

W Couplings at LEP

Tim Barklow

SLAC

For the Four LEP Collaborations ADLO

**39th Rencontres De Moriond On Electroweak
Interactions And Unified Theories**

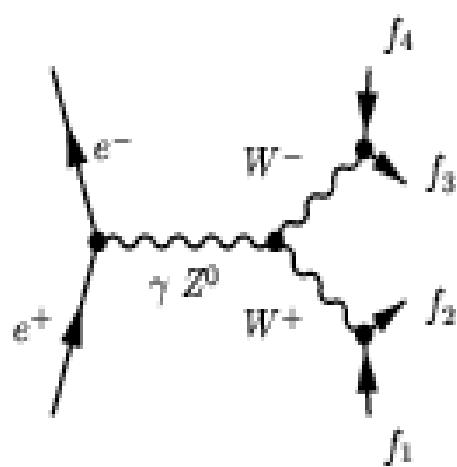
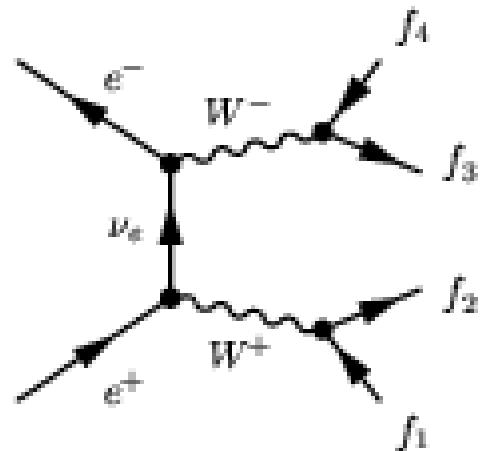
22 Mar 2004, La Thuile, Aosta Valley, Italy

Topics

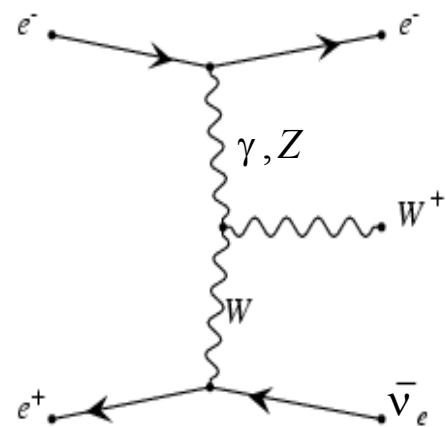
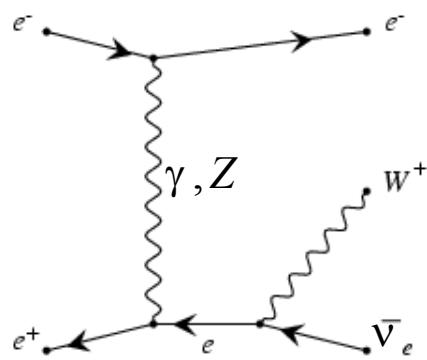
- W Pair Production Cross Section
- W Branching Fractions
- WW γ Cross Section and Limits on Quartic Gauge Boson Couplings
- W Polarization
- Triple Gauge Couplings and Technipion Form Factor

W Boson Production at LEP2

- $e^+e^- \rightarrow W^+W^-$

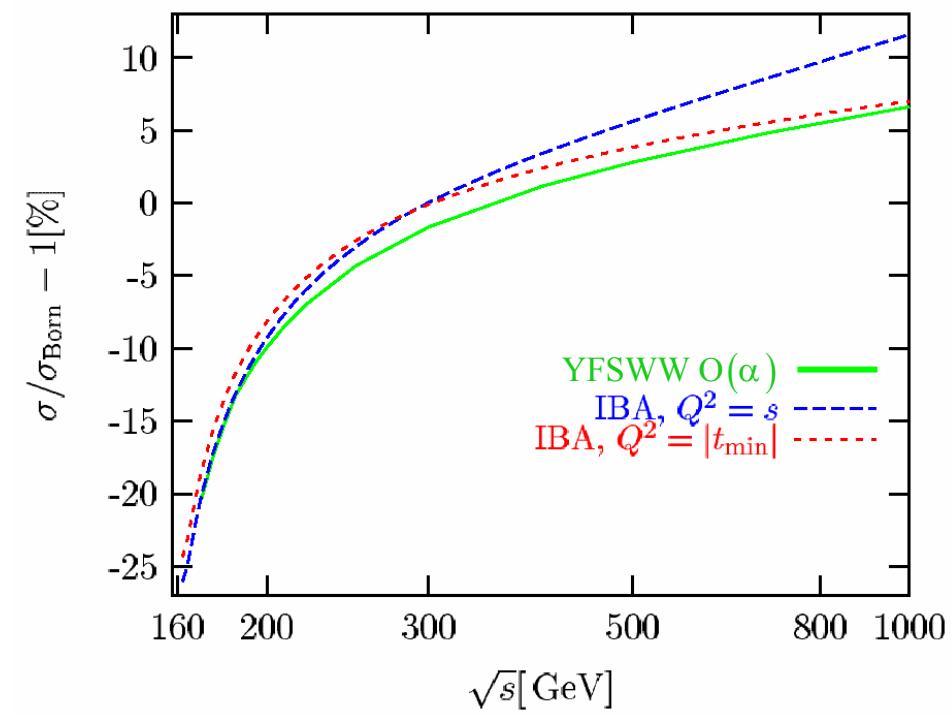


- $e^+e^- \rightarrow We\nu_e$



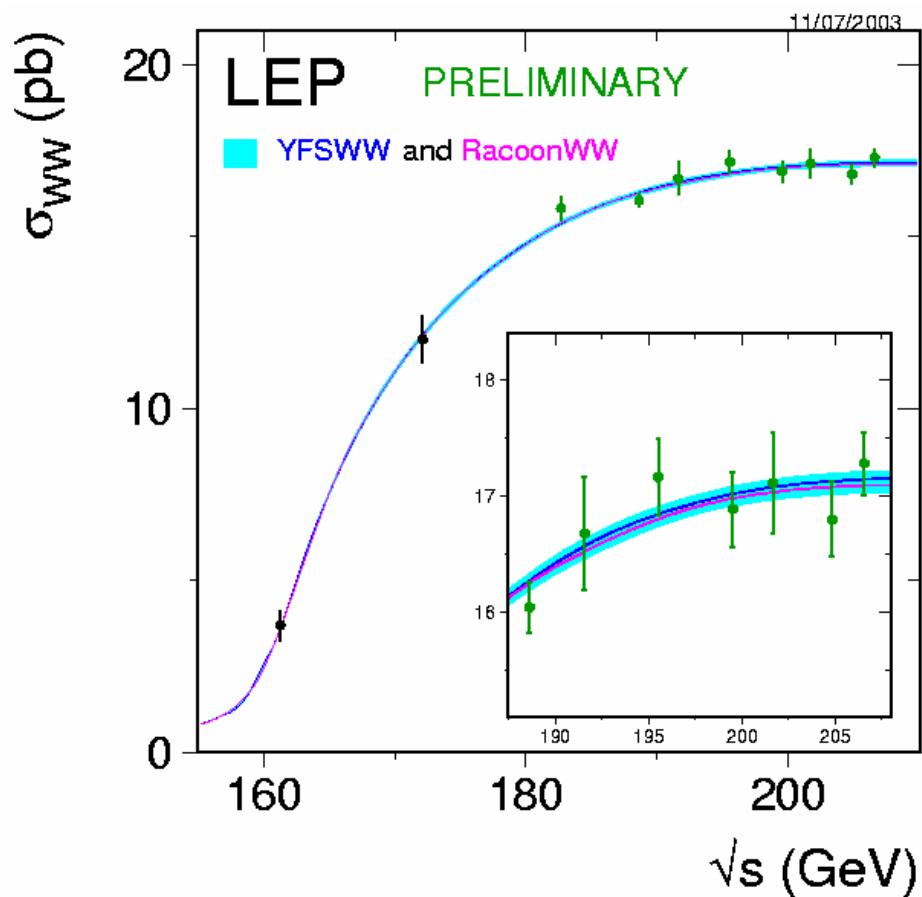
WW Cross Section

Theory cross sec **with** and
without $\mathcal{O}(\alpha)$ corrections:

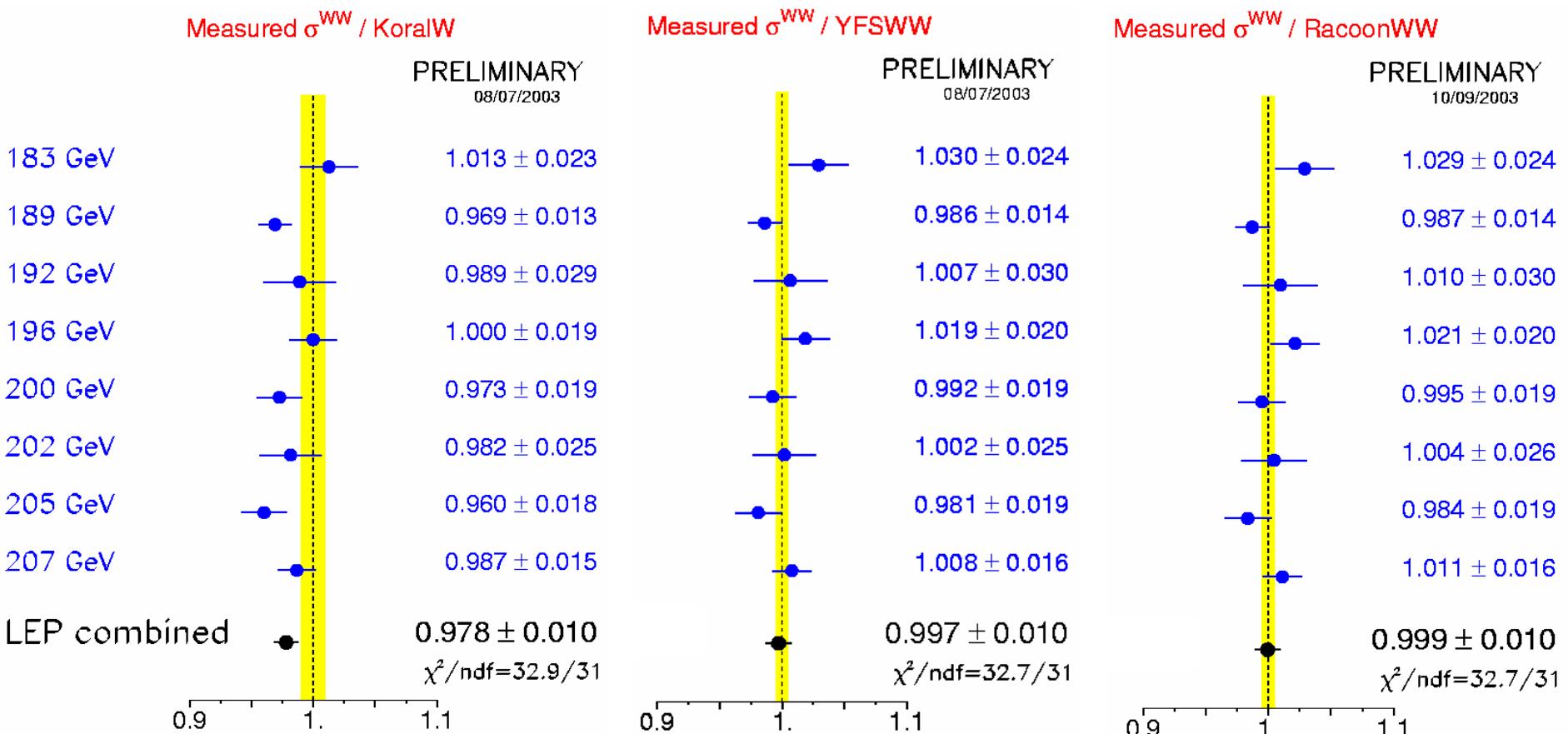


LEP Combination

DELPHI results are final



WW Cross Section

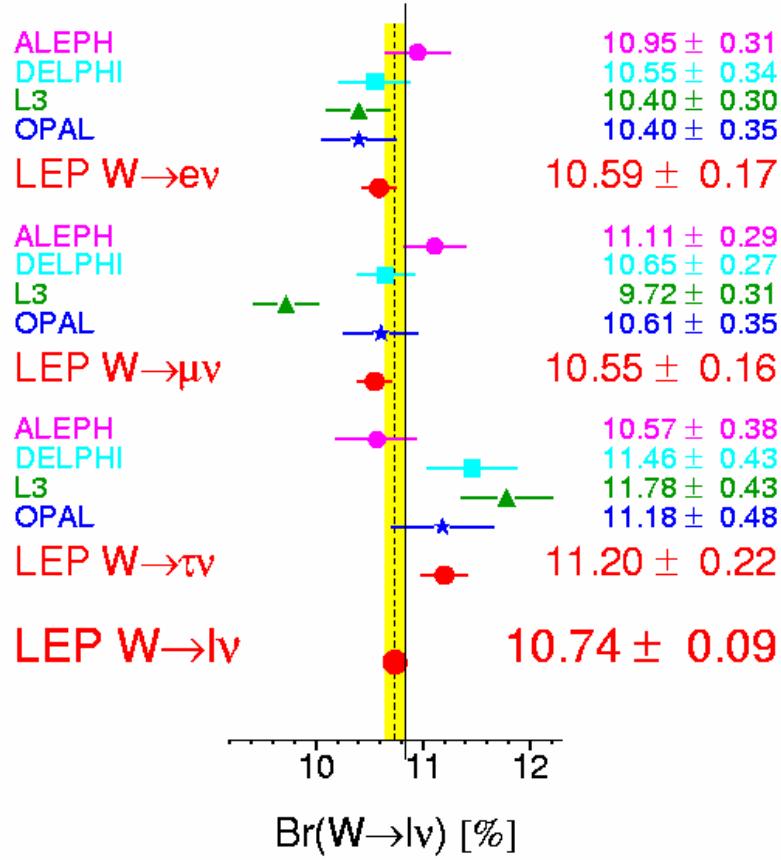


W Branching Fractions

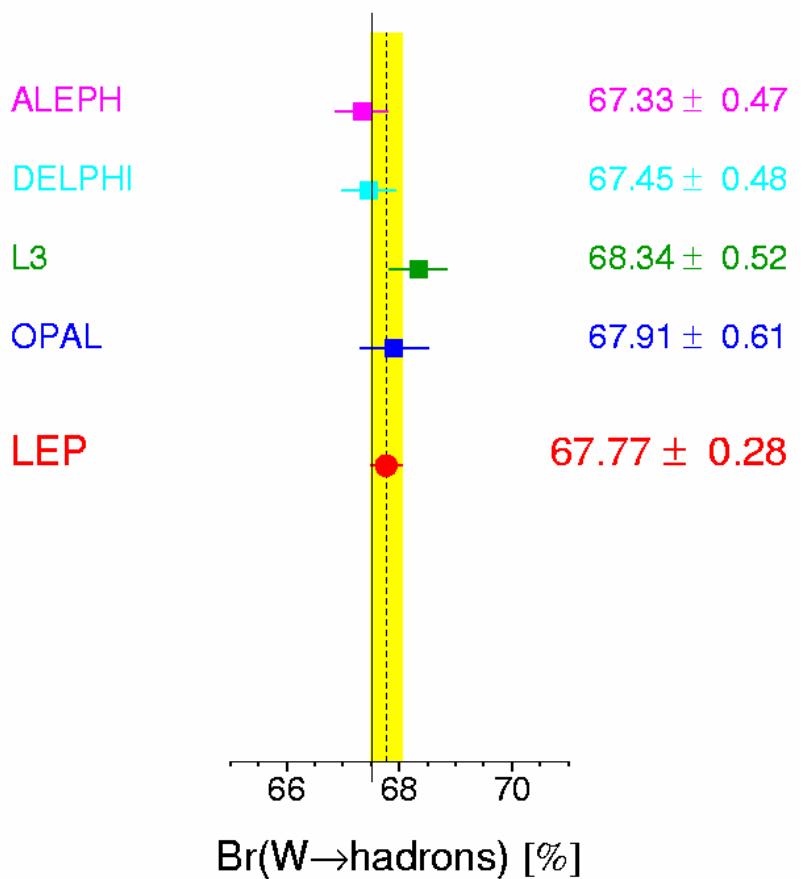
SM: $Br(W \rightarrow l\nu) = 10.83\%$

$Br(W \rightarrow hadrons) = 67.51\%$

W Leptonic Branching Ratios



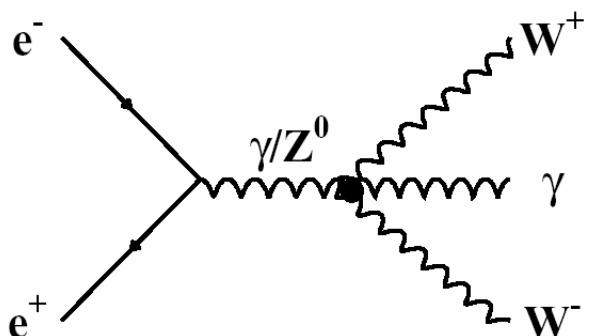
$Br(W \rightarrow \text{hadrons}) [\%]$



$$\rightarrow |V_{cs}| = 0.989 \pm 0.014$$

$$e^+ e^- \rightarrow W^+ W^- \gamma$$

- Tests real photon radiative corrections to $e^+ e^- \rightarrow W^+ W^-$
- Probes very anomalous 4 gauge boson couplings $\gamma\gamma W^+ W^-$ and $\gamma Z W^+ W^-$



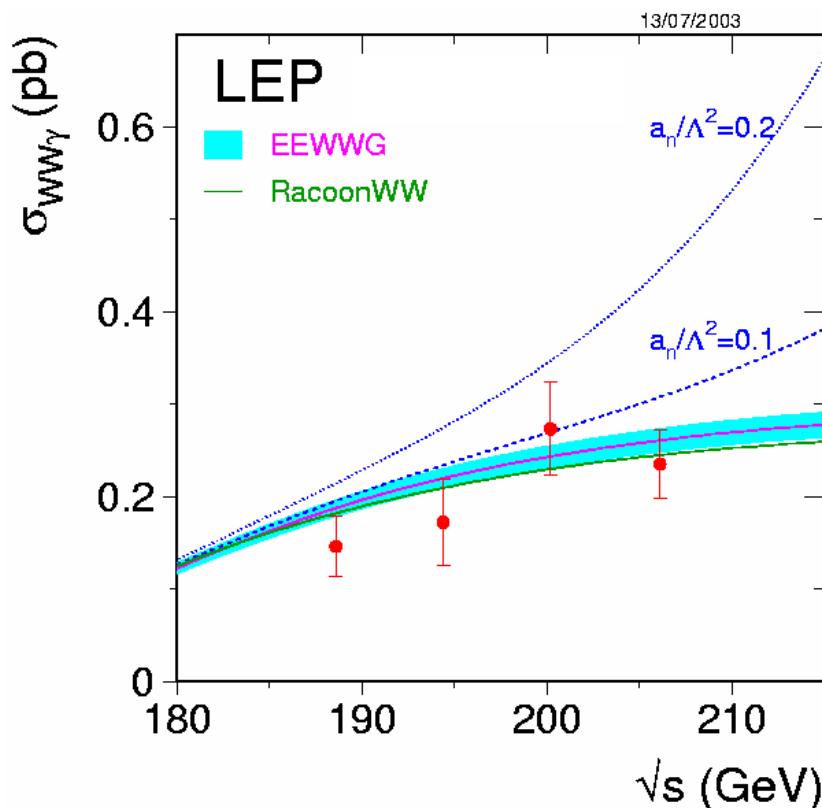
LEP Combination Signal Defn:

$E_\gamma > 5 \text{ GeV}$

$|\cos\theta_\gamma| < 0.95$

$|\cos\theta_{\gamma,f}| < 0.90$

$|M_{f,f'} - M_W| < 2\Gamma_W$



Final LEP Results (DLO)
on $W^+ W^- \gamma$ Cross Section

Lowest dimension operators involving photons which generate quartic gauge couplings but not triple gauge couplings:

$$\begin{aligned}\mathcal{L}_6^0 &= -\frac{e^2}{16\Lambda^2} a_0 F^{\mu\nu} F_{\mu\nu} \vec{W}^\alpha \cdot \vec{W}_\alpha , & \gamma\gamma W^+W^- \\ \mathcal{L}_6^c &= -\frac{e^2}{16\Lambda^2} a_c F^{\mu\alpha} F_{\mu\beta} \vec{W}^\beta \cdot \vec{W}_\alpha , & \gamma\gamma W^+W^- \\ \mathcal{L}_6^n &= i \frac{e^2}{16\Lambda^2} a_n \epsilon_{ijk} W_{\mu\alpha}^{(i)} W_\nu^{(j)} W^{(k)\alpha} F^{\mu\nu} & \gamma Z W^+W^-\end{aligned}$$

95% C.L. Limits on quartic couplings in GeV^{-2} from $W^+W^-\gamma$

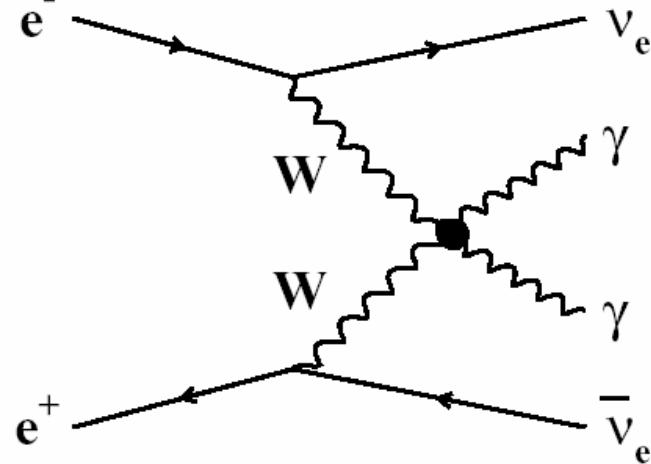
DELPHI

L3

OPAL

$-0.020 < a_0 / \Lambda^2 < 0.020$	$-0.017 < a_0 / \Lambda^2 < 0.017$	$-0.020 < a_0 / \Lambda^2 < 0.020$
$-0.063 < a_c / \Lambda^2 < 0.032$	$-0.052 < a_c / \Lambda^2 < 0.026$	$-0.053 < a_c / \Lambda^2 < 0.037$
$-0.180 < a_n / \Lambda^2 < 0.140$	$-0.140 < a_n / \Lambda^2 < 0.130$	$-0.160 < a_n / \Lambda^2 < 0.150$

$$e^+ e^- \rightarrow v \bar{v} \gamma \gamma$$



95% C.L. Limits on quartic couplings in GeV^{-2} from combining
 $W^+ W^- \gamma$ and $v \bar{v} \gamma \gamma$ measurements:

L3

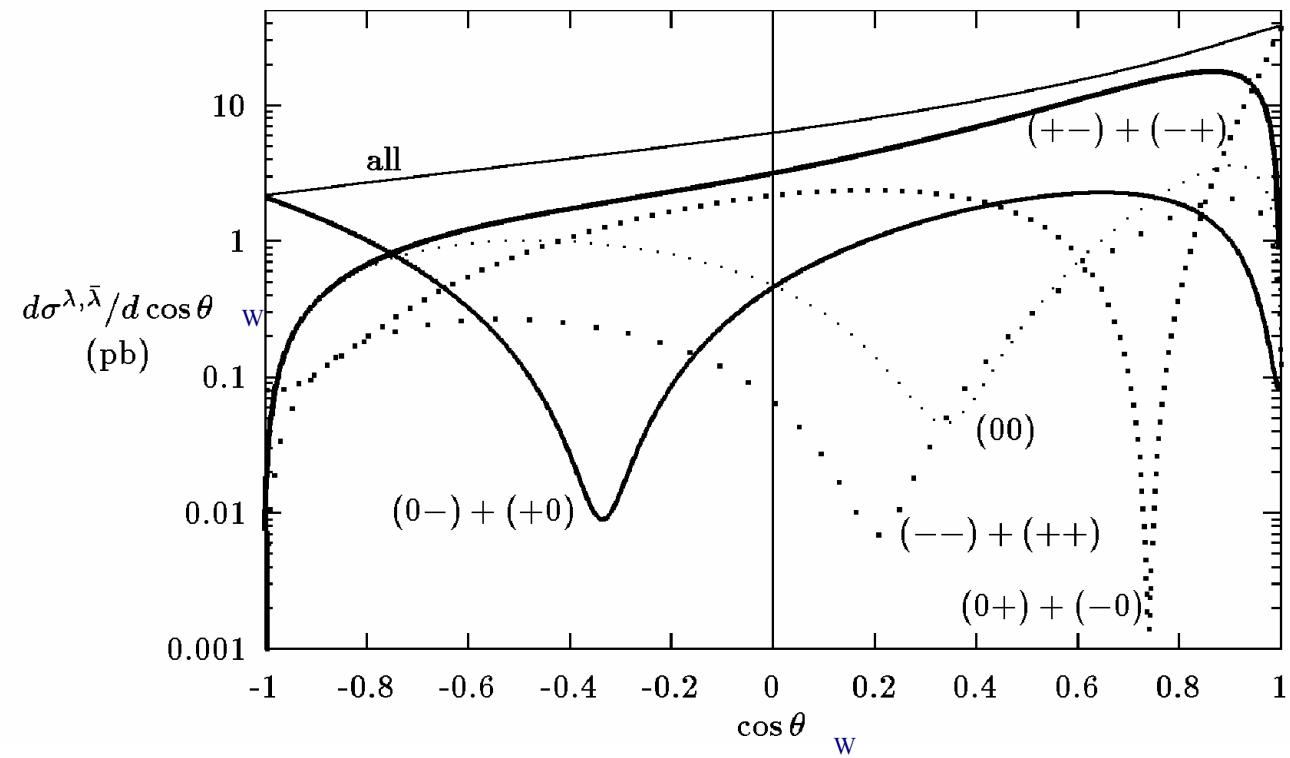
$$\begin{aligned} -0.015 &< a_0 / \Lambda^2 &< 0.015 \\ -0.048 &< a_c / \Lambda^2 &< 0.026 \\ -0.140 &< a_n / \Lambda^2 &< 0.130 \end{aligned}$$

OPAL

$$\begin{aligned} -0.020 &< a_0 / \Lambda^2 &< 0.020 \\ -0.052 &< a_c / \Lambda^2 &< 0.037 \\ -0.160 &< a_n / \Lambda^2 &< 0.150 \end{aligned}$$

W Polarization in $e^+e^- \rightarrow W^+W^-$

Measure spin density matrices $\rho_{kk}(s, \cos\theta_W)$ and extract polarized diff cross sec



$$\begin{aligned}\frac{d\sigma_L}{d\cos\theta_W} &= \rho_{00} \cdot \frac{d\sigma}{d\cos\theta_W} \\ \frac{d\sigma_T}{d\cos\theta_W} &= (\rho_{++} + \rho_{--}) \cdot \frac{d\sigma}{d\cos\theta_W}\end{aligned}$$

Fit for ρ_{kk} (L3)

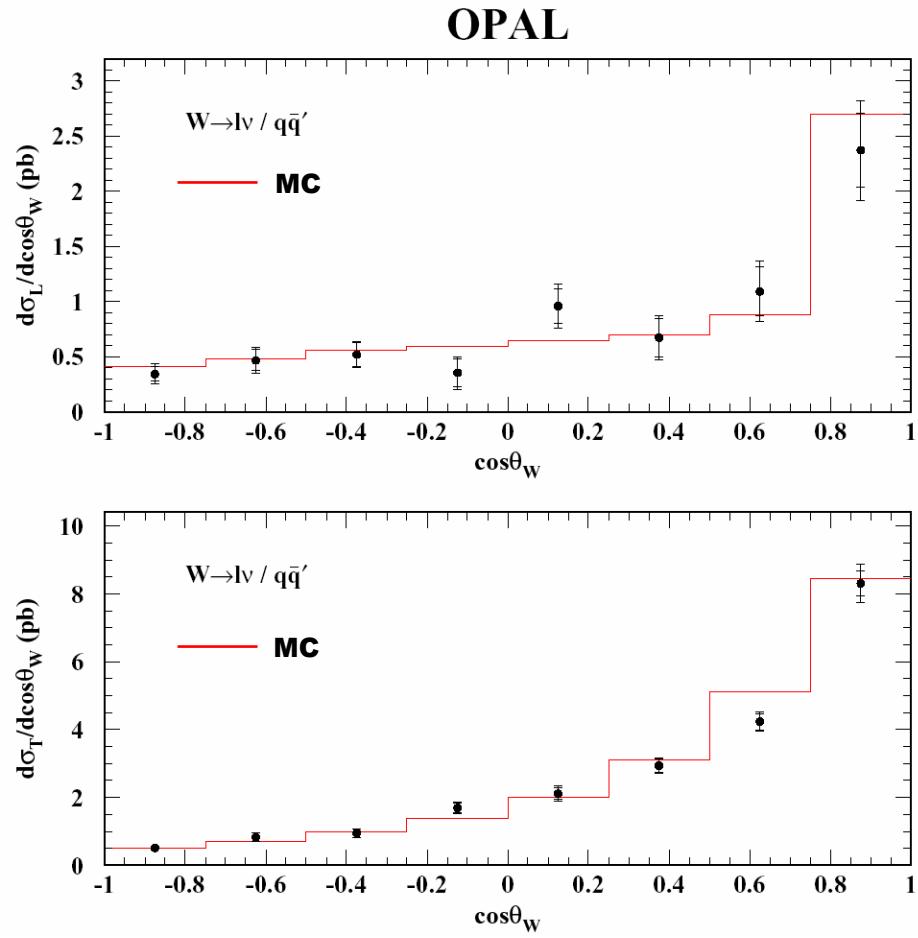
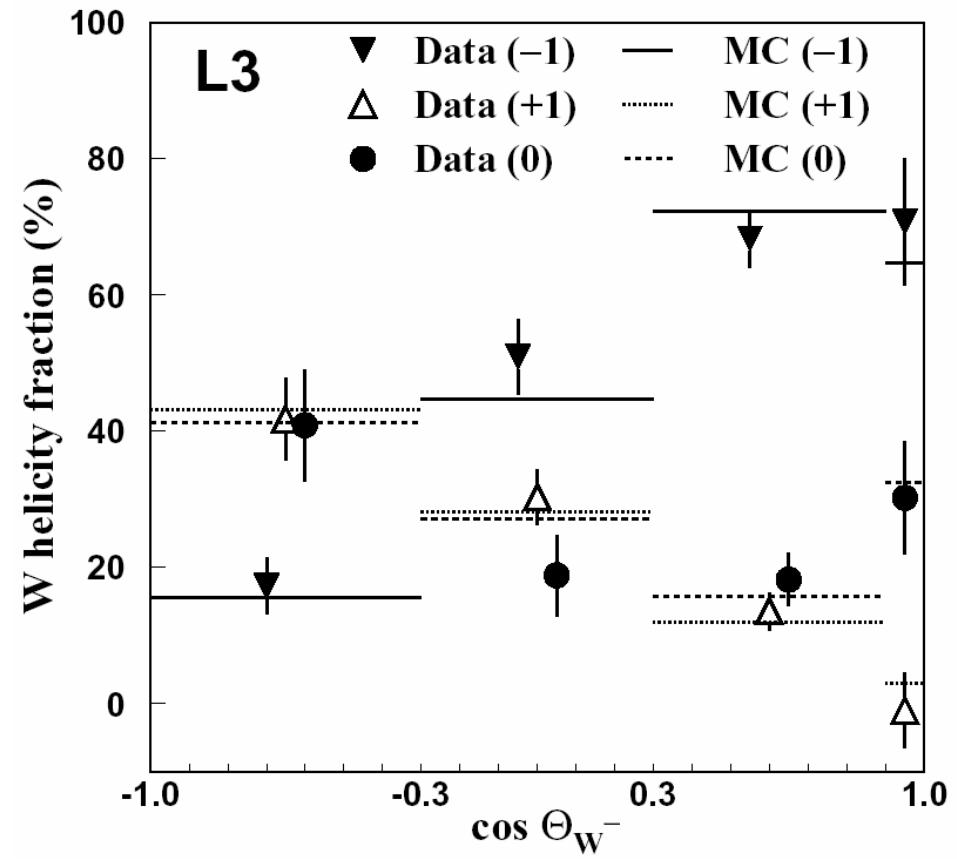
Use avg value of projection op Λ_{kk} (OPAL)

$$\begin{aligned}\frac{1}{\sigma} \frac{d\sigma}{d\cos\theta_f^*} &= \rho_{--} \frac{3}{8} (1 + \cos\theta_f^*)^2 + \rho_{00} \frac{3}{4} \sin^2\theta_f^* \\ &\quad + \rho_{++} \frac{3}{8} (1 - \cos\theta_f^*)^2.\end{aligned}$$

$$\rho_{\tau\tau'}^{W^-}(s, \cos\theta_W) = \frac{\int \frac{d^3\sigma}{d\cos\theta_W d\cos\theta_f^* d\phi_f^*} \cdot \Lambda_{\tau\tau'} d\cos\theta_f^* d\phi_f^*}{\frac{d\sigma}{d\cos\theta_W}}$$

W Polarization in $e^+e^- \rightarrow W^+W^-$

Polarized Differential Cross Sections



Triple Gauge Couplings

7 Complex Triple Gauge Couplings (TGCs) in Lorentz Invariant
 WWV Vertex ($V = \gamma, Z$)

	g_1^V	κ_V	λ_V	g_5^V	g_4^V	$\tilde{\kappa}_V$	$\tilde{\lambda}_V$
C	+	+	+	-	-	+	+
P	+	+	+	-	+	-	-
SM	1	1	0	0	0	0	0

electric charge $Q_W = e g_1^\gamma$

magnetic dipole moment $\mu_W = \frac{e}{2M_W} (1 + \kappa_\gamma + \lambda_\gamma)$

electric dipole moment $d_W = \frac{e}{2M_W} (\tilde{\kappa}_\gamma + \tilde{\lambda}_\gamma)$

Precision Electroweak Data \Rightarrow Effective Lagrangian must be SU(2)XU(1) Invariant to a Very Good Approximation

This can be used to constrain allowed TGC values IF assumptions about low energy ($< 1\text{TeV}$) particle content are made:

Assuming effective Lagrangian is C and P invariant , a relatively light Higgs boson, and no particles beyond SM at low energy \Rightarrow

$g_1^Z \kappa_\gamma \lambda_\gamma$ are free parameters
 $\Delta \kappa_Z = -\Delta \kappa_\gamma \tan^2 \theta_W + \Delta g_1^Z$

$$\lambda_Z = \lambda_\gamma$$

$$g_1^\gamma = 1$$

all other TGCs = 0

This model used for
1d, 2d, 3d fits by all
4 experiments, and
for 1d & 2d LEP comb

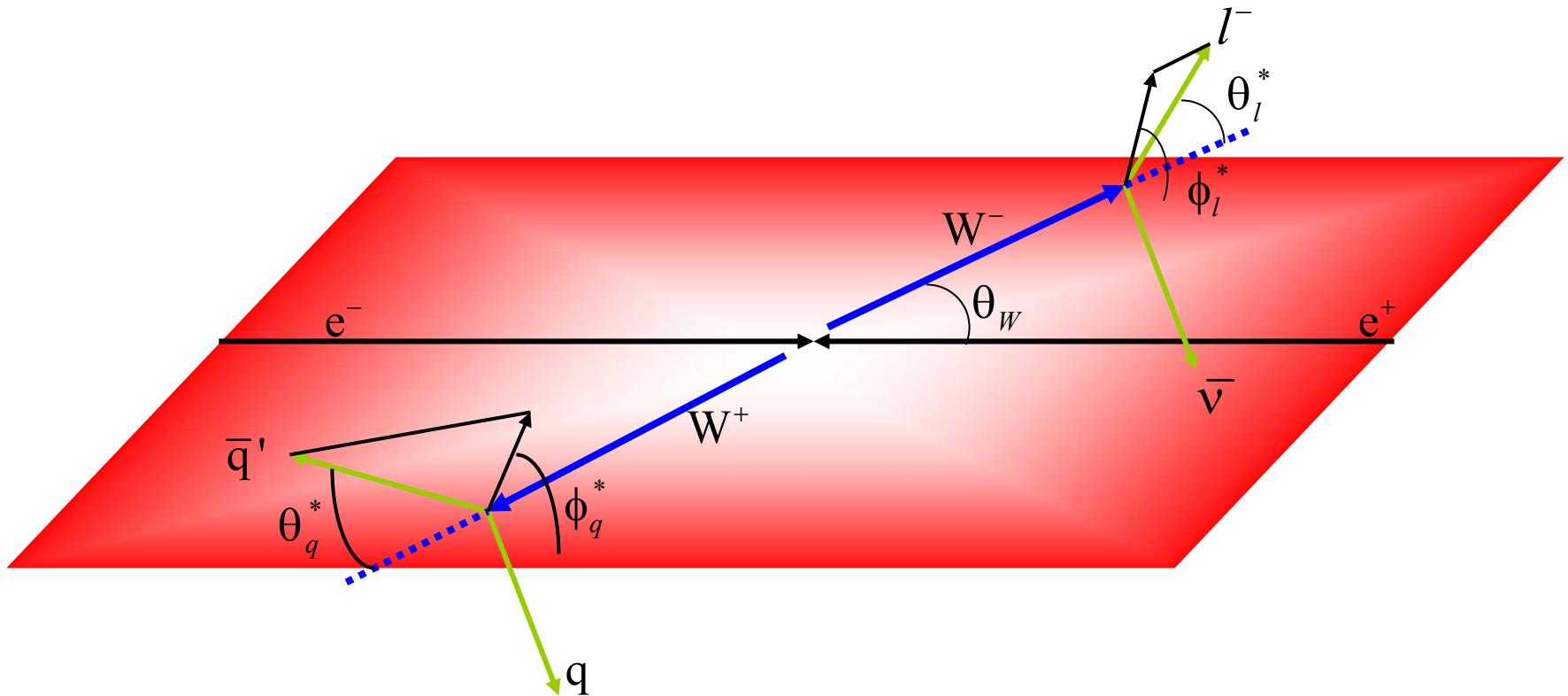
Assuming effective Lagrangian is C and P invariant ,a heavy (or no) Higgs boson and no particles beyond SM at low energy \Rightarrow

$g_1^Z \kappa_\gamma \kappa_Z$ are free parameters
 $g_1^\gamma = 1$

all other TGCs = 0

Triple Gauge Couplings

Most important process for studying TGCs is $e^+e^- \rightarrow W^+W^-$



Also some sensitivity to $WW\gamma$ TGCs from

$$e^+e^- \rightarrow W^+e^-\bar{\nu}_e$$

and

$$e^+e^- \rightarrow \nu_e\bar{\nu}_e\gamma$$

Triple Gauge Couplings: W^+W^- Analysis

Use angular distributions from all event topologies:

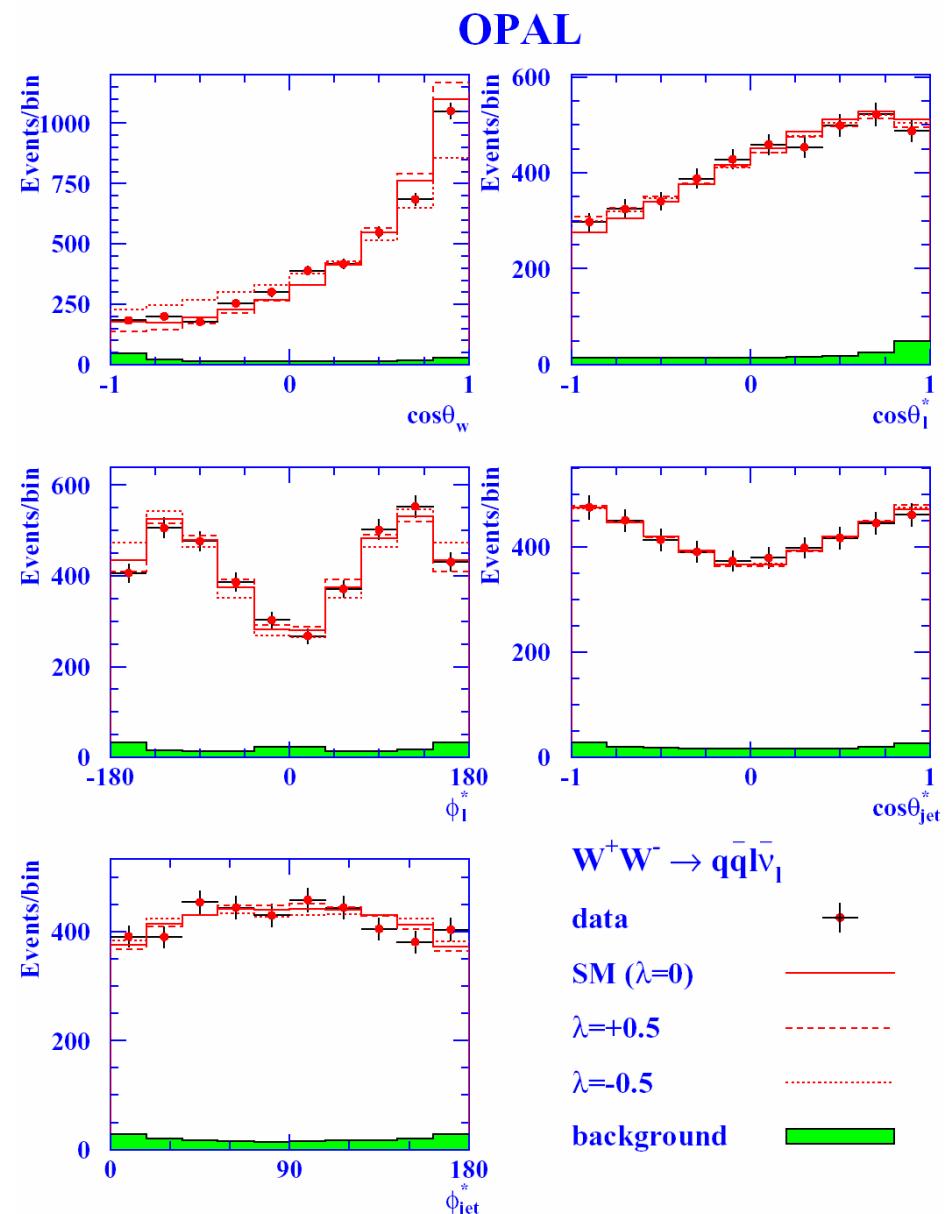
$$W^+W^- \rightarrow l^-\bar{v}q\bar{q}$$
$$q\bar{q}q\bar{q}$$
$$l^-\bar{v}l^+\nu$$

No jet flavor tagging - average over jet directions in W rest frame.

Do W charge tagging to obtain W^- direction in $q\bar{q}q\bar{q}$ events

Include total cross section

Use Monte Carlo to correct for detector effects and to implement radiative corrections



Triple Gauge Couplings: Systematic Errors

OPAL

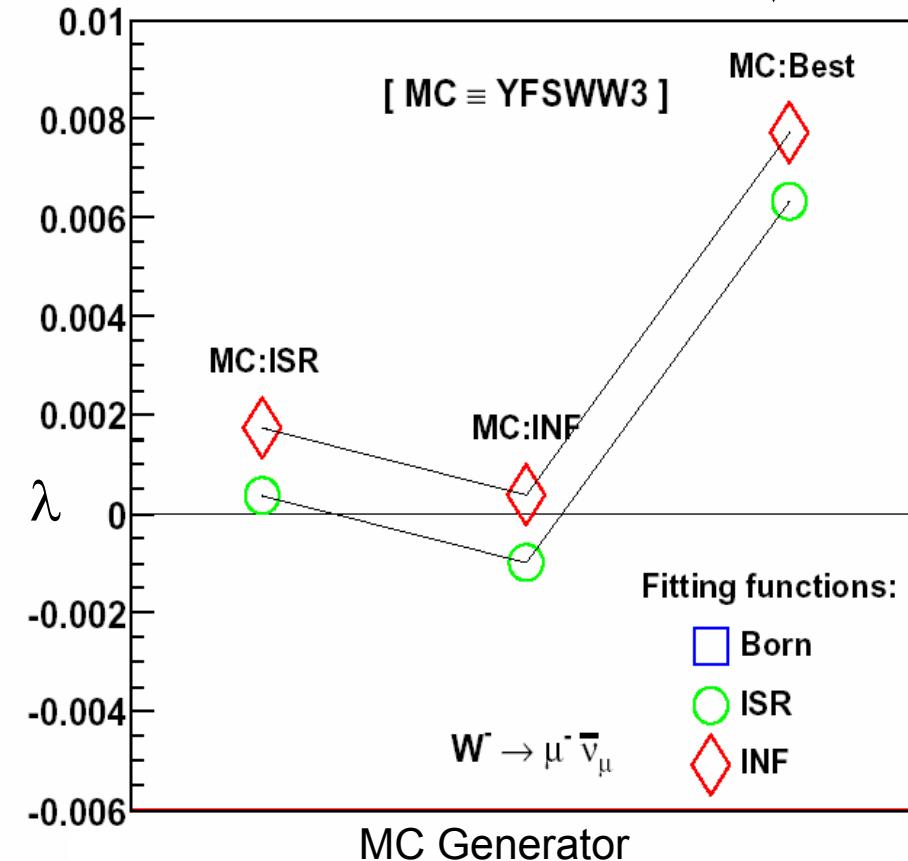
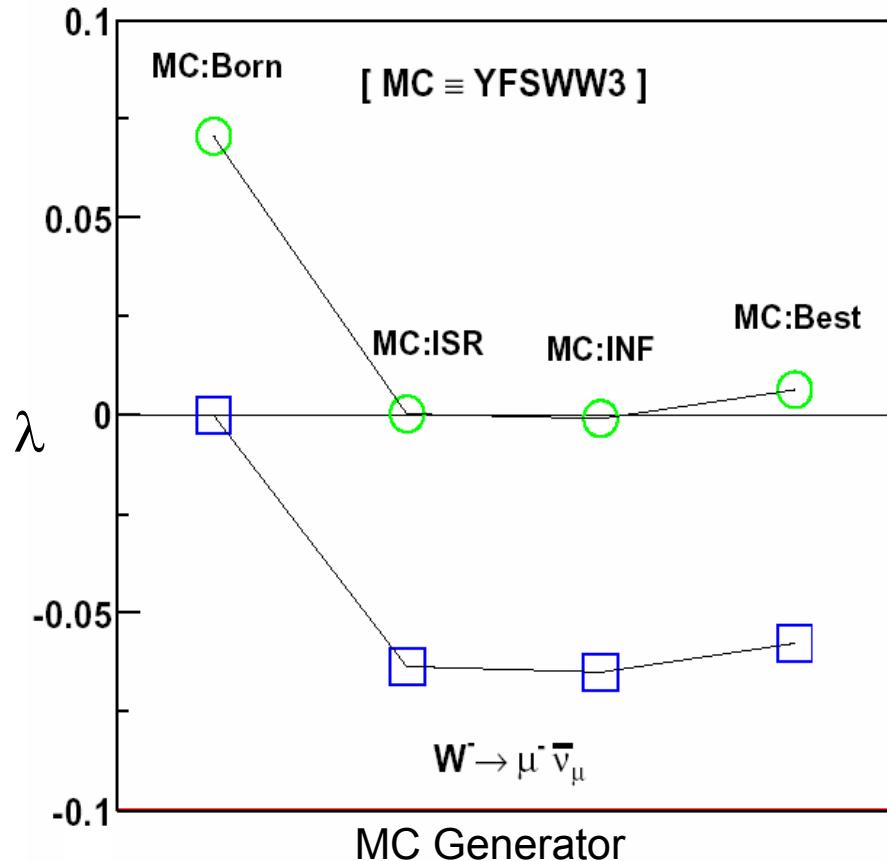
Source	$\Delta\kappa_\gamma$	Δg_1^z	λ	g_5^z
a) $\mathcal{O}(\alpha)$ correction	0.029	0.011	0.010	0.031
b) ISR	0.006	0.002	0.003	0.003
c) Fragmentation	0.038	0.013	0.018	0.047
d) TGC matrix element	0.011	0.005	0.004	0.005
e) Detector simulation	0.006	0.003	0.005	0.013
f) Background	0.015	0.004	0.011	0.012
g) \sqrt{s} , M_W	0.008	0.004	0.005	0.017
h) Bose-Einstein correlations	0.001	0.000	0.004	0.005
i) Colour reconnection	0.004	0.003	0.005	0.000
Total	0.053	0.019	0.026	0.061

Triple Gauge Couplings: $O(\alpha)$ Shape Sys Error

$O(\alpha)$ electroweak corrections to angular distribution shift λ by 0.008

Total theory error estimated to be $\Delta\lambda = 0.005$

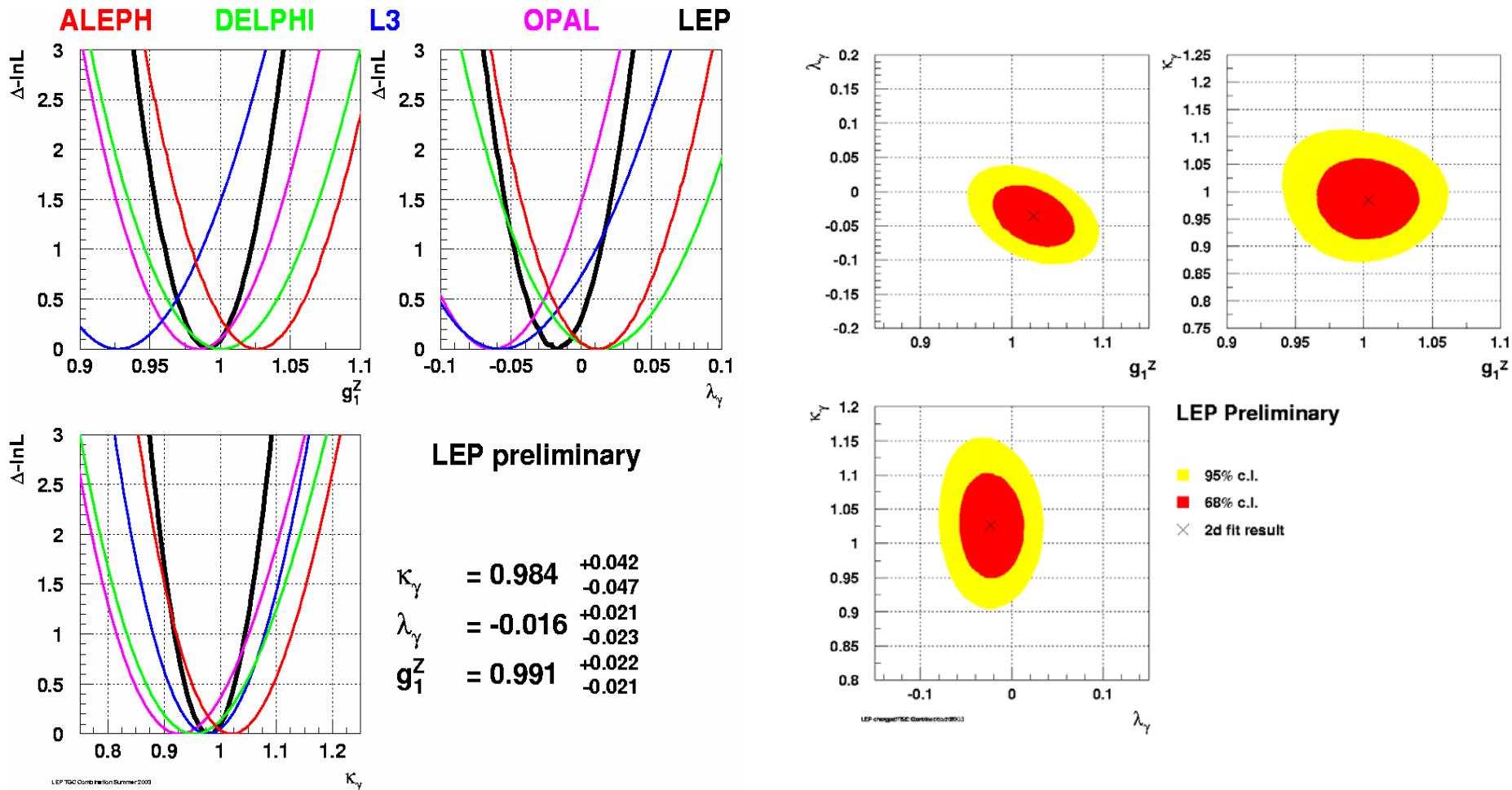
Fits of λ to $\cos\theta_W^*$ distribution for BARE $_{4\pi}$



OPAL & DELPHI assign $O(\alpha)$ theory error = total shift in TGC due to $O(\alpha)$ corr.

ALEPH & L3 assign $O(\alpha)$ theory error = 1/2 shift in TGC due to $O(\alpha)$ corr.

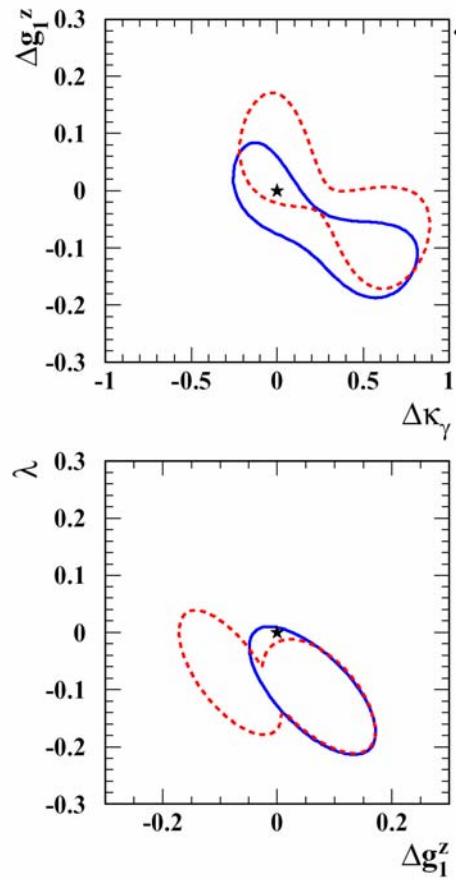
Triple Gauge Couplings: 1d & 2d Fit LEP Results



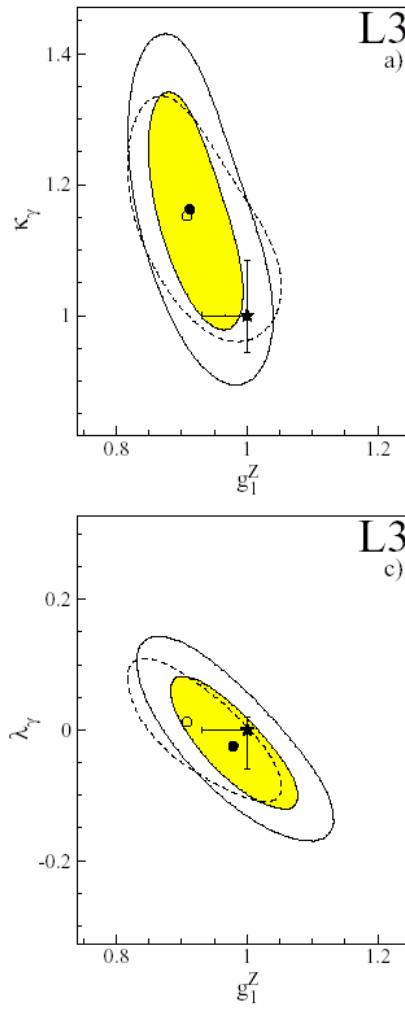
L3 and OPAL results are final

Triple Gauge Couplings: 3d Fit Results

OPAL



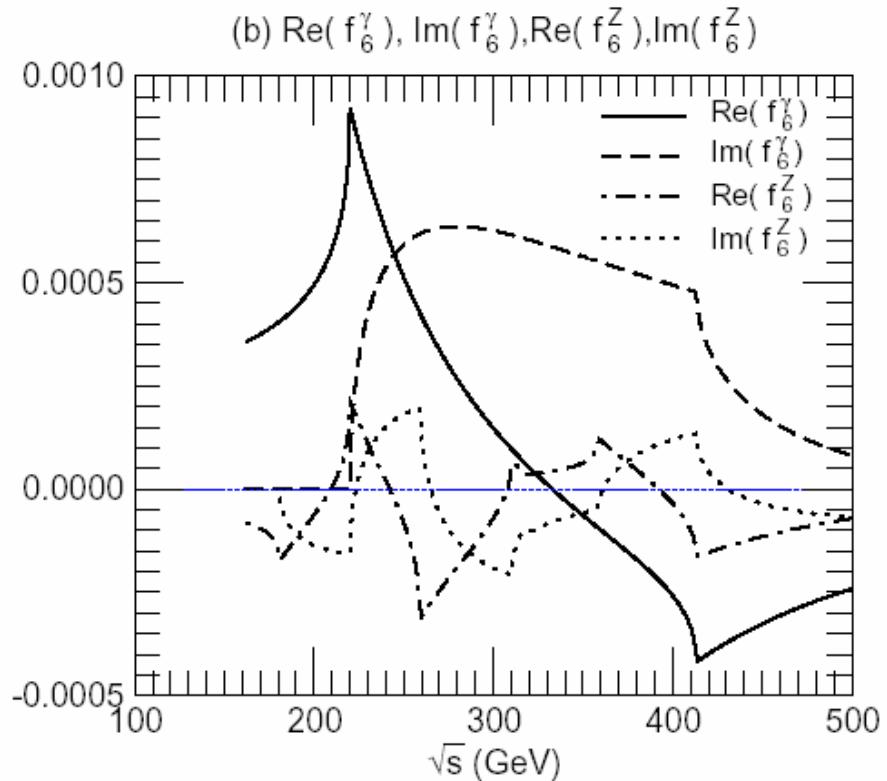
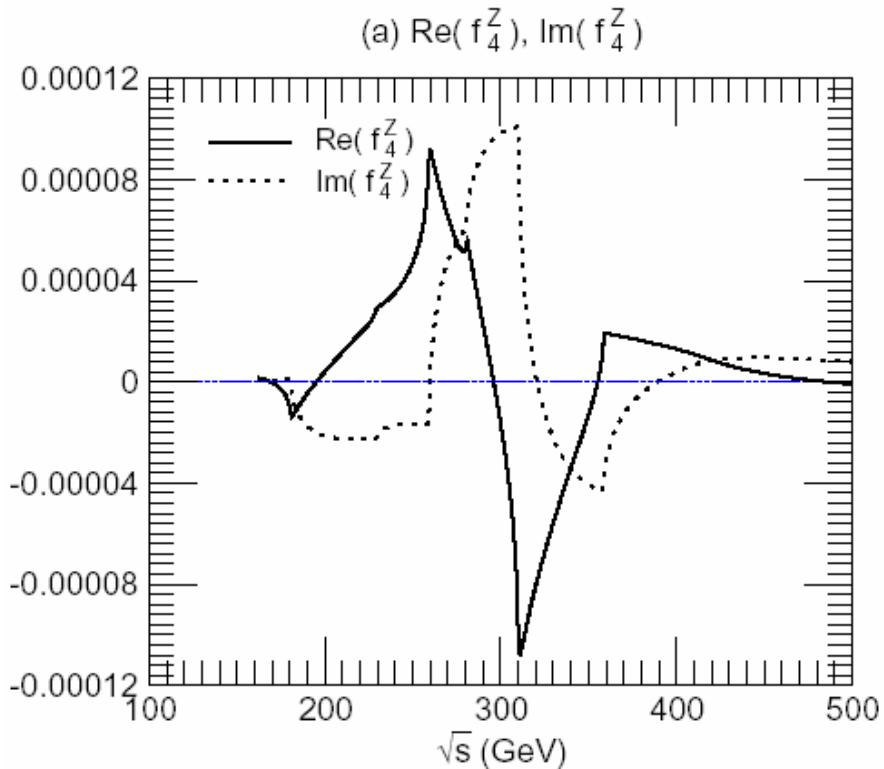
2D Fit —————
 3D Fit -----
 SM ★



★ Standard Model
 ┌─┐ 68% C.L., 1-par fit
 ● 2-par fit
 ■ 68% C.L., 2-par fit
 □ 95% C.L., 2-par fit
 ○ 3-par fit
 ---- 68% C.L., 3-par fit proj

One-Loop SUSY Contribution to CP Violating TGCs

Hagiwara,Kanemura,Klasen,Umeda hep-ph/0212135



$$f_4^Z = g_4^Z$$

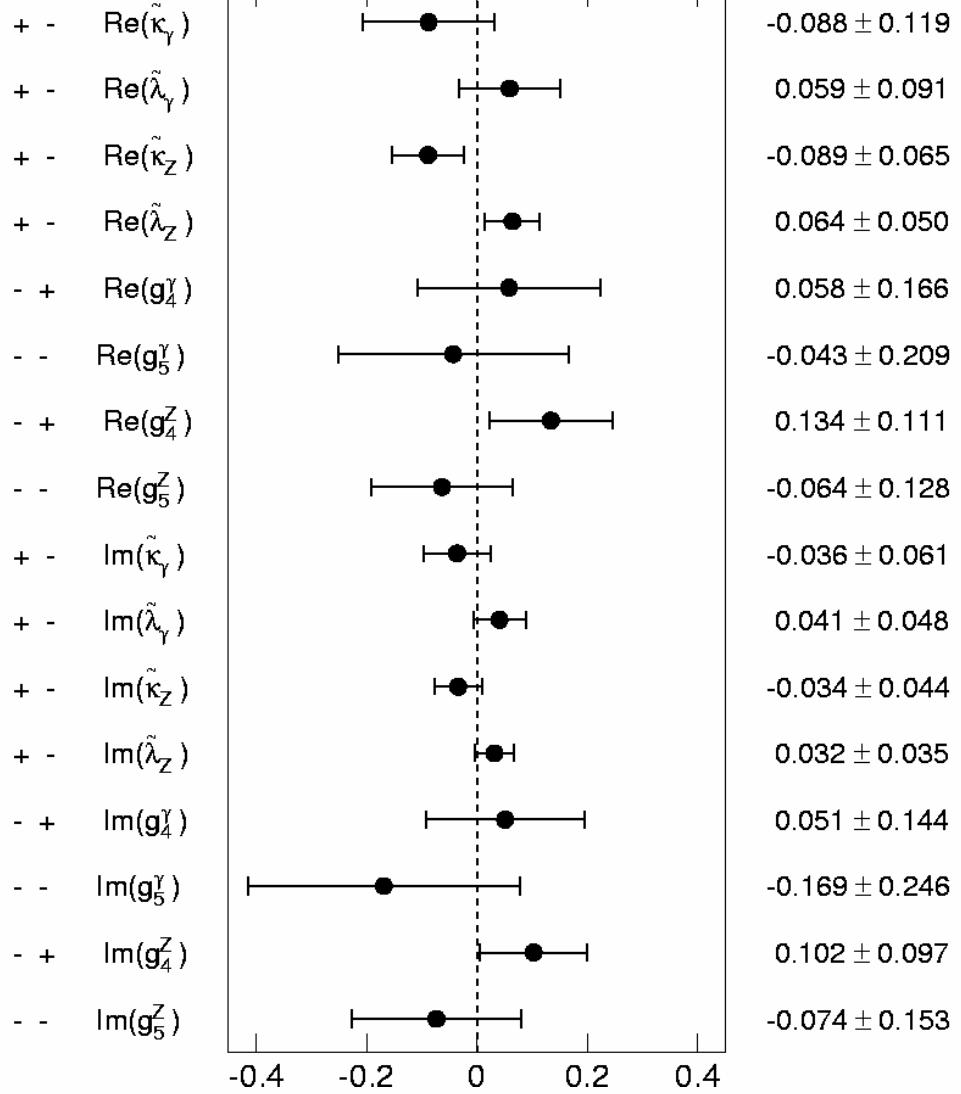
$$f_6^V = \tilde{\kappa}_V - \tilde{\lambda}_V$$

ALEPH Preliminary

C, P Violating TGCs

183-209 GeV Data (684.0 pb⁻¹)

C P



L3 (Final)

OPAL (Final)

0.00 ± 0.139

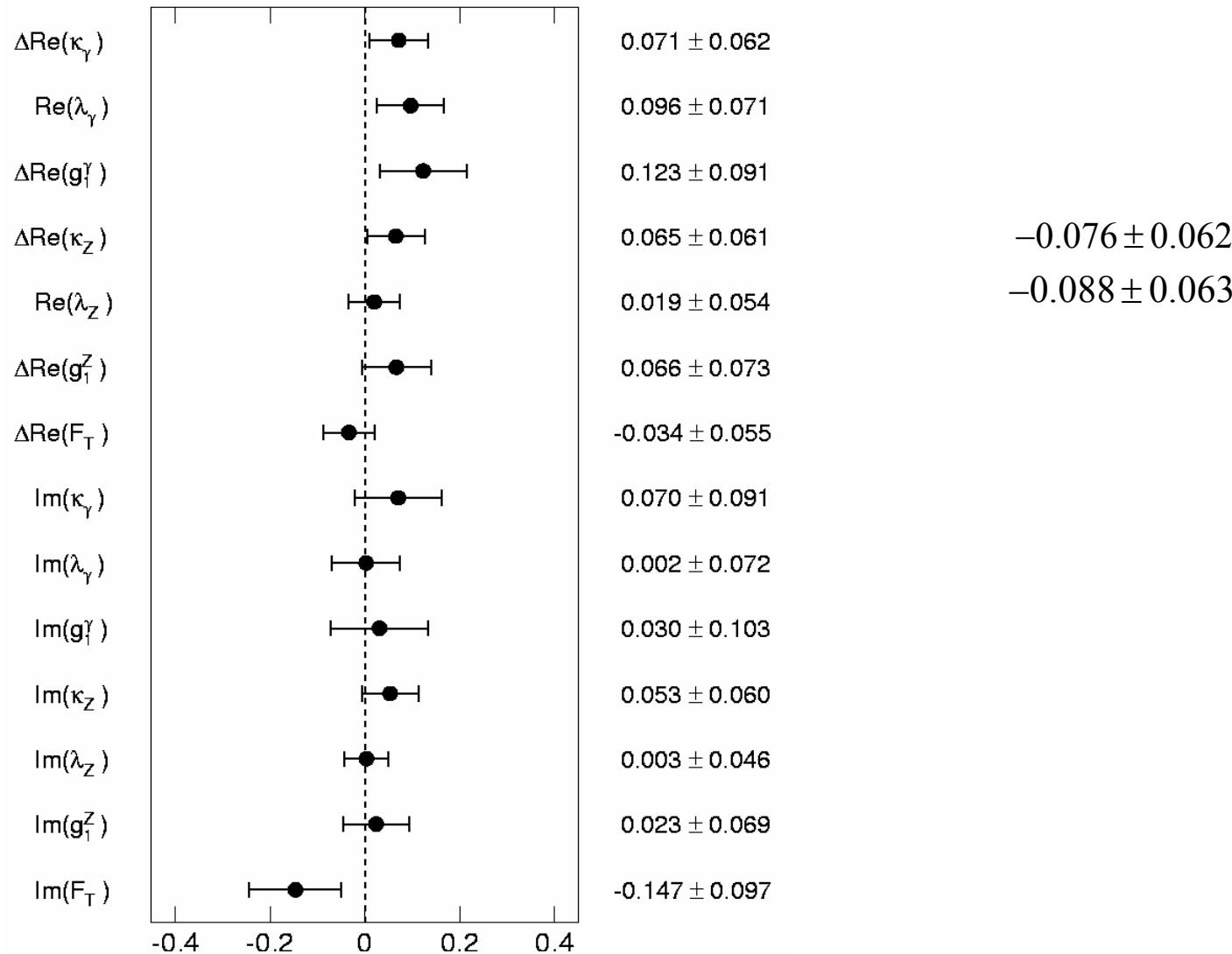
-0.04 ± 0.125

ALEPH Preliminary

L3 (Final)

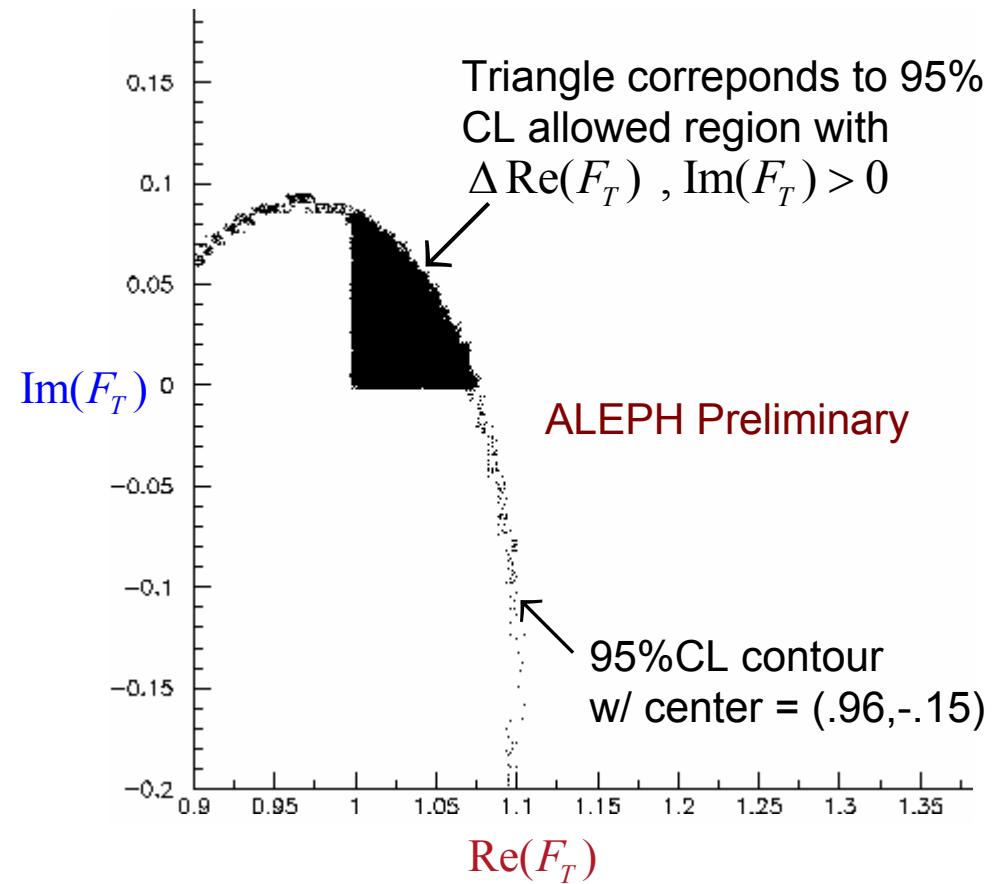
C, P Conserving TGCs, No SU(2) X U(1) Constraints

183-209 GeV Data (684.0 pb⁻¹)

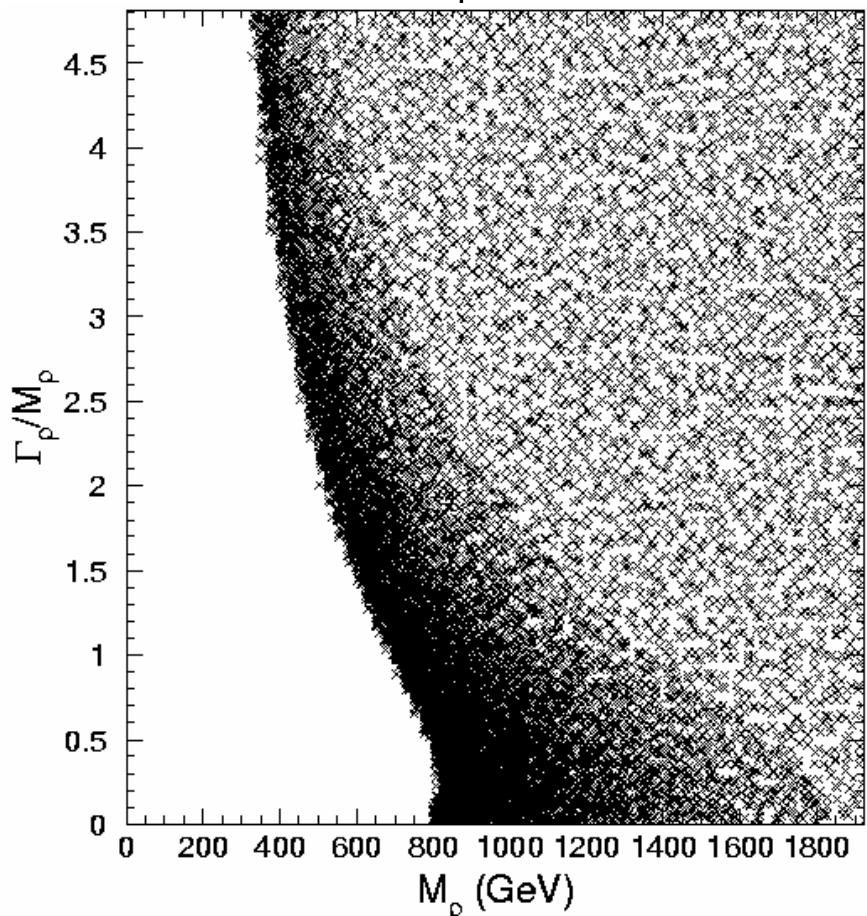


Form Factor F_T for Vector Resonance Enhancement of $e^+e^- \rightarrow W_L^+W_L^-$

$$F_T = 1 + \left(1 + \frac{\Gamma_\rho^2}{M_\rho^2} \right)^{-1} \frac{s}{M_\rho^2} + i \frac{\Gamma_\rho}{M_\rho} \left(1 + \frac{\Gamma_\rho^2}{M_\rho^2} \right)^{-1} \frac{s}{M_\rho^2}$$



Map triangle onto $(M_\rho, \Gamma_\rho / M_\rho)$ plane



For $\frac{\Gamma_\rho}{M_\rho} < 1$ the technirho mass $M_\rho > 675 \text{ GeV}$ at 95% C.L.
 For $\frac{\Gamma_\rho}{M_\rho} < 0.5$ the technirho mass $M_\rho > 775 \text{ GeV}$ at 95% C.L.

Summary

- W Pair Production Cross Section Agrees with SM at all LEP2 energies. Agreement is best when $\mathcal{O}(\alpha)$ electroweak rad corr are included.
- W Decay Branching Fractions Agree with SM.
- No Anomalous Quartic Couplings Observed.
- Fraction of Longitudinal and Transverse W Polarizations in Agreement with SM.
- TGCs measured to few percent accuracy. No deviation from the SM is observed.