



Measurement of φ_3 with $B \rightarrow D^{(*)0} K$ Dalitz analysis at Belle

A. Poluektov

BINP, Novosibirsk, Russia

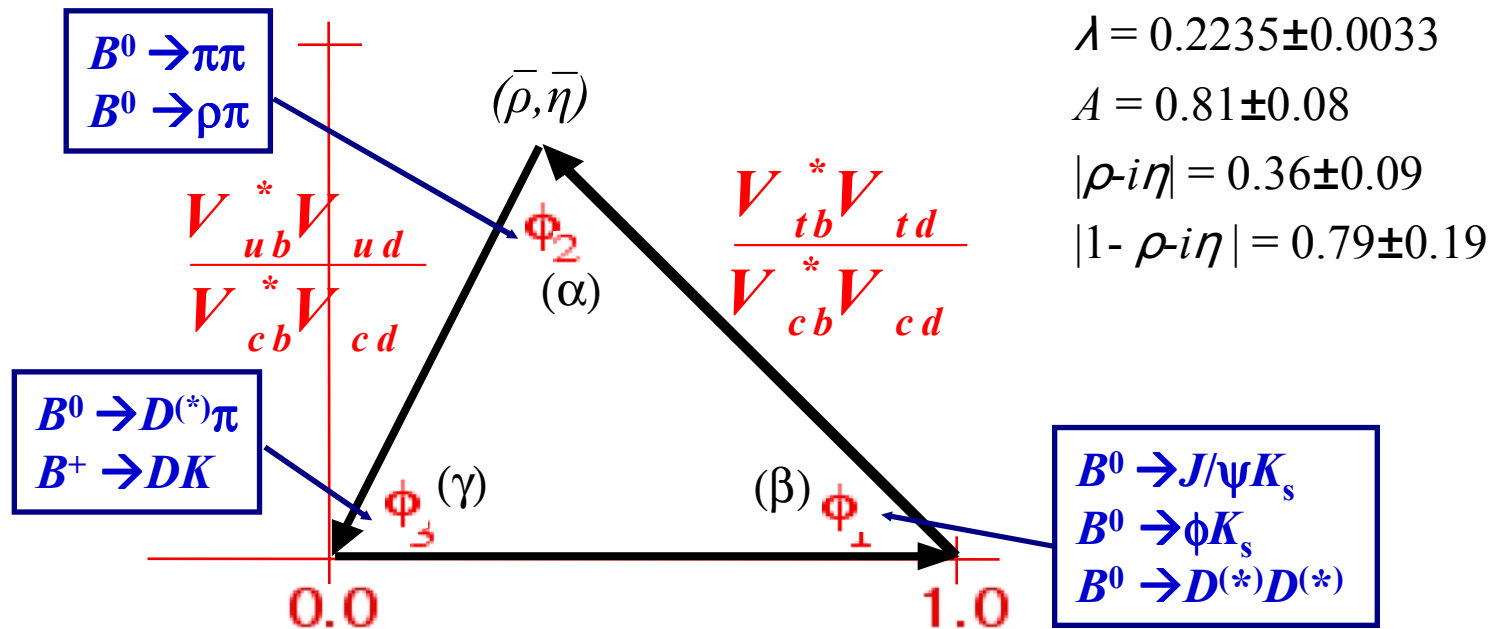
Outline:

- Introduction to the technique
- D^0 model determination
- Signal selection
- Estimation of statistical errors with toy MC
- Estimation of systematic errors
- Combined $B^+ \rightarrow D^0 K^+$ and $B^+ \rightarrow D^{*0} K^+$ fit
- Conclusion



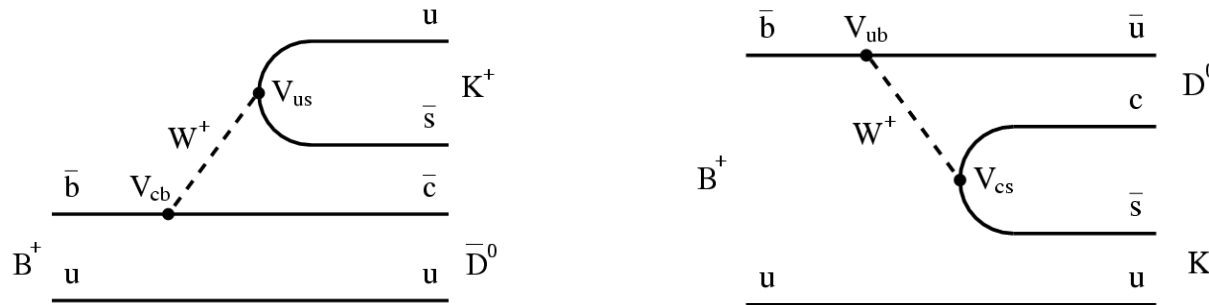
CKM matrix & unitarity triangle

$$V_{ij} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \approx \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$





$B^+ \rightarrow D^0 K^+$ decay



$$M_1 \sim V_{cb}^* V_{us} \sim A \lambda^3 \qquad M_2 \sim V_{ub}^* V_{cs} \sim A \lambda^3 (\rho + i\eta) \sim e^{i\phi_3}$$

If both D^0 and \bar{D}^0 decay into the same final state, $B^+ \rightarrow D^0 K^+$ and $B^+ \rightarrow \bar{D}^0 K^+$ amplitudes interfere. Mixed state is produced: $|\tilde{D}^0\rangle = |\bar{D}^0\rangle + re^{i\theta} |D^0\rangle$

Phase θ is a sum of strong and weak phases: $\theta = \phi_3 + \delta$

Use 3-body final state, identical for D^0 and \bar{D}^0 : $K_s \pi^+ \pi^-$.

Dalitz plot density: $d\sigma(m_{K_s \pi^+}^2, m_{K_s \pi^-}^2) \propto |M|^2 dm_{K_s \pi^+}^2 dm_{K_s \pi^-}^2$

$$|M(m_{K_s \pi^+}^2, m_{K_s \pi^-}^2)|^2 = |f(m_{K_s \pi^+}^2, m_{K_s \pi^-}^2) + re^{i\theta} f(m_{K_s \pi^-}^2, m_{K_s \pi^+}^2)|^2$$

(assuming CP conservation in D^0 decay)



$B^+ \rightarrow D^0 K^+$ decay

$|\tilde{D}^0\rangle = |\bar{D}^0\rangle + r e^{i\theta} |D^0\rangle$ If D^0 decay model is known, parameters r and θ can be obtained by Dalitz plot analysis.

For $B^- \rightarrow D^0 K^-$ weak phase of color-suppressed amplitude changes sign:

$$M_2 \propto V_{ub} V_{cs}^* \propto A \lambda^3 (\rho - i\eta) \propto e^{-i\varphi_3}$$

Strong phase is not changed. Therefore, $\theta_- = \delta - \varphi_3$

(r, φ_3, δ) can be obtained with simultaneous fit of B^+ and B^- data.

Use unbinned likelihood technique to fit Dalitz plots.

$$r \approx \frac{|V_{ub}^* V_{cs}|}{|V_{cb}^* V_{us}|} \times \frac{|a_2|}{|f a_1 + a_2|} = 0.09 / 0.22 \times 0.35 \approx 1/8$$

Factor $|a_2|/|f a_1 + a_2| = 0.35$ related to color suppression can be estimated from the ratio of $B^0 \rightarrow D^0 K^0$ and $B^+ \rightarrow D^0 K^+$ branching fractions (measured by Belle)

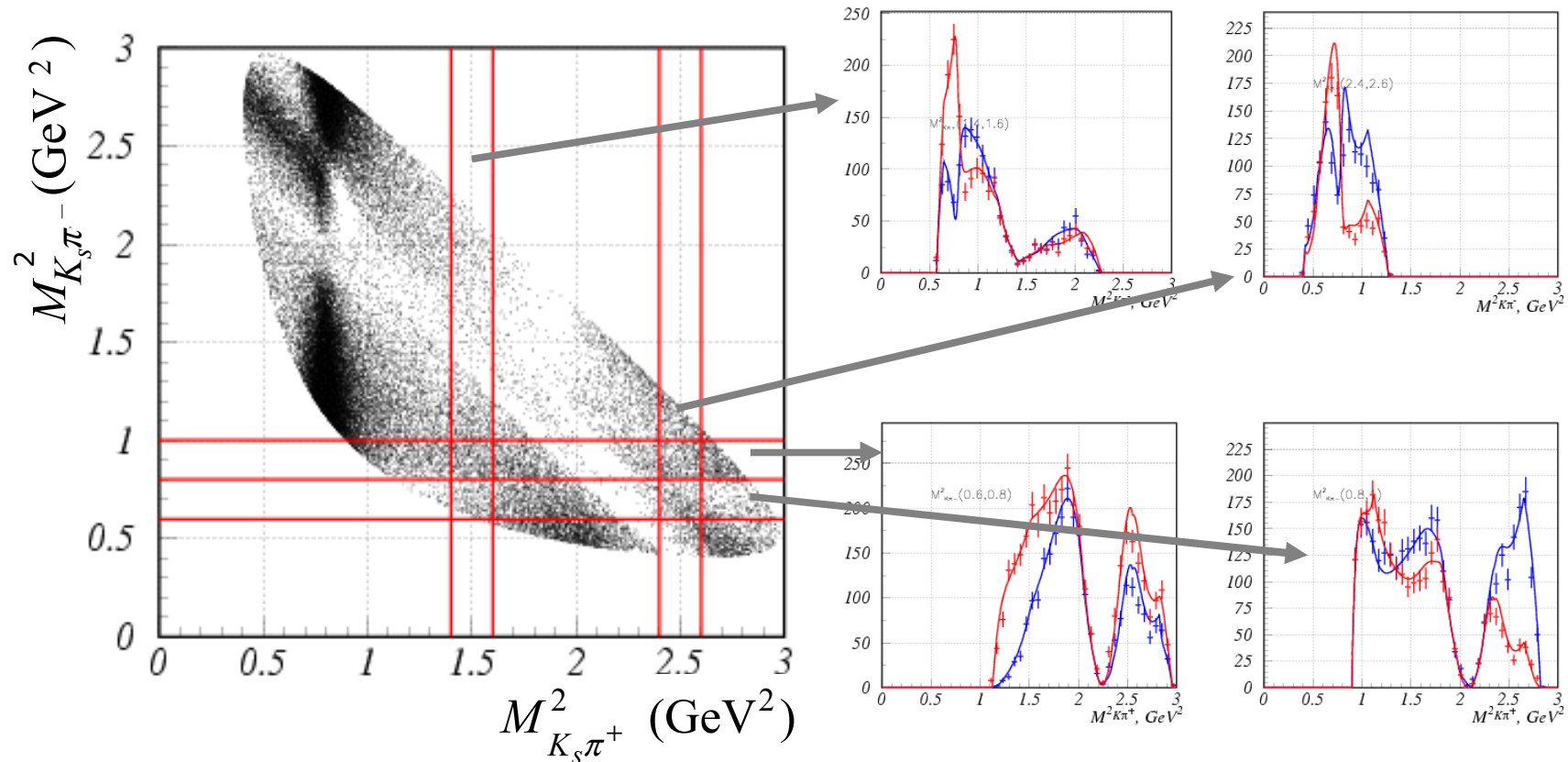
References:

- A. Giri, Yu. Grossman, A. Soffer, J. Zupan, hep-ph/0303187
- Belle collaboration, hep-ex/0308043 (Contributed to LP2003)



Effect of CPV and ϕ_3 (MC)

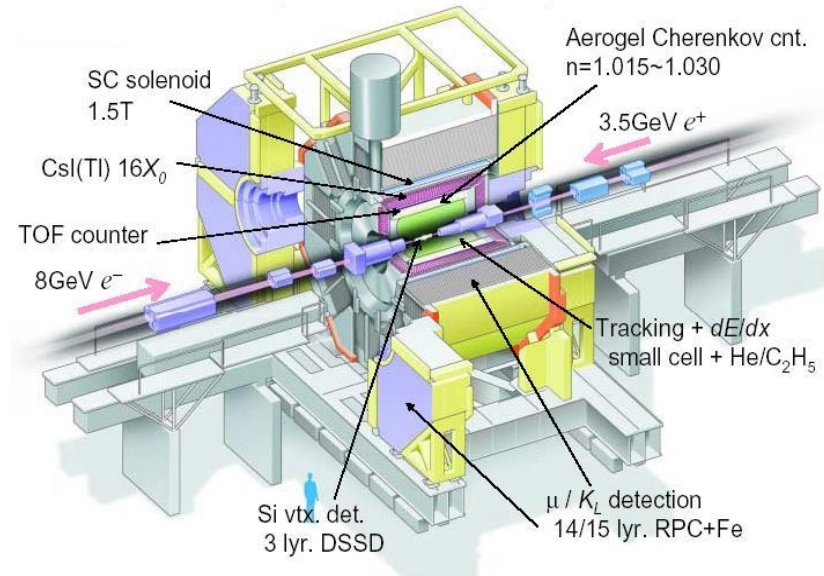
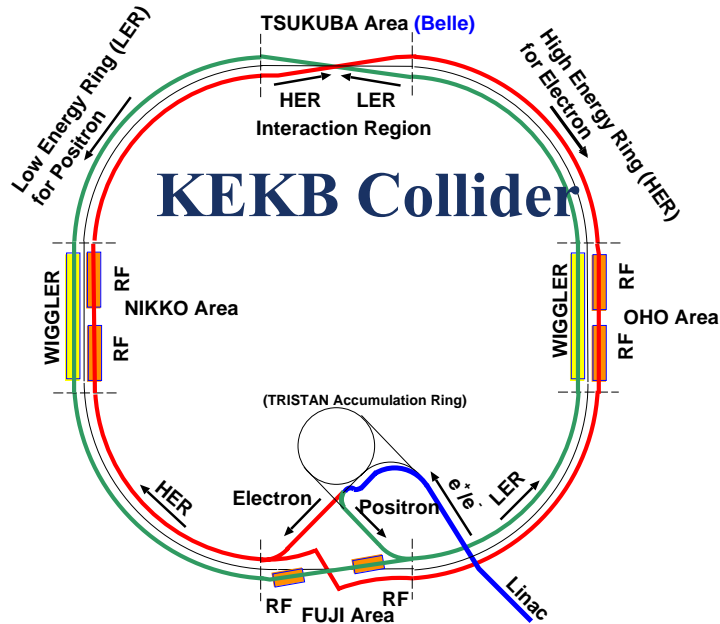
MC generated statistics (50000 $B \rightarrow D^0 K$ decays)



Most sensitive regions of the Dalitz plot ($r = 0.125, \delta = 0, \phi_3 = 70^\circ$)



Belle detector



3.5 GeV e^+ & 8 GeV e^- **asymmetric** Collider

3 km circumference, 11 mrad crossing angle

$L = 1.2 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$ (**world record**)

$\int L dt = 219 \text{ fb}^{-1}$ @ $Y(4S) + \text{off} (\sim 10\%)$

(140 fb^{-1} : $1.52 \times 10^8 \text{ B}\bar{\text{B}}$ pairs)



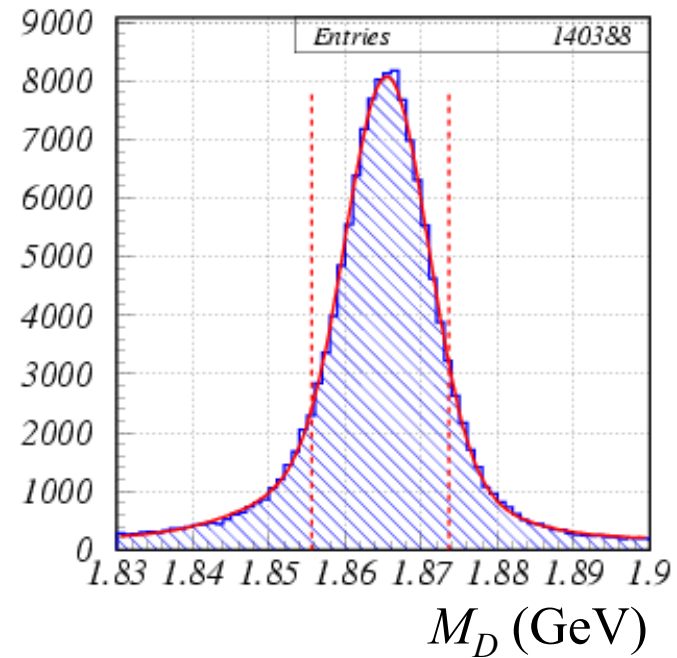
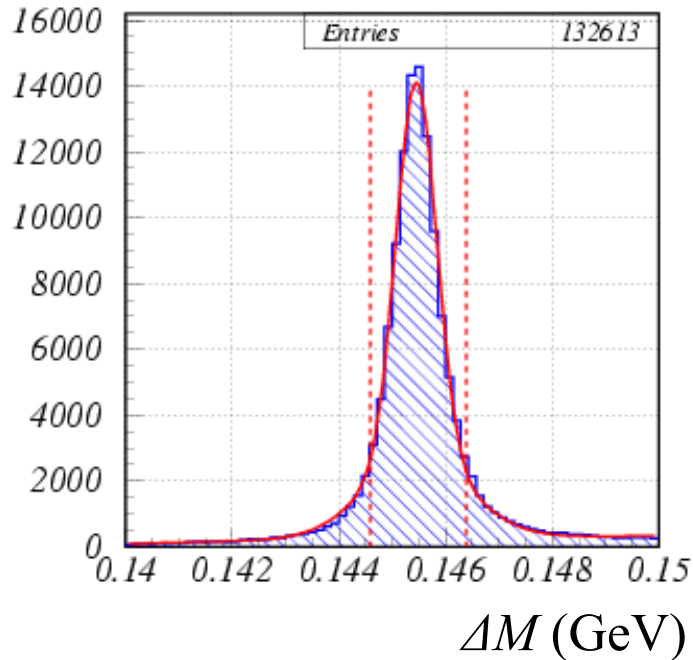
~350 scientists, 55 institutions



Analysis overview

- Determination of $D^0 \rightarrow K_s \pi^+ \pi^-$ decay model
 - Use flavor tagged sample of D^0 's from $D^{*-} \rightarrow D^0 \pi^-$, $D^0 \rightarrow K_s \pi^+ \pi^-$ produced in continuum
- Selection of $B^+ \rightarrow D^0 K^+$ events
- Selection of $B^+ \rightarrow D^{*0} K^+$, $D^{*0} \rightarrow D^0 \pi^0$ events
- Unbinned maximum likelihood fit of the D^0 Dalitz plots with free parameters (r , φ_3 , δ)
- Fits to control samples without opposite flavor contributions:
 $B^+ \rightarrow D^0 \pi^+$, $B^+ \rightarrow D^{*0} \pi^+$, $B^0 \rightarrow D^{*+} \pi^-$
- Evaluation of statistical errors using large number of toy MC pseudo-experiments
- Evaluation of systematic and model errors
- Combined φ_3 measurement



$$D^{*-} \rightarrow D^0 \pi^-, D^0 \rightarrow K_S \pi^+ \pi^- \text{ selection}$$


140 fb⁻¹ statistics
 101800 events
 3.1% background
 (shape from ΔM sidebands)

- $144.6 < M_{D^*} - M_D < 146.4$ MeV
- $1.856 < M_D < 1.874$ GeV
- $P_{D^*} > 2.7$ GeV

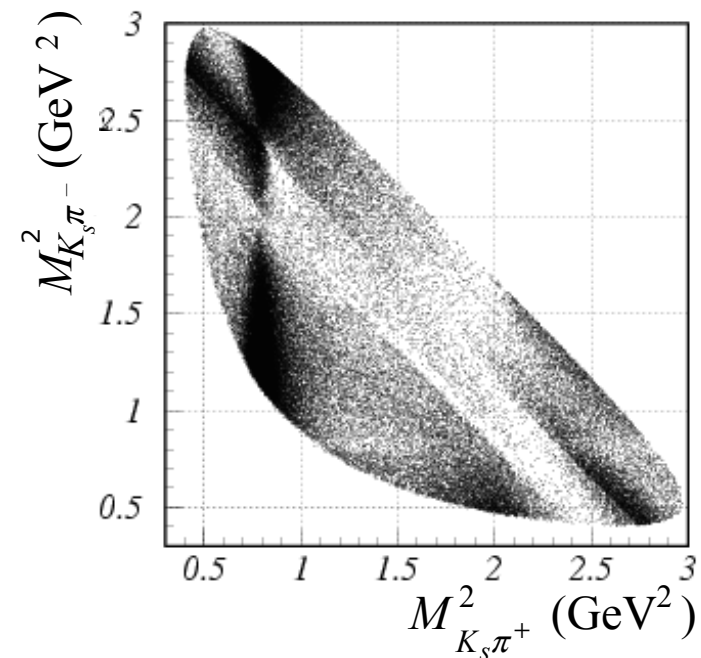


$D^0 \rightarrow K_S \pi^+ \pi^-$ decay model

Resonance	Our fit		
	Amplitude	Phase, °	Fit fraction
$\sigma_1 K_S$	1.66 ± 0.11	218.0 ± 3.8	11%
$\rho(770) K_S$	1	0	21%
ωK_S	$(3.30 \pm 1.13) \cdot 10^{-2}$	114.3 ± 2.3	0.4%
$f_0(980) K_S$	0.405 ± 0.008	212.9 ± 2.3	4.8%
$\sigma_2 K_S$	0.31 ± 0.05	236 ± 11	0.9%
$f_2(1270) K_S$	1.36 ± 0.06	352 ± 3	1.5%
$f_0(1370) K_S$	0.82 ± 0.10	308 ± 8	0.9%
$K^*(892) \pi^+$	1.656 ± 0.012	137.6 ± 0.6	60%
$K^*(892) \pi^-$	0.149 ± 0.007	325.2 ± 2.2	0.5%
$K^*_0(1430) \pi^+$	1.96 ± 0.04	357.3 ± 1.5	5.8%
$K^*_0(1430) \pi^-$	0.30 ± 0.05	128 ± 8	0.1%
$K^*_2(1430) \pi^+$	1.32 ± 0.03	313.5 ± 1.8	2.8%
$K^*_2(1430) \pi^-$	0.21 ± 0.03	281.5 ± 9	0.07%
$K^*(1680) \pi^-$	2.56 ± 0.22	70 ± 6	0.4%
$K^*(1680) \pi^+$	1.02 ± 0.22	102 ± 11	0.07%
Non resonant	6.1 ± 0.3	146 ± 3	24%

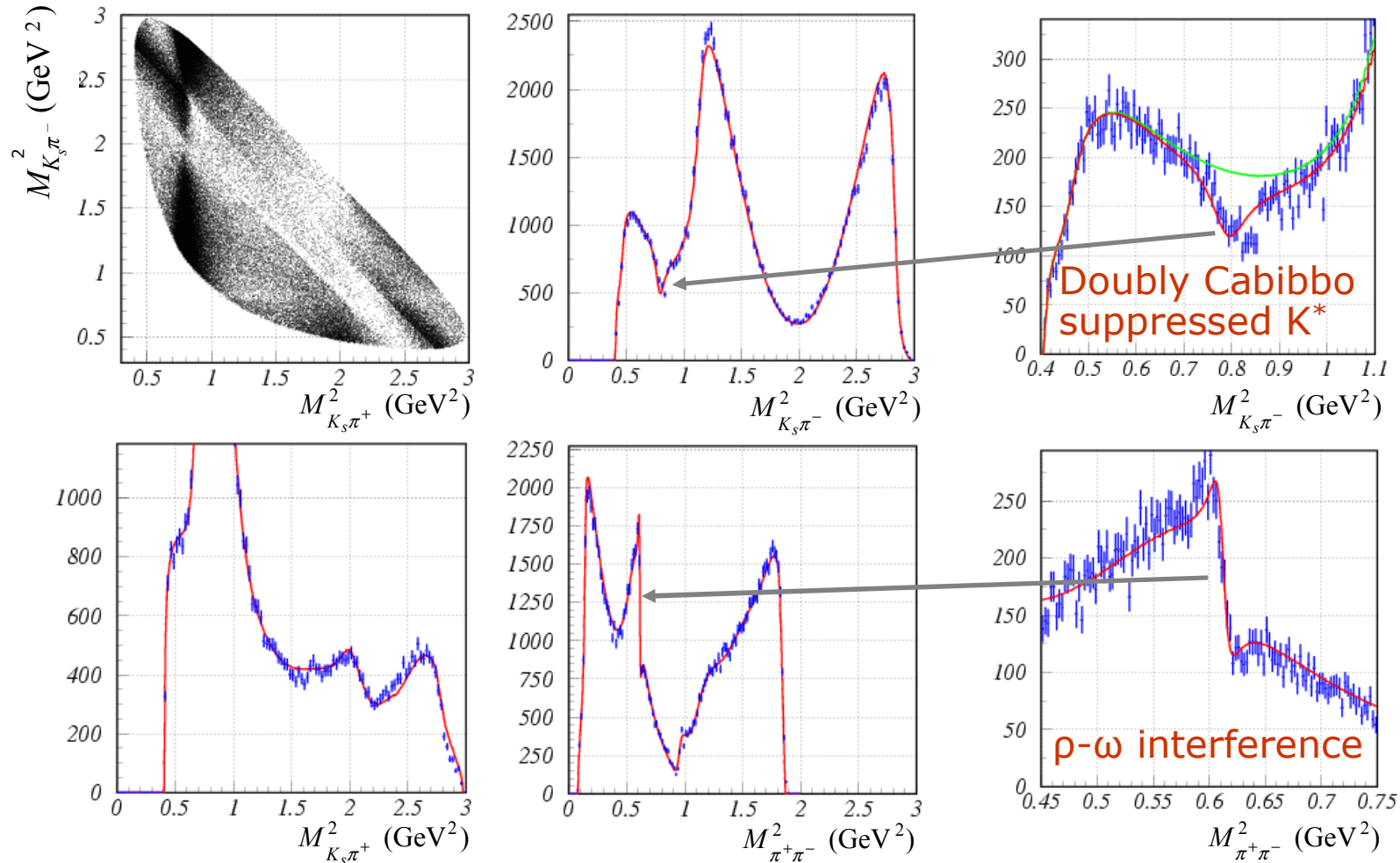
Sum of two-body amplitudes:

$$f = a_{K^*} e^{i\phi_{K^*}} [F_D F_{K^*} M^J BW(m_{K_S \pi^-}^2)] + a_\rho e^{i\phi_\rho} [F_D F_\rho M^J BW(m_{\pi^+ \pi^-}^2)] + \dots$$





$D^{*-} \rightarrow D^0 \pi^-, D^0 \rightarrow K_s \pi^+ \pi^-$ Dalitz plot





B candidate selection

Pairs of B mesons are produced in $Y(4S)$ decays (near $B\bar{B}$ mass threshold)

$\Rightarrow E_B = E_{cm} / 2$, low p in CM frame

CM energy difference:

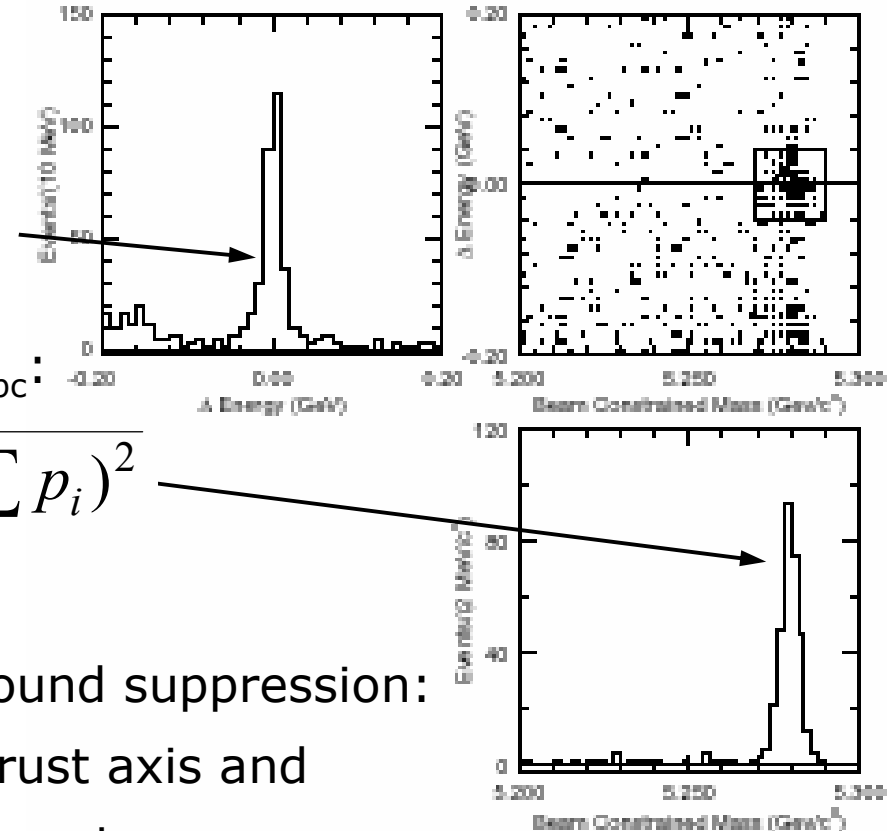
$$\Delta E = \sum E_i - (E_{cm} / 2)$$

B meson beam-constrained mass M_{bc} :

$$M_{bc} = \sqrt{(E_{cm} / 2)^2 - (\sum p_i)^2}$$

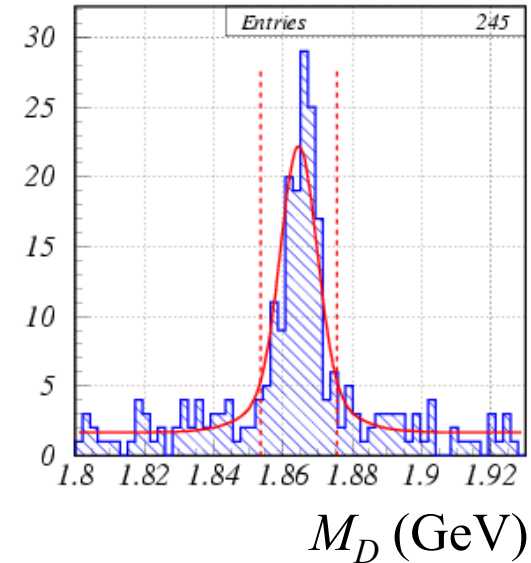
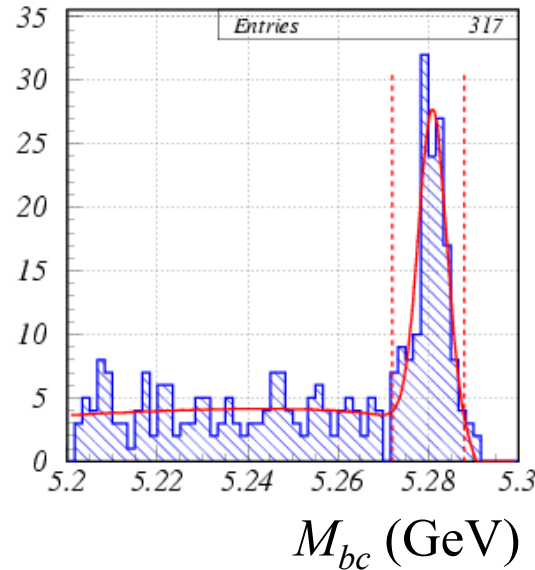
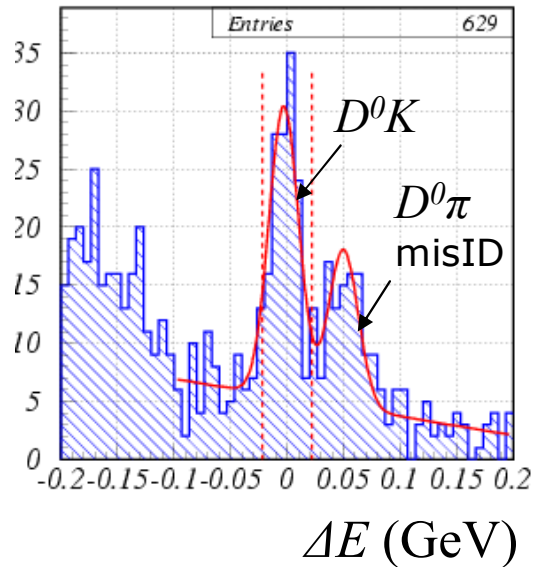
Continuum ($e^+e^- \rightarrow uu, dd, ss$) background suppression:

- Angle between B candidate thrust axis and thrust axis of the rest of the event
- Fisher discriminant based on "virtual calorimeter"





$B^+ \rightarrow D^0 K^+$ signal with 140 fb 1



12% reconstruction efficiency

146 events

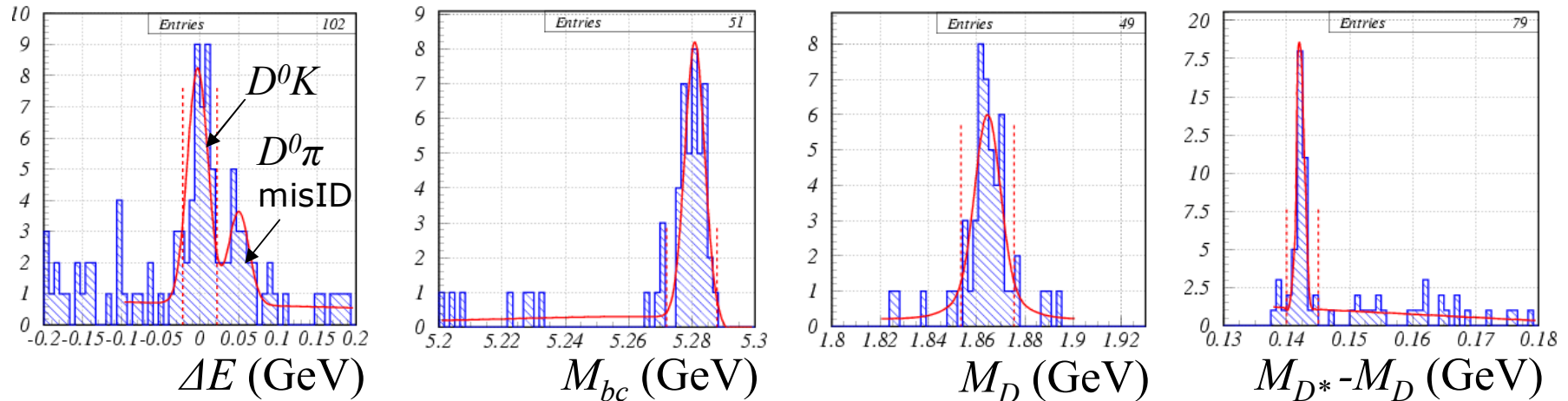
112 ± 12 signal

36 ± 3 background (25%)

- $|\Delta E| < 22$ MeV
- $5.272 < M_{bc} < 5.288$ GeV
- $|M_D - 1.86 \text{ GeV}| < 11$ MeV
- $|\cos \Theta_{thr}| < 0.8$
- Fisher discriminant $\mathcal{F} > -0.7$
- $\text{PID}(K/\pi) > 0.7$



$B^+ \rightarrow D^{*0} K^+$ signal with 140 fb⁻¹



6.2% reconstruction efficiency

39 events

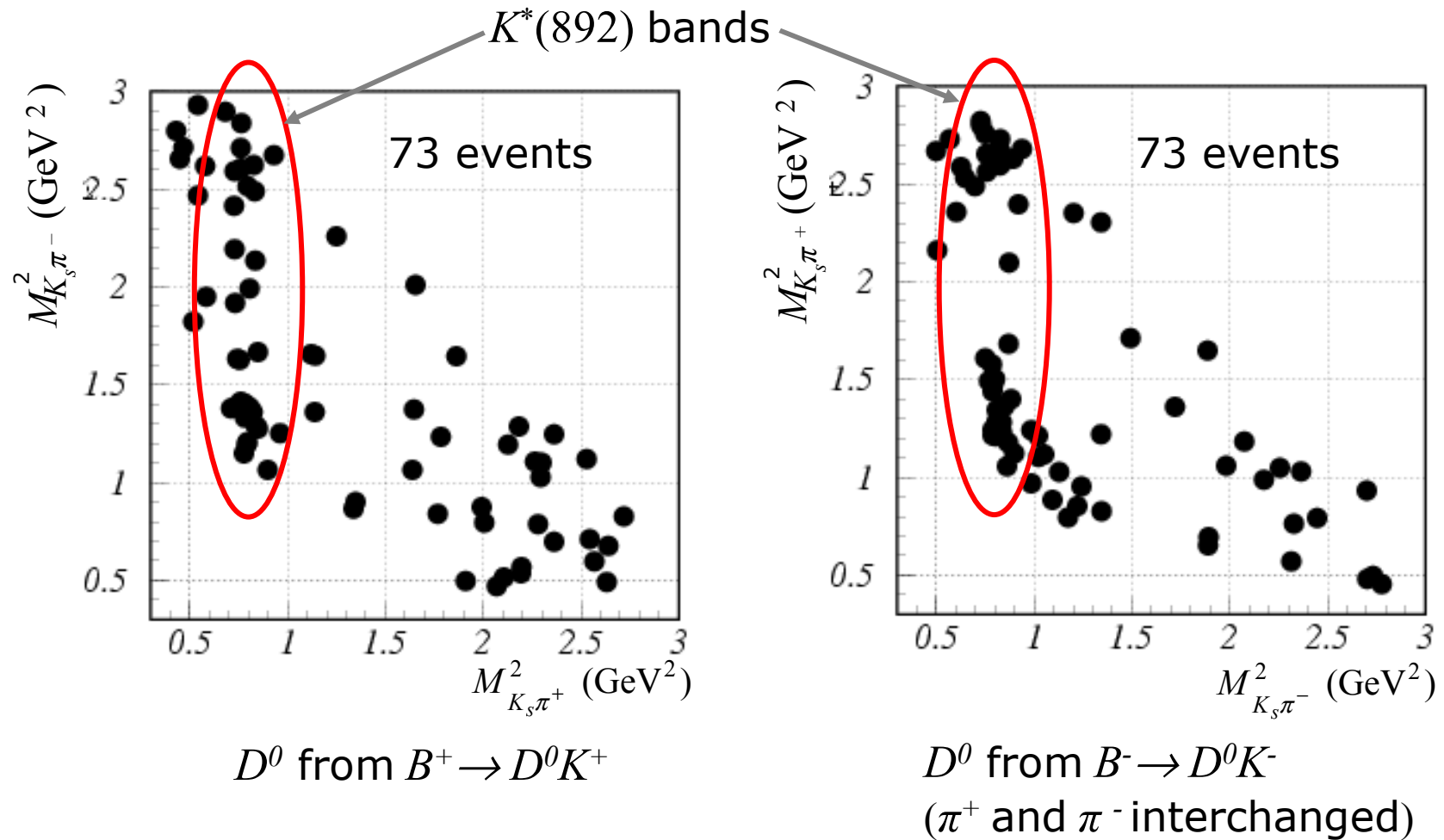
33.6 ± 6.2 signal

4.6 ± 1.1 background (12%)

- $|\Delta E| < 22$ MeV
- $5.272 < M_{bc} < 5.288$ GeV
- $|M_D - 1.86 \text{ GeV}| < 11$ MeV
- $140 < M_{D^*} - M_D < 145$ MeV
- $|\cos\Theta_{thr}| < 0.8$
- Fisher discriminant $\mathcal{F} > -0.7$
- $\text{PID}(K/\pi) > 0.7$

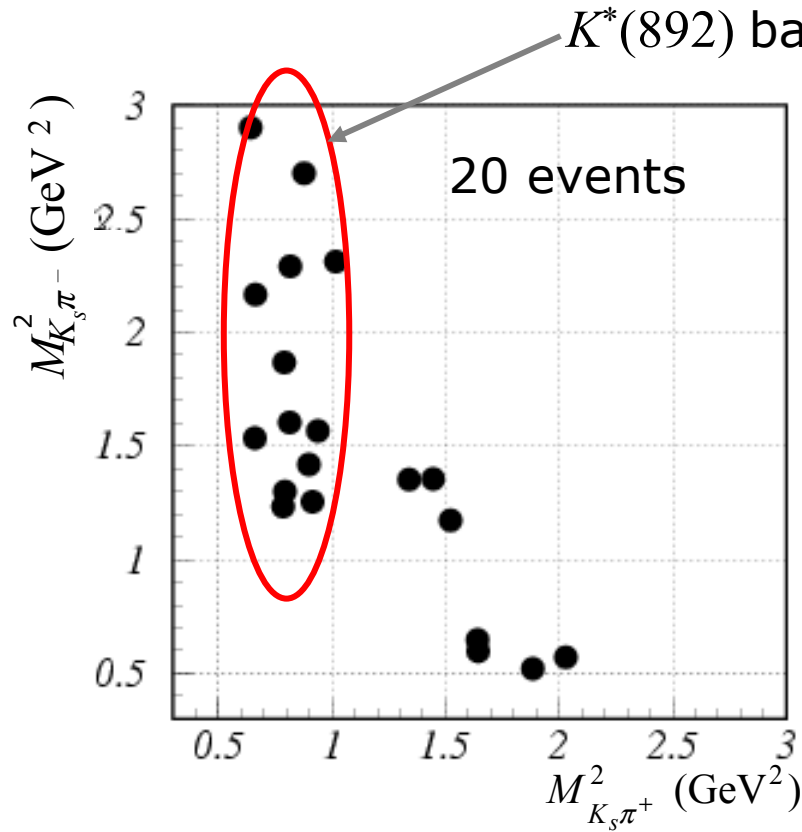


$B^+ \rightarrow D^0 K^+, D^0 \rightarrow K_S \pi^+ \pi^-$ Dalitz plot

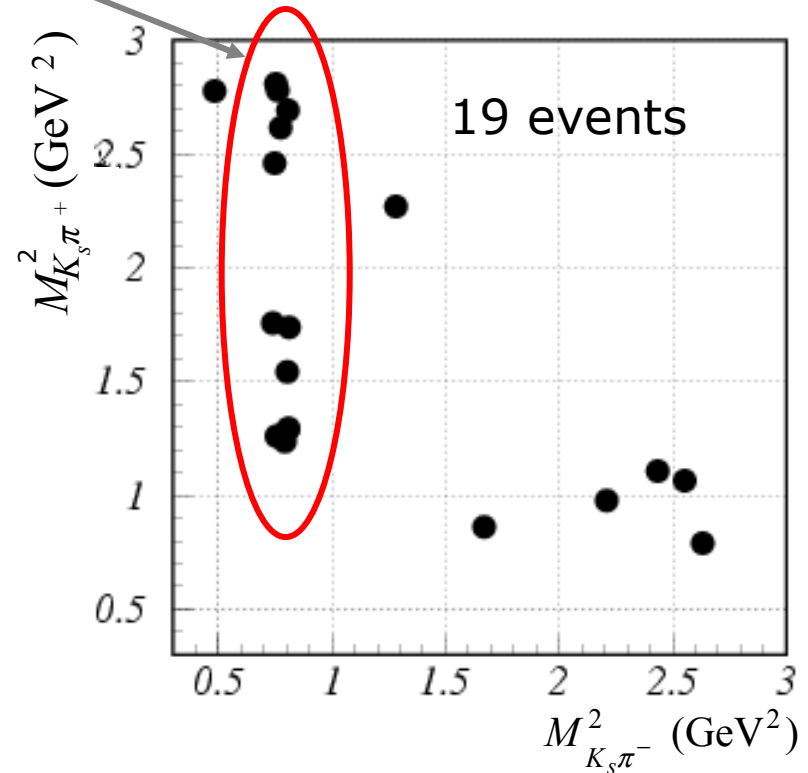




$B^+ \rightarrow D^{*0} K^+, D^0 \rightarrow K_s \pi^+ \pi^-$ Dalitz plot



D^0 from $B^+ \rightarrow D^{*0} K^+$



D^0 from $B^- \rightarrow D^{*0} K^-$
(π^+ and π^- interchanged)



Likelihood function

Minimizing logarithmic likelihood:

$$-2 \log \mathcal{L} = -2 \sum_{i=1}^N \log f(m_{+,i}^2, m_{-,i}^2) + 2 \log \int f(m_+^2, m_-^2) dm_+^2 dm_-^2$$

$m_{+,i}^2, m_{-,i}^2$ are Dalitz plot points

$$f(m_+^2, m_-^2) = |M(m_+^2, m_-^2)|^2 \times \mathcal{E}(m_+^2, m_-^2) \oplus \sigma_p(m_{\pi^+\pi^-}^2) + b(m_+^2, m_-^2)$$

Matrix element $M(m_+^2, m_-^2) = f(m_+^2, m_-^2) + r e^{i\theta} f(m_-^2, m_+^2)$

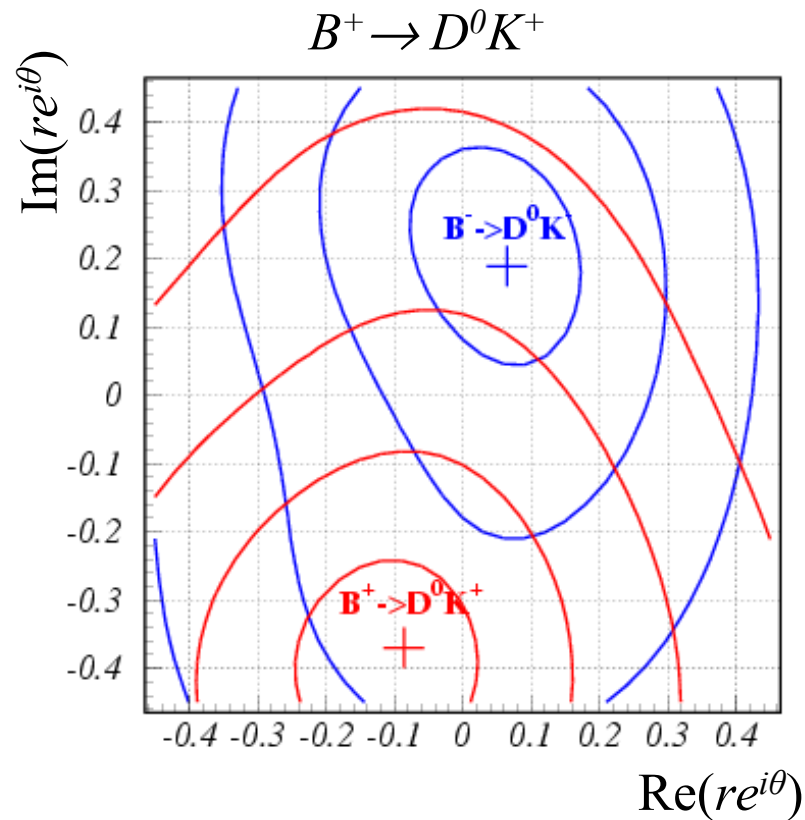
Efficiency shape $\mathcal{E}(m_+^2, m_-^2)$ - from phase-space MC

Momentum resolution $\sigma_p(m_{\pi^+\pi^-}^2)$ - from phase-space MC

Background $b(m_+^2, m_-^2)$

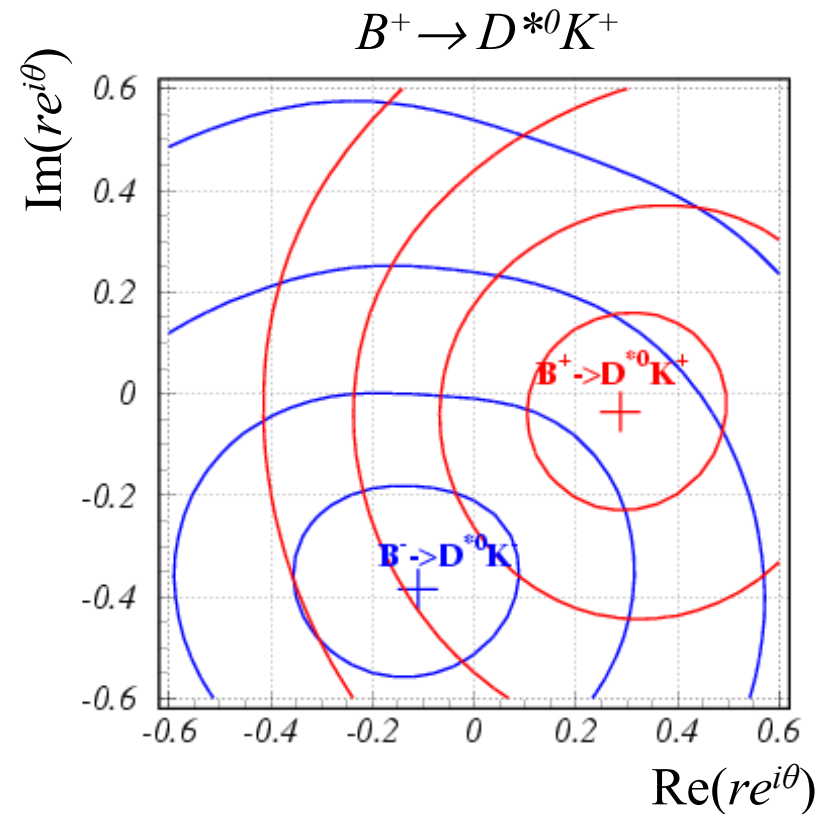


$B^+ \rightarrow D^{(*)0} K^+$ fit results



$$r_+ = 0.40 \pm 0.15, \theta_+ = 256 \pm 19^\circ$$

$$r_- = 0.21 \pm 0.15, \theta_- = 71 \pm 37^\circ$$



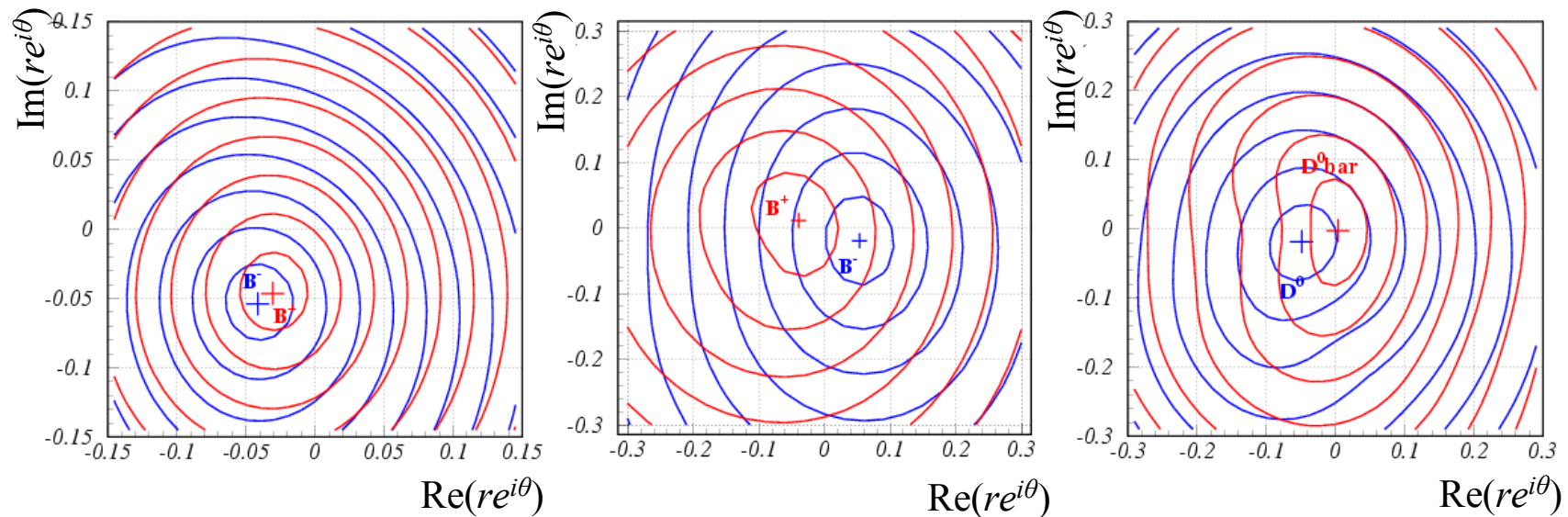
$$r_+ = 0.29 \pm 0.19, \theta_+ = 353 \pm 38^\circ$$

$$r_- = 0.38 \pm 0.19, \theta_- = 249 \pm 32^\circ$$



Test sample fits

$B^+ \rightarrow D^0 \pi^+$ (1850 events) $B^+ \rightarrow D^{*0} \pi^+$ (351 events) $B^0 \rightarrow D^{*+} \pi^-$ (517 events)

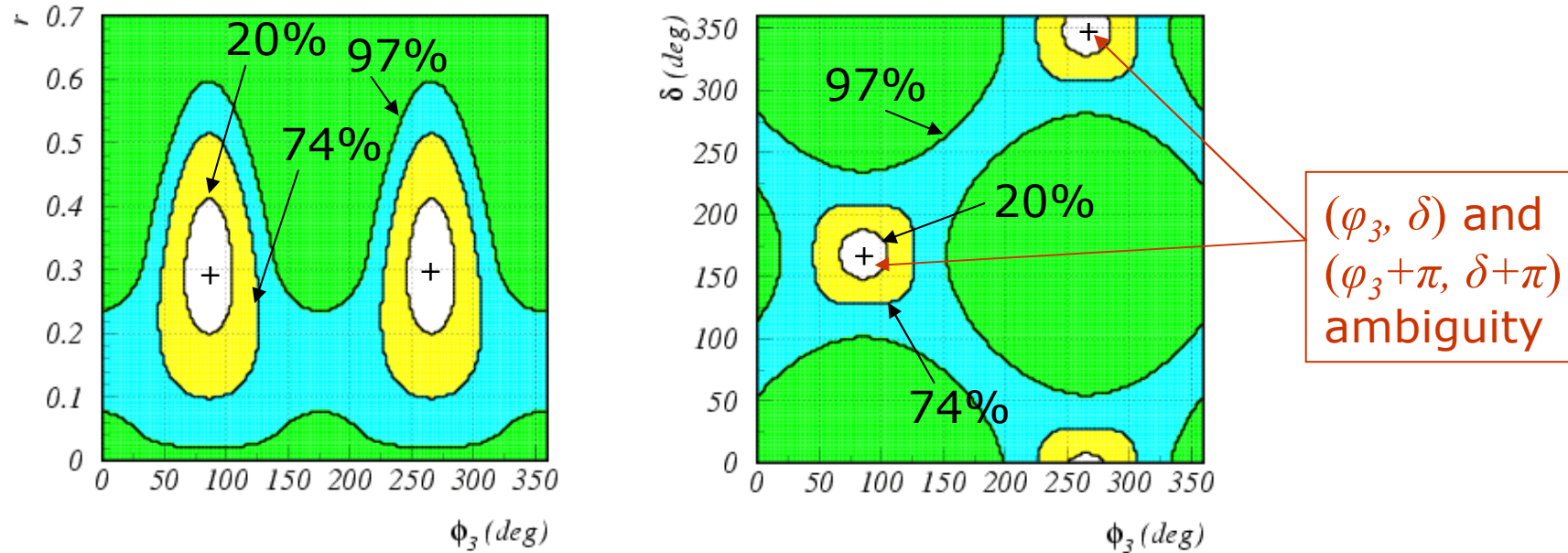


$$\begin{array}{lll}
 r_+ = 0.065 \pm 0.029, \theta_+ = 232 \pm 24^\circ & r_+ = 0.041 \pm 0.069, \theta_+ = 164 \pm 100^\circ & r_+ = 0.005 \pm 0.058, \theta_+ = 324 \pm 686^\circ \\
 r_- = 0.069 \pm 0.027, \theta_- = 228 \pm 23^\circ & r_- = 0.057 \pm 0.054, \theta_- = 340 \pm 65^\circ & r_- = 0.052 \pm 0.053, \theta_- = 201 \pm 57^\circ
 \end{array}$$

Bias in $B^+ \rightarrow D^0 \pi^+$ sample (background, fluctuation?),
however, **no CP violation observed**



$B^+ \rightarrow D^0 K^+$ constraints



$r = 0.28^{+0.09}_{-0.11}$, $\varphi_3 = 86 \pm 20^\circ$, $\delta = 168 \pm 20^\circ$ — $< 68\%$ CL interval from MC-based PDF

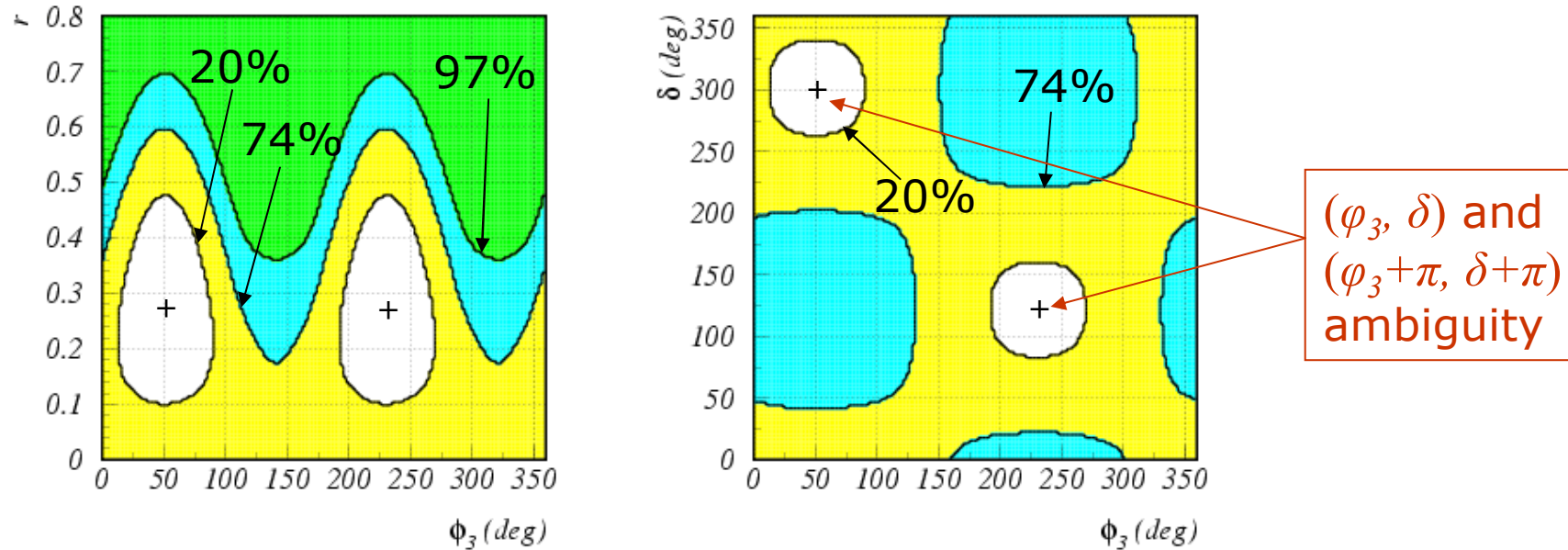
$0.07 < r < 0.45$, $37^\circ < \varphi_3 < 135^\circ$, $119^\circ < \delta < 217^\circ$ — $< 95\%$ CL interval.

CP violation significance: 94% ($\varphi_3 \neq 0$).

$r > 0$ with 97% CL.



$B^+ \rightarrow D^{*0} K^+$ constraints



$r < 0.25, \varphi_3 = 51 \pm 47^\circ, \delta = 302 \pm 47^\circ$ — $< 68\%$ CL interval from MC-based PDF

$r < 0.44, -31^\circ < \varphi_3 < 133^\circ, 220^\circ < \delta < 384^\circ$ — $< 95\%$ CL interval.

CP violation significance: 38% ($\varphi_3 \neq 0$).



Estimation of systematic errors

	$B^+ \rightarrow D^0 K^+$	$B^+ \rightarrow D^{*0} K^+$
Background shape	4.6°	1.3°
Background fraction	0.1°	0.6°
Efficiency shape	3.5°	0.8°
Momentum resolution	2.5°	2.5°
$B^+ \rightarrow D^0 \pi^+$ test sample bias:	11°	11°
Total	13°	11°



Model uncertainty

D^0 decay amplitude $f = |f(m_+^2, m_-^2)| e^{i\phi(m_+^2, m_-^2)}$

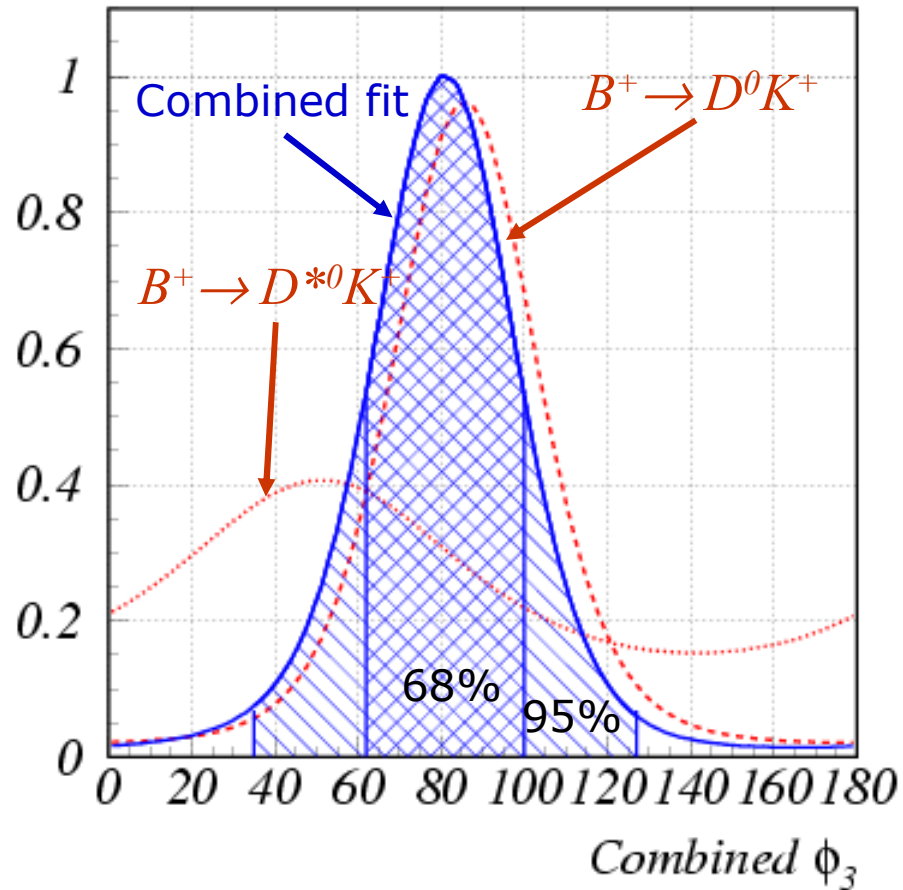
$|f(m_+^2, m_-^2)|^2$ directly measured

$\phi(m_+^2, m_-^2)$ model-dependent

Fit model	$(\Delta\phi_3)_{\max}, ^\circ$
K^*, ρ, ω, f_0 + non-resonant	9.9
Meson formfactors $F_r = F_D = 1$	3.1
Constant BW width $\Gamma(q^2) = \text{Const}$	4.7
Non-resonant amplitude $a_{NR} = 0$	0.4
No $\sigma(500)$	0.7
Total	11



$B^+ \rightarrow D^0 K^+$ and $B^+ \rightarrow D^{*0} K^+$ combined



Multiply ϕ_3 PDF's for
 $B^+ \rightarrow D^0 K^+$ and $B^+ \rightarrow D^{*0} K^+$
 samples
 (r and δ left independent)

Stat. confidence intervals:

$$\phi_3 = 81 \pm 19^\circ \text{ (68\% CL)}$$

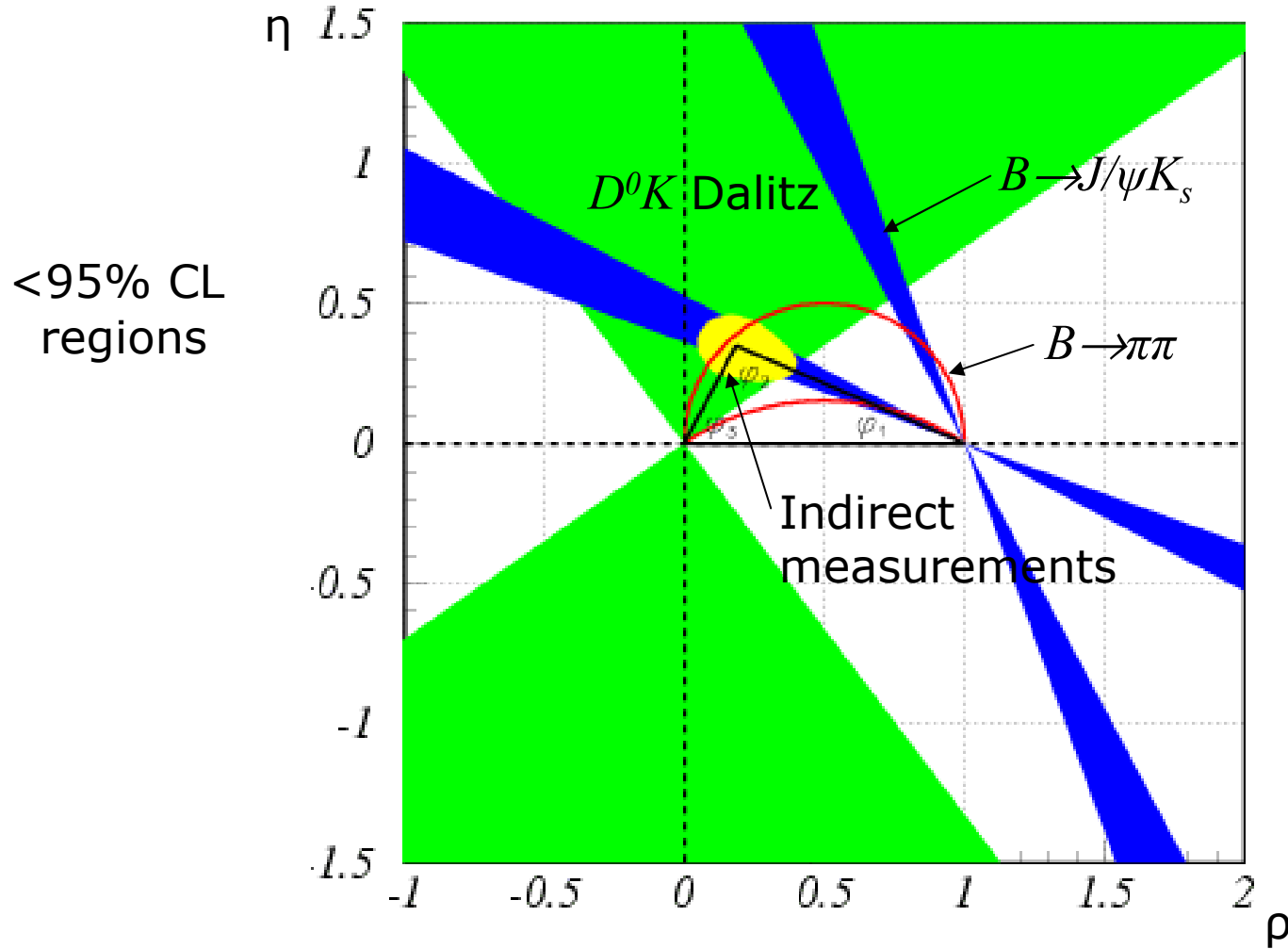
$$\phi_3 = 81 \pm 46^\circ \text{ (95\% CL)}$$

Combined result:

$$\phi_3 = 81 \pm 19^\circ \pm 13^\circ(\text{syst}) \pm 11^\circ(\text{model})$$



Constraints on unitarity triangle





Conclusion

- $B^+ \rightarrow D^0 K^+$ and $B^+ \rightarrow D^{*0} K^+$, $D^0 \rightarrow K_s \pi^+ \pi^-$ samples analyzed with 140 fb^{-1}
 $\varphi_3 = 81^\circ \pm 19^\circ \pm 13^\circ (\text{syst}) \pm 11^\circ (\text{model})$ for combined fit
95% CL interval from combined fit: $35^\circ < \varphi_3 < 127^\circ$
- Direct CP violation effect significance is 94%.
- A new promising method to measure φ_3 using Dalitz plot analysis of D^0 from $B \rightarrow D^{(*)0} K$ decay is applied to the data collected by Belle.
- Advantages:
 - Higher statistical power than methods based on branching fractions
 - No absolute branching fractions involved \Rightarrow lower detector systematics
 - Model-independent approach exists based on the $c\tau$ -factory data.
- The precision can be increased by adding other suitable modes (neutral B decays, other three- and four-body D^0 decays)



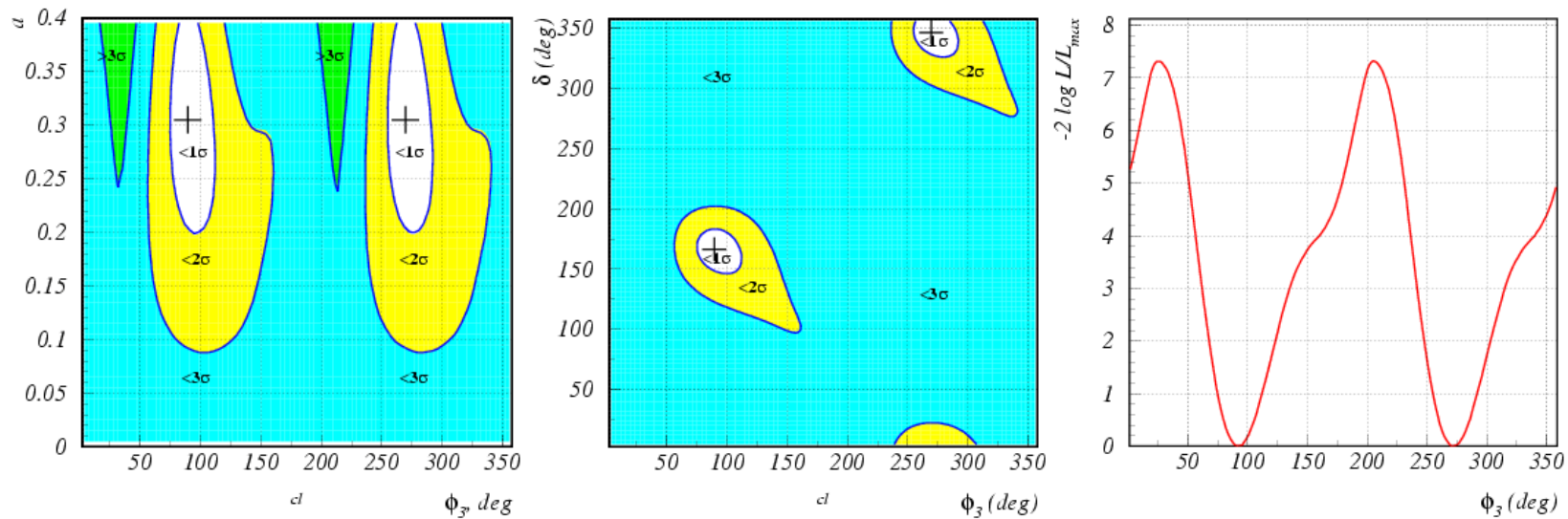
$D^0 \rightarrow K_s \pi^+ \pi^-$ fit result (discussion)

- Needed to introduce two scalars in $\pi^+ \pi^-$ channel:
 - σ_1 with mass $M=538 \pm 9$ MeV, BW width $\Gamma=452 \pm 15$ MeV
 - σ_2 with mass $M=1048 \pm 8$ MeV, BW width $\Gamma=109 \pm 11$ MeV
- Large non-resonant amplitude observed.
 - Correlated with σ_1 amplitude:
 - $a_{\text{NR}}=4.66 \pm 0.15$ for $a_\sigma=0$ (compared to 6.1 ± 0.3)
 - $a_\sigma=0.78 \pm 0.05$ for $a_{\text{NR}}=0$ (compared to 1.65 ± 0.10)
 - Probably indicates poor description of σ_1 . Consider as a systematic effect.
- Use symmetric set of resonances, i.e. take doubly Cabibbo suppressed partners for all flavor-specific modes ($K^*(892)^+ \pi^-$, $K^*_0(1430)^+ \pi^-$, $K^*_0(1430)^+ \pi^+$, $K^*(1680)^+ \pi^-$). Otherwise systematic bias of opposite flavor admixture r .



$B^+ \rightarrow D^0 K^+$ fit result

Error estimation from the fit likelihood



CL vs. (δ, φ_3)

CL vs. (r, φ_3)

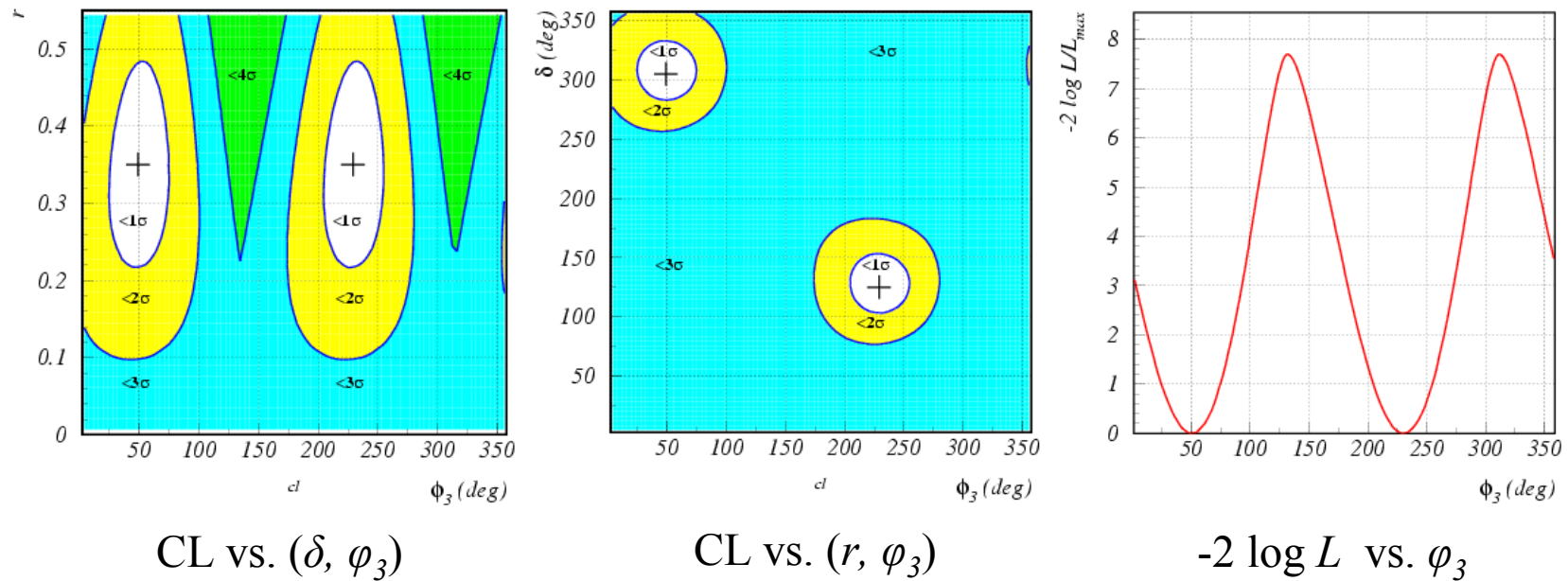
$-2 \log L$ vs. φ_3

$$r=0.31 \pm 0.11, \varphi_3=86 \pm 17^\circ, \delta=168 \pm 17^\circ \text{ or } (\varphi_3 + \pi, \delta + \pi)$$



$B^+ \rightarrow D^{*0} K^+$ fit result

Error estimation from the fit likelihood



$$r=0.34 \pm 0.14, \varphi_3=51 \pm 25^\circ, \delta=302 \pm 25^\circ \text{ or } (\varphi_3 + \pi, \delta + \pi)$$



Parameterization of fit PDF

PDF for the single Dalitz plot fit:

$$d^2 P(r, \theta) \propto \exp\left[-\frac{(r \cos \theta - \bar{r} \cos \bar{\theta})^2 + (r \sin \theta - \bar{r} \sin \bar{\theta})^2}{2\sigma^2}\right] r dr d\theta$$

$\bar{r}, \bar{\theta}$ - true values, r, θ - reconstructed values

PDF of *reconstructed* values r, φ_3, δ for a given set of *true* values $\bar{r}, \bar{\varphi}_3, \bar{\delta}$ for combined fit of two Dalitz plots (B^+ and B^-):

$$\frac{d^3 P}{dr d\varphi_3 d\delta}(r, \varphi_3, \delta) \propto \frac{d^2 P}{dr d\theta_+}(r, \delta + \varphi_3) \cdot \frac{d^2 P}{dr d\theta_-}(r, \delta - \varphi_3)$$

Can also obtain PDF of *true* values $\bar{r}, \bar{\varphi}_3, \bar{\delta}$ for a given set of *reconstructed* values r, φ_3, δ with this parameterization. This PDF is used to obtain confidence intervals and significance.

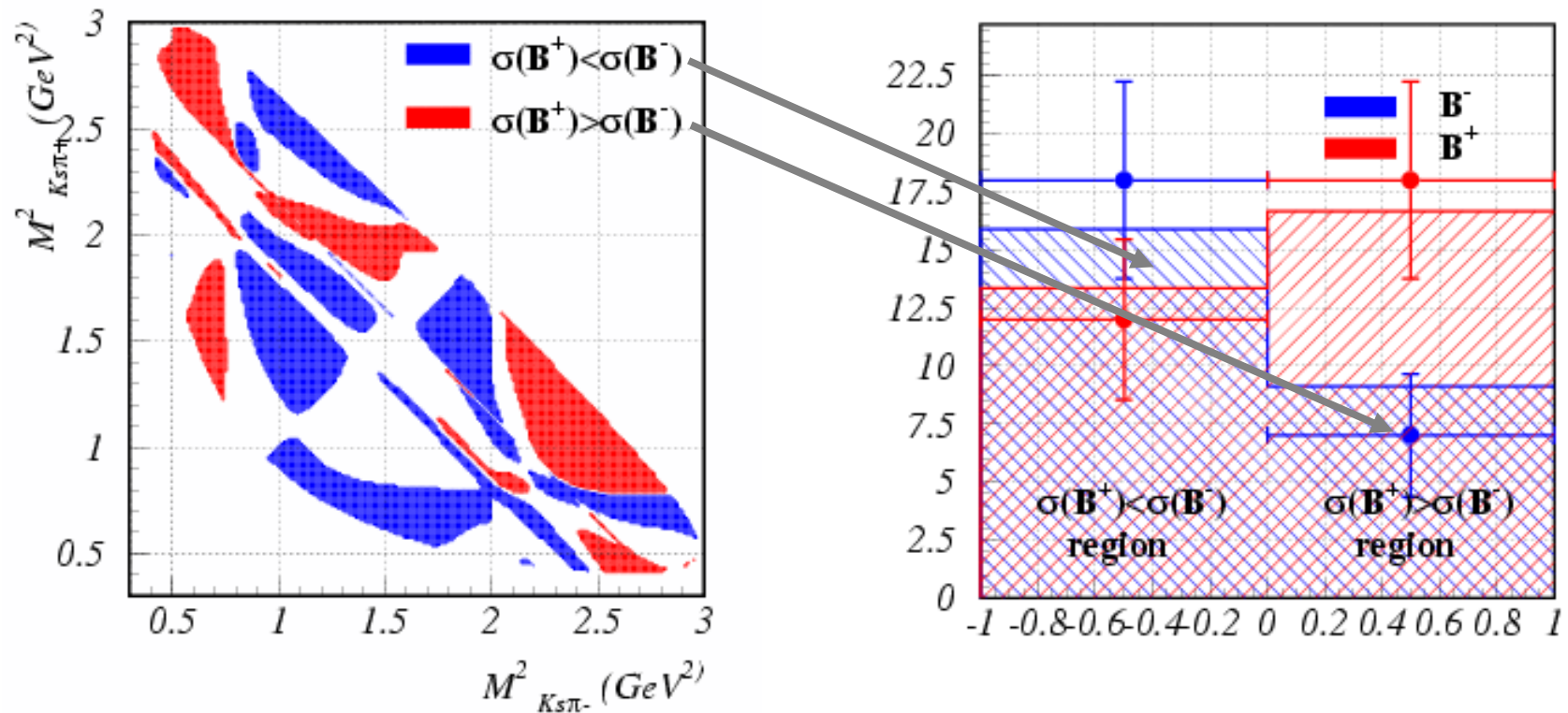


Backgrounds

	$B \rightarrow D^0 K$	$B \rightarrow D^{*0} K$
<ul style="list-style-type: none"> • $q\bar{q}$ combinatorial (including real D^0) <ul style="list-style-type: none"> – Fraction: from ΔE distribution – Dalitz plot: from continuum data 	22.1%	9.0%
<ul style="list-style-type: none"> • Other B decays <ul style="list-style-type: none"> – Fraction and Dalitz plot: from generic MC 	2.2%	2.1%
<ul style="list-style-type: none"> • “Wrong” particles in D^0 decay <ul style="list-style-type: none"> – Fraction and Dalitz plot: from $B \rightarrow D^0 K$ MC 	1.0%	0.6%
<ul style="list-style-type: none"> • $B \rightarrow D^0 \pi$ with K/π misID <ul style="list-style-type: none"> – Fraction: from ΔE distribution – Dalitz plot: D^0 	0.4%	0.4%
<ul style="list-style-type: none"> • Flavor tagging K from combinatorics <ul style="list-style-type: none"> – Fraction from MC 	<0.4%	<0.4%



Illustration of CP asymmetry



Select regions on Dalitz plot with $\sigma(B^+) > \sigma(B^-)$ or $\sigma(B^-) > \sigma(B^+)$ by $>20\%$

Calculate the number of B^+ and B^- decays in each of the regions.

CP asymmetry \Rightarrow difference in number of B^+ and B^- events