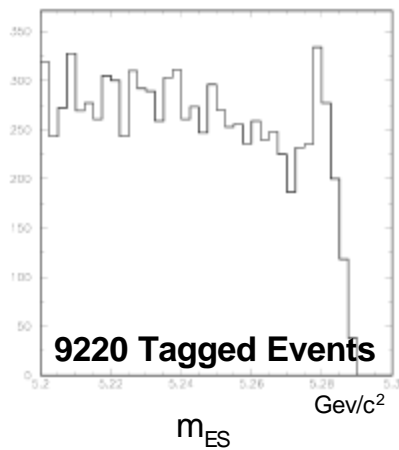
Vertexing (Δt) cont'.

- Since Δt resolution is **dominated** by the “*other*” B, **signal resolution** determined from **large** sample of **fully reconstructed B's** using same model as $\sin 2\beta$ analysis.
- Background shape determined from sidebands.



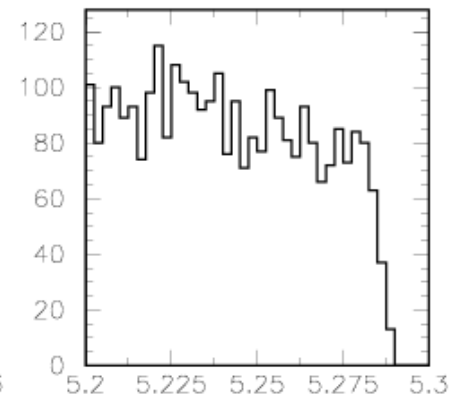
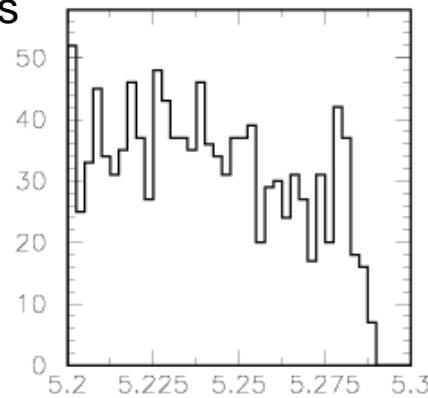
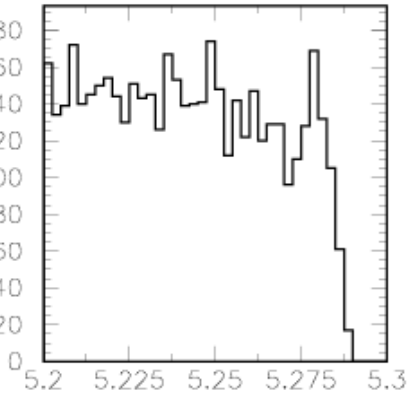
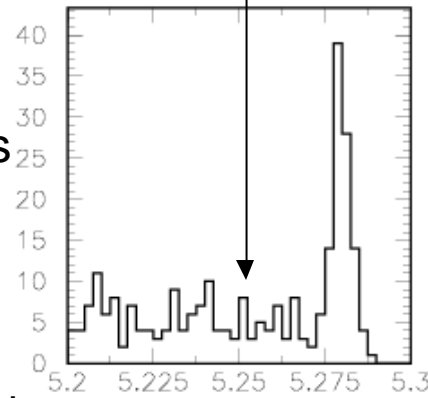
Flavor Tagging

- Use same flavor tagging as $\sin 2\beta$ measurement
- Look for **tracks** whose **charge** carry flavor information in various **categories**.



Separate into categories

Few **Leptons** in background



Multivariate Tag Categories

- Exploit mixing to measure signal performance (Dilutions) and efficiencies in **large** sample of **fully reconstructed B's**.

Mixing/Lifetime Validation

- Measure **B lifetime** using $B^0 \rightarrow p^+ p^- / K^\pm p^\mp$

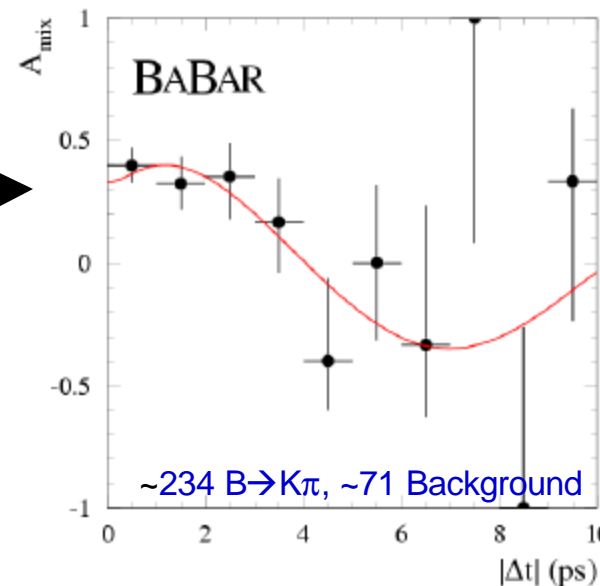
$$\Rightarrow t = 1.66 \pm 0.09 \text{ ps}$$

- Measure Δm_d using $B^0 \rightarrow K^+ p^-$

$$\Rightarrow \Delta m_d = 0.517 \pm 0.062 \text{ ps}^{-1}$$

Cross-check

Select $B \rightarrow K\pi$ sample and plot the asymmetry between mixed/unmixed events.

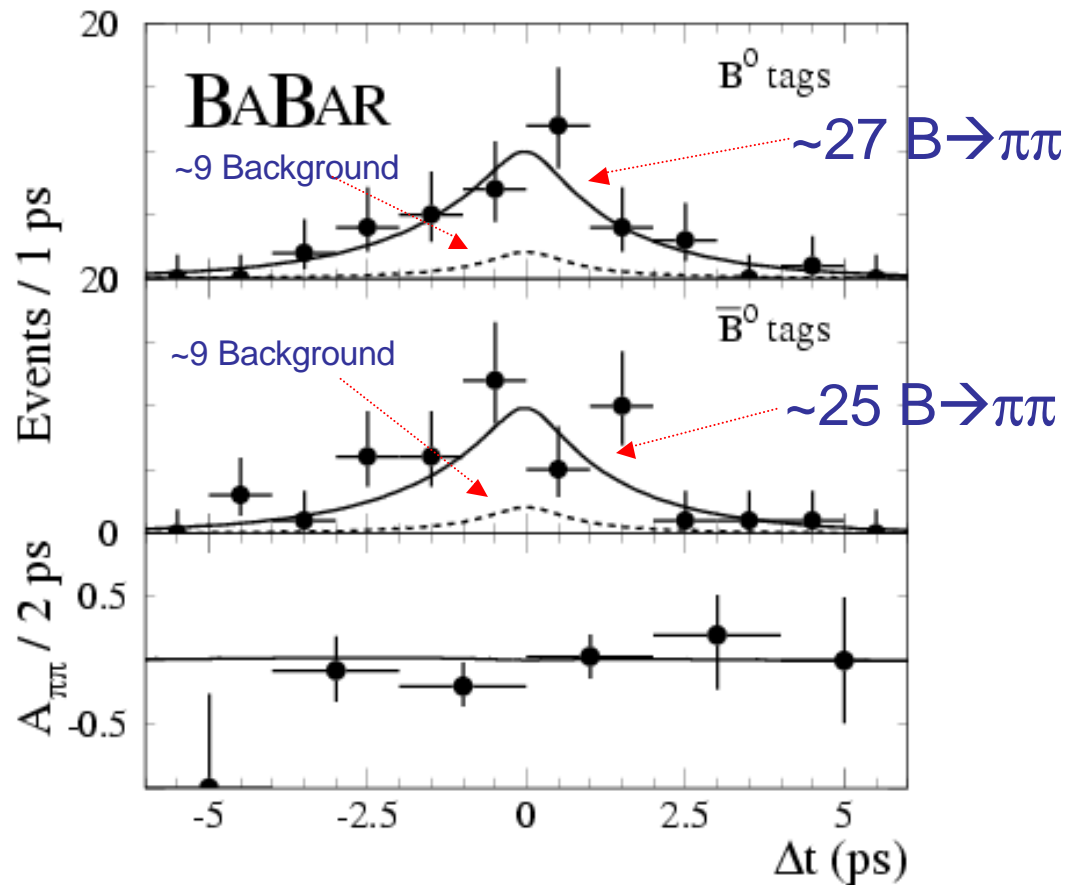


Time-dependent CP Measurement

$$S_{\pi\pi} = -0.01 \pm 0.37 \pm 0.07 \quad [-0.66, +0.62]$$

$$C_{\pi\pi} = -0.02 \pm 0.29 \pm 0.07 \quad [-0.54, +0.48]$$

90% CL



Select $B \rightarrow \pi\pi$ sample and plot the asymmetry between mixed/unmixed events.

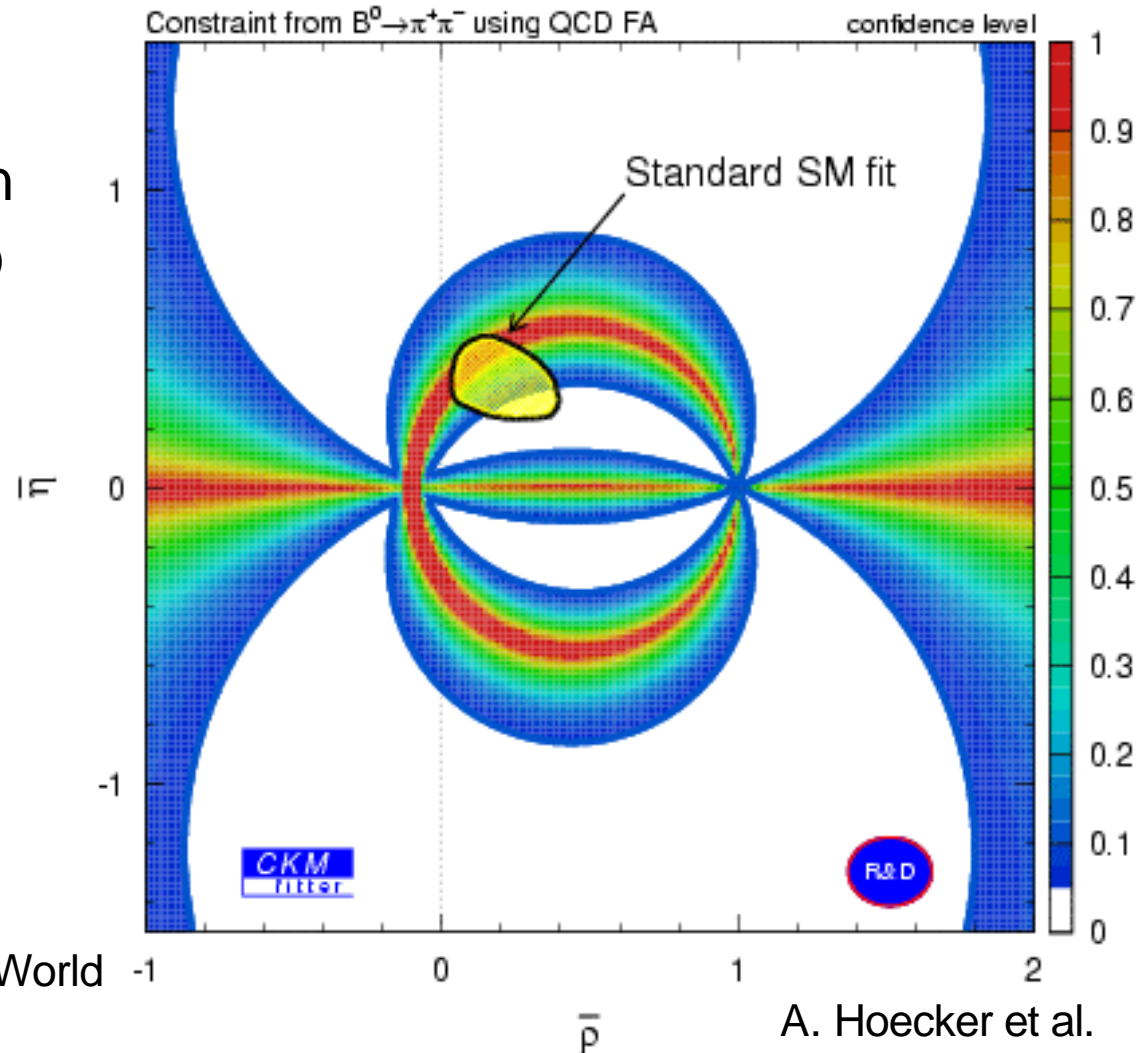
Time-dependent CP Measurement

Using $S_{\pi\pi}$ and
QCD Factorization
(BBNS)

“Standard SM fit”:

- ε
- V_{ub}/V_{cb}
- Δm_d
- Δm_s
- $\sin 2\beta$

Summer World
Average



A. Hoecker et al.

Summary of Results

$$S_{pp} = -0.01 \pm 0.37 \pm 0.07 [-0.66, +0.62]$$

$$C_{pp} = -0.02 \pm 0.29 \pm 0.07 [-0.54, +0.48]$$

$$A_{Kp} = -0.05 \pm 0.06 \pm 0.01 [-0.15, +0.05]$$

Belle: Not sure about signs

$$S_{\pi\pi} = -1.21^{+0.38}_{-0.27} \quad {}^{+0.16}_{0.13}$$

$$-C_{\pi\pi} = 0.94^{+0.25}_{-0.31} \quad +/-0.09$$

90% CL

Mode	BaBar (10^{-6}) (60M B's)	CLEO (10^{-6}) (9.66M B's)	Belle (10^{-6}) (11.1M B's)
$B^0 \rightarrow p^+ p^-$	$5.4 \pm 0.7 \pm 0.4$	$4.3^{+1.6}_{-1.5} \pm 0.5$	$5.9^{+2.4}_{-2.1} \pm 0.5$
$B^0 \rightarrow K^+ p^-$	$17.8 \pm 1.1 \pm 0.8$	$17.2^{+2.5}_{-2.4} \pm 1.2$	$18.7^{+3.3}_{-3.0} \pm 1.6$
$B^0 \rightarrow K^+ K^-$	< 1.1 (90% CL)	< 1.9	< 2.7