

Recent Results from KTeV

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- $K_L \rightarrow \pi^0 \mu^+ \mu^-$
- $\Xi^0 \rightarrow \Sigma^+ \mu^- \nu$
- $|V_{us}|$ and related measurements

Phys Rev Lett **93**, 181802 (2004)

Phys Rev **D80**, 092007 (2004)

Phys Rev **D70**, 092005 (2004)

Phys Rev **D71**, 012001 (2005)

$$K_L \rightarrow \pi^0 \mu^+ \mu^-$$

Background from radiative muonic Dalitz decay of the kaon, $K_L \rightarrow \mu^+ \mu^- \gamma \gamma$

$$Br(K_L \rightarrow \mu^+ \mu^- \gamma \gamma, m_{\gamma\gamma} > 1 \text{ MeV}) =$$

$$(10.4^{+7.5}_{-5.9 \text{ STAT}} \pm 0.7 \text{ SYS}) \times 10^{-9}$$

Phys.Rev.D62:112001(2000)

$$|K_L\rangle \approx |K_{\text{ODD}}\rangle + \varepsilon |K_{\text{EVEN}}\rangle$$

Indirect CPV

$$\rightarrow \pi^0 \gamma^* \rightarrow \pi^0 \ell^+ \ell^-$$

$$Br(K_L \rightarrow \pi^0 \ell^+ \ell^-) =$$

$$|\varepsilon|^2 \frac{\tau_L}{\tau_S} Br(K_S \rightarrow \pi^0 \ell^+ \ell^-)$$

Direct CPV

$$\rightarrow \pi^0 \gamma^* \rightarrow \pi^0 Z^* \rightarrow \pi^0 \ell^+ \ell^-$$

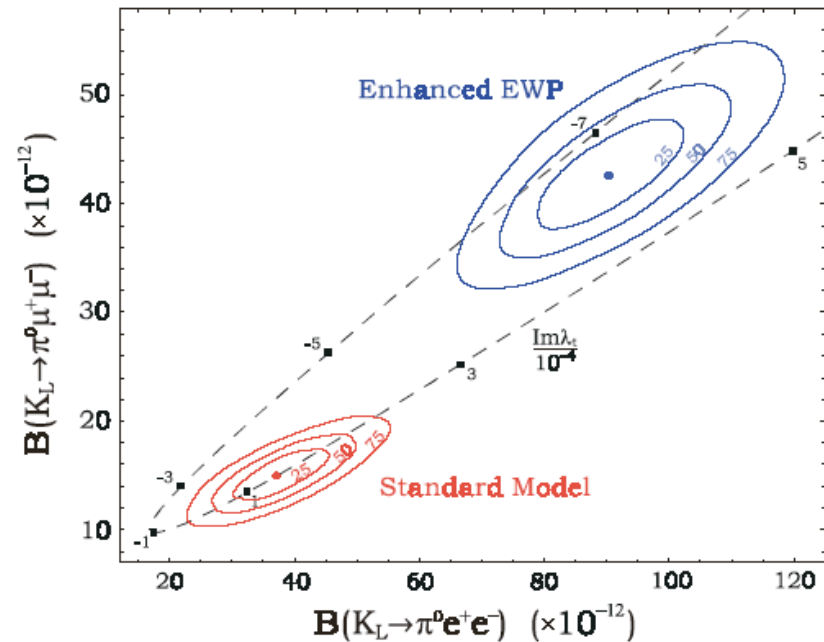
$$\pi^0 W^{+*} W^{-*}$$

$$\rightarrow \pi^0 \gamma^* \gamma^* \rightarrow \pi^0 \ell^+ \ell^- \quad \text{CPC}$$

Theoretical:

*Isidori, Smith & Unterdorfer,
Eur.Phys.J.C36:57-66(2004)*

Combo of $\pi^0\mu^+\mu^-$ & $\pi^0e^+e^-$
valuable in elucidating new physics



Experimental:

Park, et.al. (HyperCP), Phys.Rev.Lett. 94,021801 (2005)

- $Br(\Sigma^+ \rightarrow p\mu^+\mu^-) = (8.6^{+6.6}_{-5.4} \text{STAT} \pm 5.5 \text{SYST}) \times 10^{-8}$ (3 events)
- Expectation is $\sim 0.1 \times 10^{-8}$
- All 3 events at the same mass: 214.3 ± 0.5 MeV; C.L. for this in S.M. is 0.8%

May indicate a new neutral intermediate state, P^0

KTeV's existing limit on $\pi^0\mu^+\mu^-$ helps constrain P^0

$Br(\Sigma^+ \rightarrow p\mu^+\mu^-)$ is too small for P^0 to likely be a hadron - it is closer to the sort of rate typical of EM interactions

$(J)^P$ conservation limits a pointlike P^0 to $(J)^P = 0^-$ or 1^- ; but if P^0 is 1^- it will contribute to $K_L \rightarrow \pi^0\mu^+\mu^-$

From HyperCP's $Br(\Sigma^+ \rightarrow pP^0)$, PDG lifetimes for Σ^+ , K_L and our limit $Br(K_L \rightarrow \pi^0\mu^+\mu^-) < 3.8 \times 10^{-10}$ *Phys.Rev.Lett.* **84**,5279(2000)

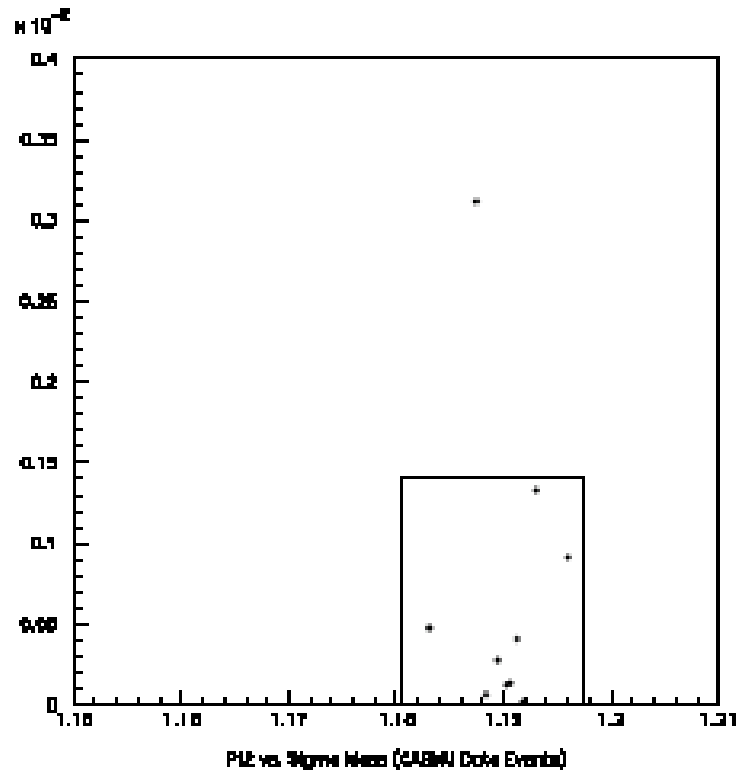
$$\Gamma(\Sigma^+ \rightarrow pP^0) \sim 2.5 \times 10^{-19} \text{ MeV}$$

$$\Gamma(K_L \rightarrow \pi^0\mu^+\mu^-) < 4.8 \times 10^{-24} \text{ MeV}$$

Rules out P^0 is $J = 1^-$ hypothesis

**New limit on $Br(K_L \rightarrow \pi^0\mu^+\mu^-)$
from full KTeV dataset in progress**

Observation of $\Xi^0 \rightarrow \Sigma^+ \mu^- \nu$



Normalized to $\Xi^0 \rightarrow \Lambda \pi^0$, $\Lambda \rightarrow p \pi^-$

With 9 events from '99 dataset,
no background events seen in
wrong sign, or in 10x MC sample -

Preliminary Result

$$\text{BR}_{\Xi^0 \rightarrow \Sigma^+ \mu^- \bar{\nu}_\mu} = (4.3 \pm 1.4) \times 10^{-6}$$

Theoretical Prediction: 2.3×10^{-6}

$|V_{us}|$ etc.

Long standing issue: 1st row unitarity $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 \neq 1$

BNL E865 (May 2003) found a higher value @ $\sim 2.2 \sigma$ level
 for $Br(K^+ \rightarrow \pi^0 e^+ \nu)$ consistent with unitarity
 but giving $|V_{us}| \sim 2.7\sigma$ above existing $Br(K_L \rightarrow \pi^\pm e^\pm \nu)$ value.

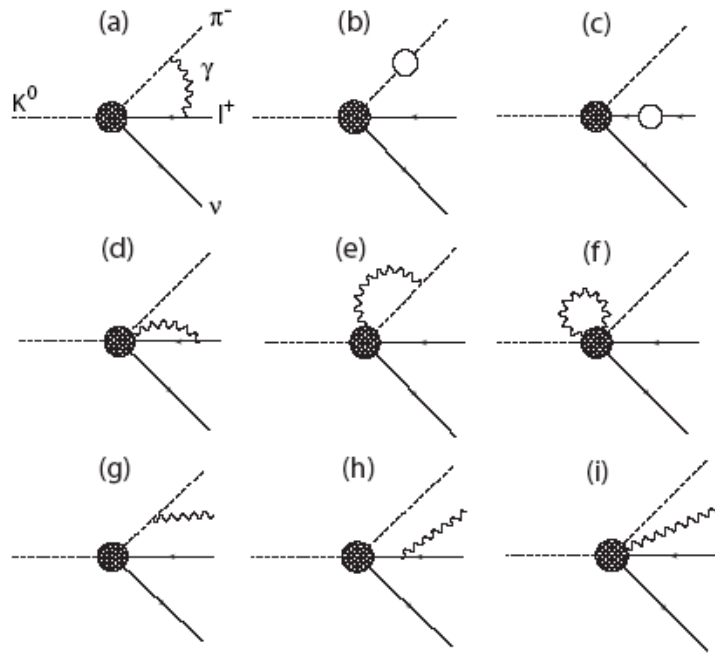
$$\Gamma_{\ell 3} = \frac{Br(K_L \rightarrow \pi^\pm \ell^\mp \nu)}{\tau_L} = \left(\frac{G_F^2 m_K^5}{384 \pi^3} \right) S_{EW} f_+^2(t=0) (1 + \delta_\ell) |V_{us}|^2 \int \hat{f}^2$$

- S_{EW} Short range EW & QCD corrections - same for e, μ
- $f_+(0)$ Form factor at $t = (P_\ell + P_\nu)^2 = 0$; we use 0.961 ± 0.008
[Leutwyler & Roos, 1984]
- δ_ℓ Long range (mode-dependent) radiative corrections
- $\int \hat{f}^2$ Integral over phase space of form factor squared

Step 1: Radiative corrections

$$\Gamma_{\ell 3} = \frac{Br(K_L \rightarrow \pi^\pm \ell^\mp \nu)}{\tau_L} = \left(\frac{G_F^2 m_K^5}{384 \pi^3} \right) S_{EW} f_+^2(t=0) (1 + \delta_\ell) |V_{us}|^2 \int \hat{f}^2$$

T.Andre, hep-ph/0406006



Take

$$\langle \pi^-(p_\pi) | \bar{s}_L \gamma^\alpha u_L | K^0(p_K) \rangle = f_+(t)[p_K + p_\pi] + f_-(t)[p_K - p_\pi]$$

Evaluate with linear, quadratic and pole model form factors f

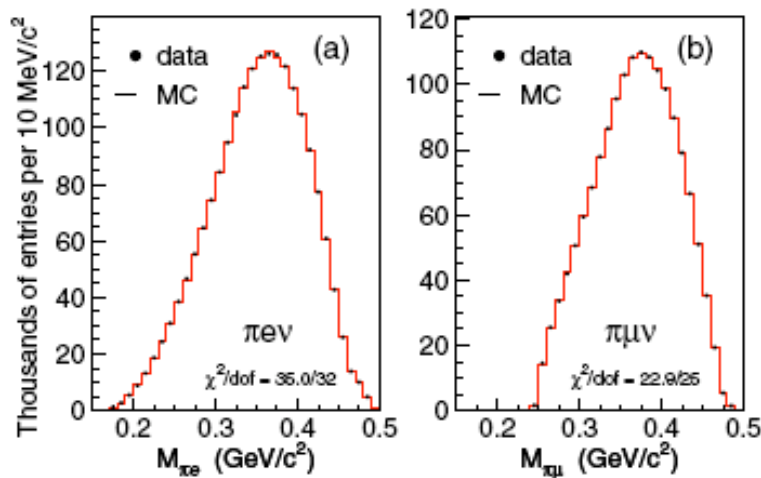
Step 2: Form factors

$$\Gamma_{\ell 3} = \frac{Br(K_L \rightarrow \pi^\pm \ell^\mp \nu)}{\tau_L} = \left(\frac{G_F^2 m_K^5}{384 \pi^3} \right) S_{EW} f_+^2(t=0) (1 + \delta_\ell) |V_{us}|^2 \int \hat{f}^2$$

We parameterize with $f_+(t)$ and $f_0(t) = f_+(t) + \frac{t}{m_K^2 - m_\pi^2} f_-(t)$

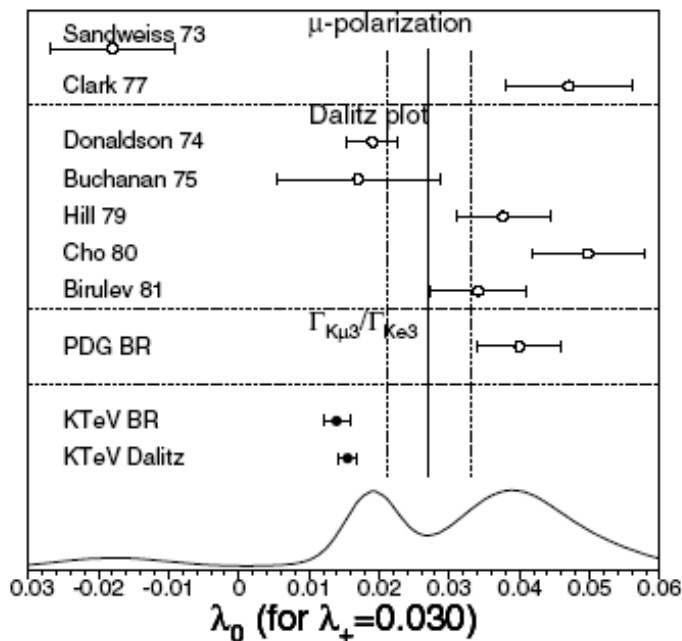
f_i expanded in powers of t / m_π^2 ; coefficients are λ_i

- Since p_K is not known, there is a two-fold reconstruction ambiguity due to unseen ν
- We use $t_\perp^\ell = (P'_\ell + P'_\nu)^2$ or $t_\perp^\pi = (P'_K - P'_\pi)^2$ - Basically, t evaluated without longitudinal coordinates to momenta. Costs $\sim 15\%$ of statistical power
- Some fits also use $m_{\ell\pi}$



	K_{e3}	$K_{\mu3}$
Linear model $\times 10^{-3}$		
λ_+	28.32 ± 0.57	27.45 ± 1.08
λ_0	-	16.57 ± 1.25
Quadratic model $\times 10^{-3}$		
λ_+'	21.67 ± 1.99	17.03 ± 3.65
λ_+''	2.87 ± 0.87	4.43 ± 1.49
λ_0	-	12.81 ± 1.83

Pole model fits also reported...



Linear model λ_+ values consistent with PDG values.

Quadratic term significant at 4σ level
Lowers phase space integral by $\sim 1\%$.

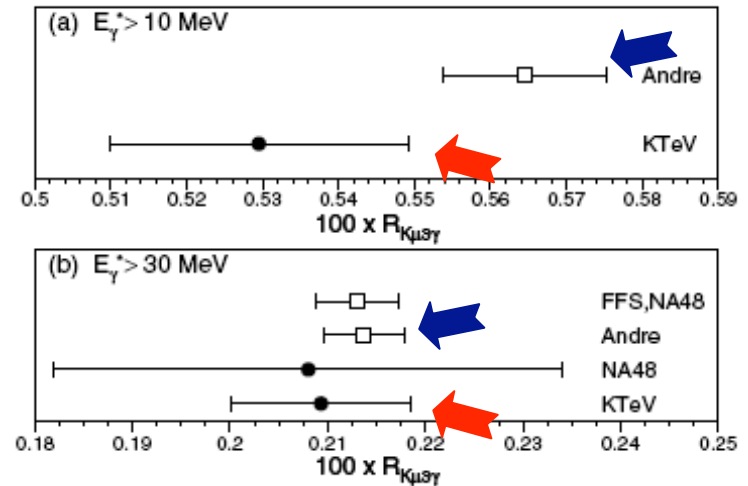
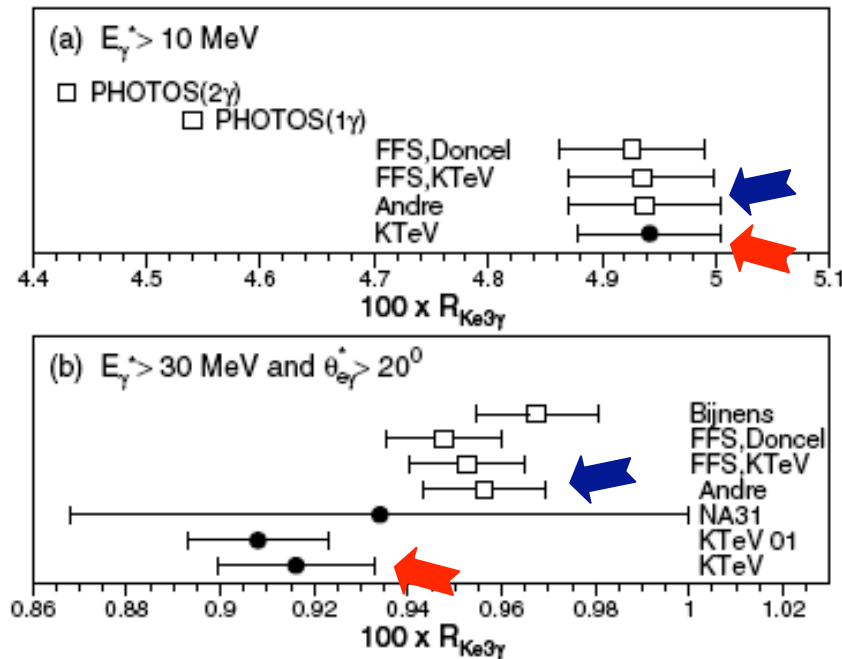
Step 3: Check steps 1&2 with $K_L \rightarrow \pi \ell \nu \gamma$

$$R_{K\gamma 3\gamma} \equiv \frac{\Gamma(K_L \rightarrow \pi^\pm \ell^\mp \nu \gamma; E_\gamma^* > 10 \text{ MeV})}{\Gamma(K_L \rightarrow \pi^\pm \ell^\mp \nu + n\gamma)}$$

Acceptance corrections for 2nd γ
via PHOTOS $\sim 1.8\%$ for K_{e3}

← Andre's prediction

← KTeV's measurement



Step 4: Get the branching ratio

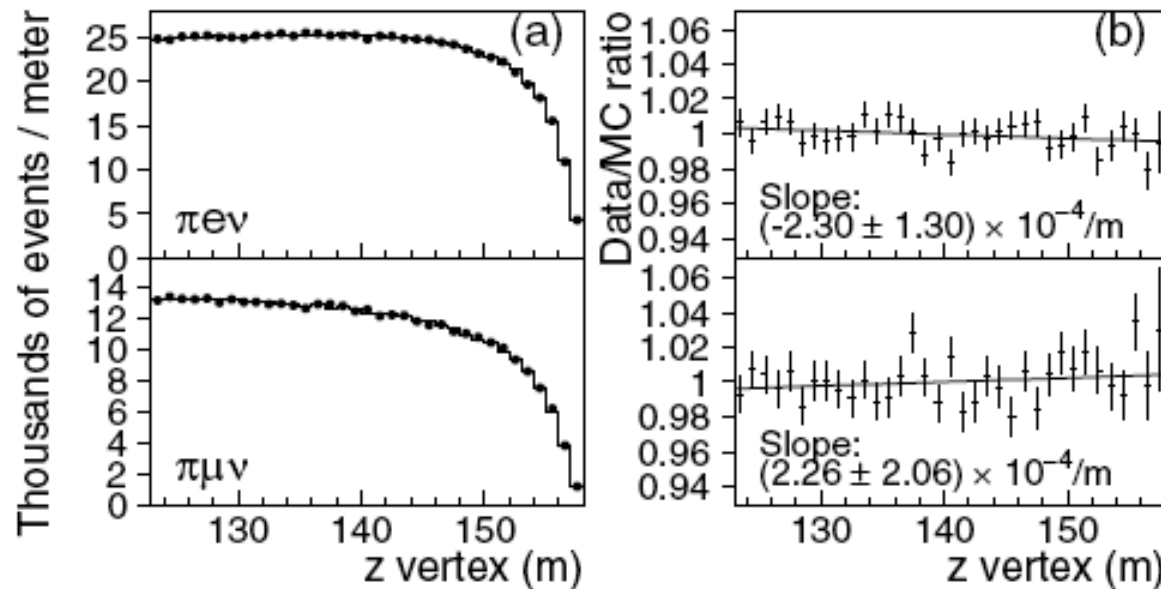
$$\Gamma_{\ell 3} = \frac{Br(K_L \rightarrow \pi^\pm \ell^\mp \nu)}{\tau_L} = \left(\frac{G_F^2 m_K^5}{384 \pi^3} \right) S_{EW} f_+^2(t=0) (1 + \delta_\ell) |V_{us}|^2 \int \hat{f}^2$$

Ordinarily, would measure something like $\Gamma(K_L \rightarrow \pi^\pm \ell^\mp \nu) / \Gamma(K_L \rightarrow \text{nice})$ where the “*nice*” mode has high statistics, a well-known rate, and is similar to $K_{\ell 3}$ in the detector. Sadly, there is no “*nice*” mode.

Measure these
5 ratios, use
 $\Sigma = 1$ constraint
to get Br

$$\begin{array}{ccc} \Gamma_{K\mu 3} / \Gamma_{Ke 3} & \Gamma_{+-0} / \Gamma_{Ke 3} & \Gamma_{000} / \Gamma_{Ke 3} \\ & \Gamma_{+-} / \Gamma_{Ke 3} & \Gamma_{000} / \Gamma_{00} \end{array}$$

- Except for $\Gamma_{000}/\Gamma_{Ke3}$, all ratios have final similar states
- Except for Γ_{00}/Γ_{000} , all ratios in same trigger; this analysis similar to the ε'/ε neutral mode analysis



- $K \rightarrow \pi \mu \nu$ ratios without/with μ ID agree to $(0.08 \pm 0.02_{\text{stat}})\%$
- $K \rightarrow \pi^+ \pi^- \pi^0$ ratios without/with $\pi^0 \rightarrow \gamma \gamma$ reconstruction in CsI -factor ~ 4 change in acceptance- agree to $(0.03 \pm 0.28_{\text{stat}})\%$

More Cross-checks

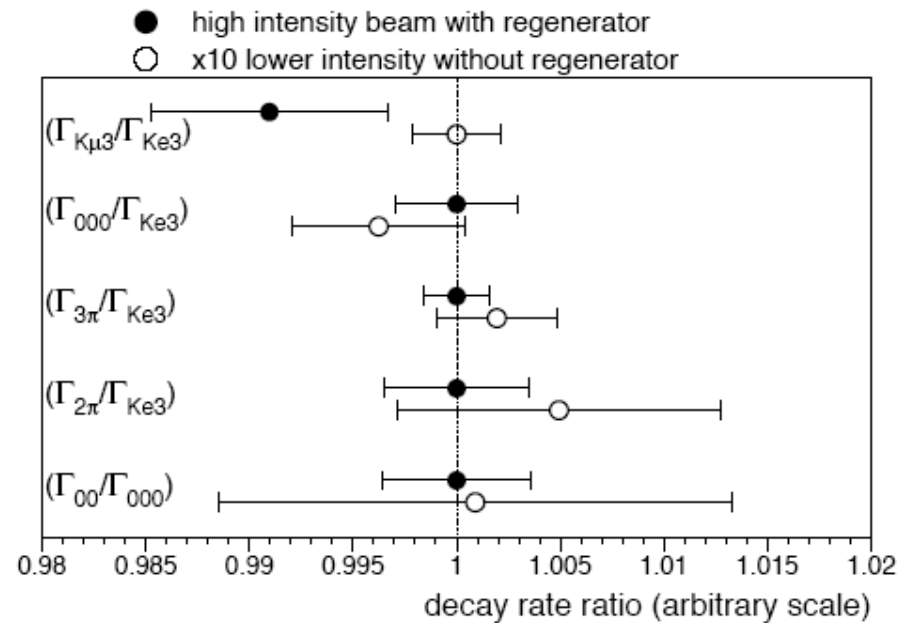
Using lepton universality,
$$\frac{\Gamma_{K\mu 3}}{\Gamma_{Ke 3}} = \frac{1 + \delta_\mu}{1 + \delta_e} \cdot \frac{\int \hat{f}_\mu}{\int \hat{f}_e}$$

Taking δ_ℓ from our radiative correction algorithm, phase-space integrals from our form factor measurements

$$\Gamma_{K\mu 3} / \Gamma_{Ke 3} = 0.6660 \pm 0.0019$$

And from the direct measurement,

$$\Gamma_{K\mu 3} / \Gamma_{Ke 3} = 0.6640 \pm 0.0014 \pm 0.0022$$



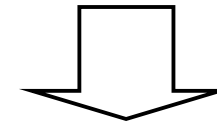
From measured ratios to $|V_{us}|$

Modes	Partial Width Ratio
$\Gamma_{K_{\mu 3}} / \Gamma_{K_{e 3}}$	$0.6640 \pm 0.0014 \pm 0.0022$
$\Gamma_{000} / \Gamma_{K_{e 3}}$	$0.4782 \pm 0.0014 \pm 0.0053$
$\Gamma_{+-0} / \Gamma_{K_{e 3}}$	$0.3078 \pm 0.0005 \pm 0.0017$
$\Gamma_{+-} / \Gamma_{K_{e 3}}$	$(4.856 \pm 0.017 \pm 0.023) \times 10^{-3}$
$\Gamma_{00} / \Gamma_{000}$	$(4.446 \pm 0.016 \pm 0.019) \times 10^{-3}$



$$Br(K_{e3}) = 0.4067 \pm 0.0011$$

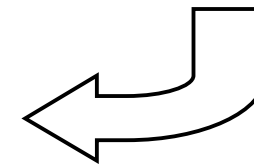
$$Br(K_{\mu 3}) = 0.2701 \pm 0.0009$$



Using $\tau_K = 51.5 \pm 0.4 \text{ ns}$

$$\Gamma(K_{e3}) = (7.897 \pm 0.065) \times 10^6 \text{ s}^{-1}$$

$$\Gamma(K_{\mu 3}) = (5.244 \pm 0.044) \times 10^6 \text{ s}^{-1}$$



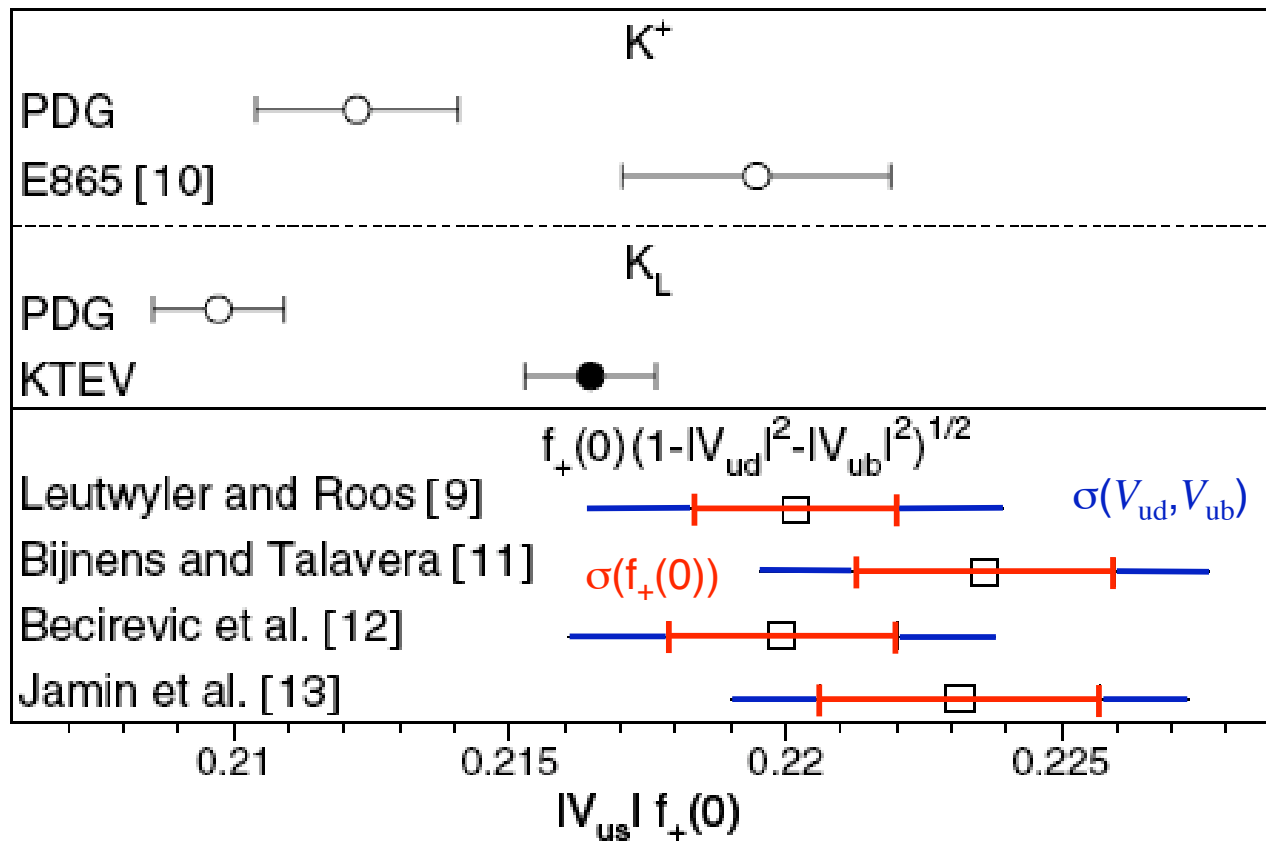
$$K_{e3}: |V_{us}| = 0.2253 \pm 0.0023$$

$$K_{\mu 3}: |V_{us}| = 0.2250 \pm 0.0023$$

$$\text{Average: } |V_{us}| = 0.2252 \pm 0.0008_{\text{KTeV}} \pm 0.0021_{\text{ext}}$$

Γ ratios,
form factors

$f_+(0)$, τ_K ,
rad corrs

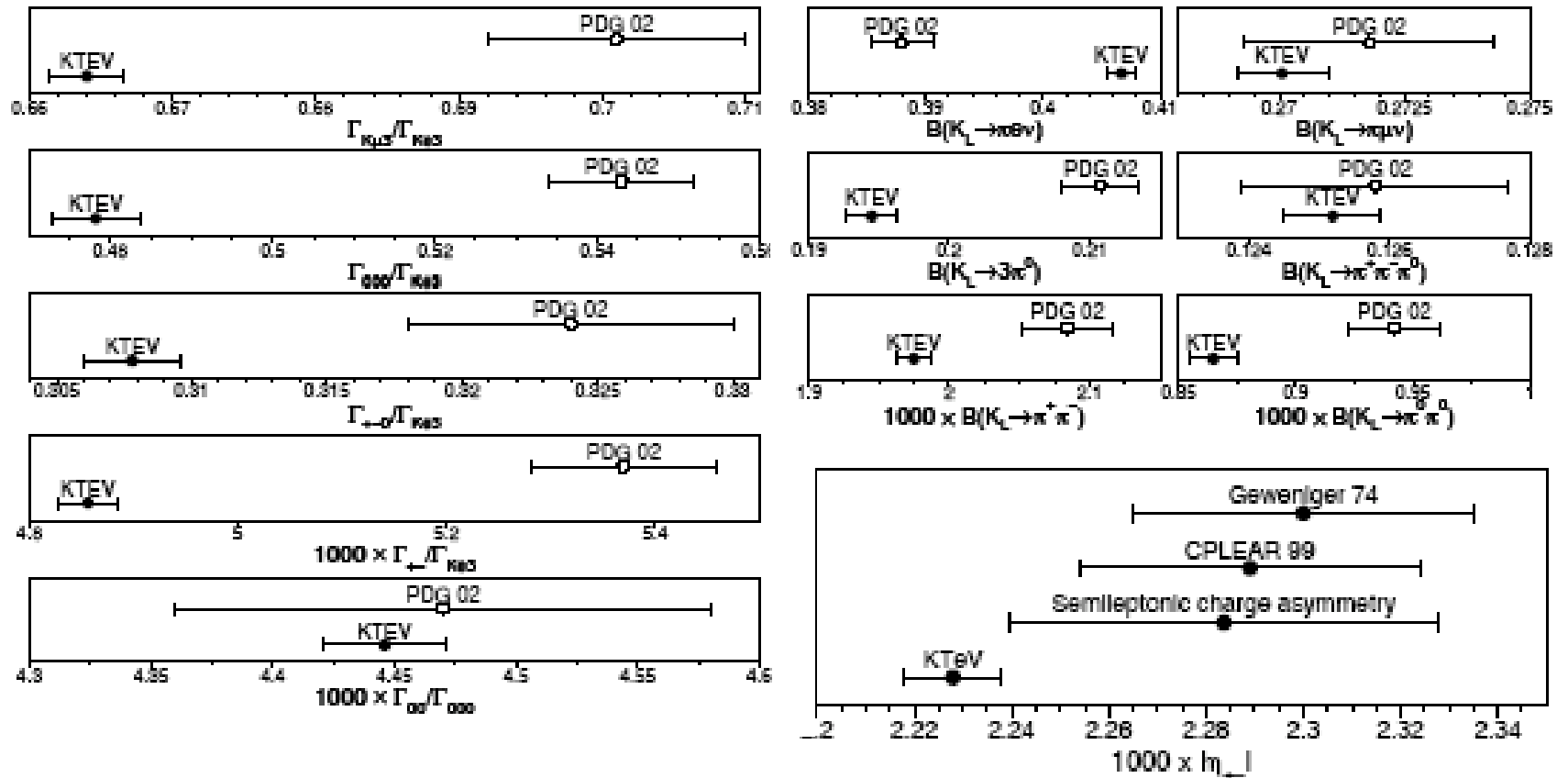


Compared to PDG-02, $Br(K_{e3})$ is $\sim 5\%$ (6σ !) higher; $Br(K_{\mu 3})$ not much changed. Phase space integrals are lower by 1.7% and 4.2% in e and μ modes, including the $\sim 1\%$ shift from quadratic term

Conclusions

- HyperCP's anomaly in $\Sigma^+ \rightarrow p\mu^+\mu^-$ is not due to a $(J)^P$ conserving vector boson
- Final KTeV result on $Br(K_L \rightarrow \pi^0\mu^+\mu^-)$ on its way -also, watch for $K_L \rightarrow e^+e^- \gamma$, $K_L \rightarrow \pi^+\pi^-e^+e^-$ form factors and branching ratio
- Preliminary results on $\Xi^0 \rightarrow \Sigma^+\mu^-\nu$ shown
- We have new and very precise results on major branching ratios, partial widths, $|\eta_{+-}|$, form factors, radiative semileptonic decays, and $|V_{us}|$ in the K_L system. They show a great deal of internal consistency and solve the CKM 1st-row unitarity problem.

Spare



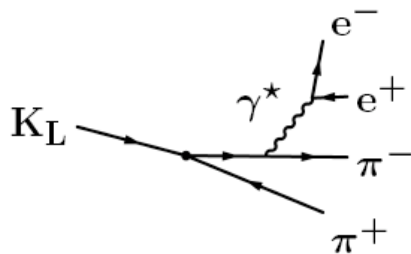
PDG 2002:

$\Gamma(\pi^\pm e^\mp \nu_e)$

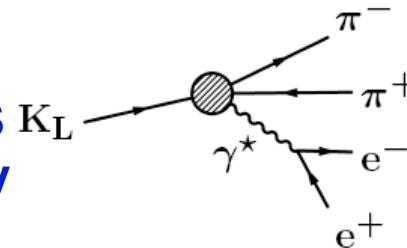
Γ_1

<u>VALUE (10^6 s^{-1})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
7.50 ± 0.08 OUR FIT		Error includes scale factor of 1.1.		
7.7 ± 0.5 OUR AVERAGE				
7.81 ± 0.56	620	CHAN	71 HBC	
$7.52^{+0.85}_{-0.72}$		AUBERT	65 HLBC	$\Delta S = \Delta Q, CP$ assumed

$K_L \rightarrow \pi^+ \pi^- e^+ e^-$



Interference between
IB and DE amplitudes
gives observable CPV



From 5241 candidates (background of 185 ± 14) in full dataset:

$$\tilde{g}_{M1} = 1.11 \pm 0.12(stat) \pm 0.07(syst)$$

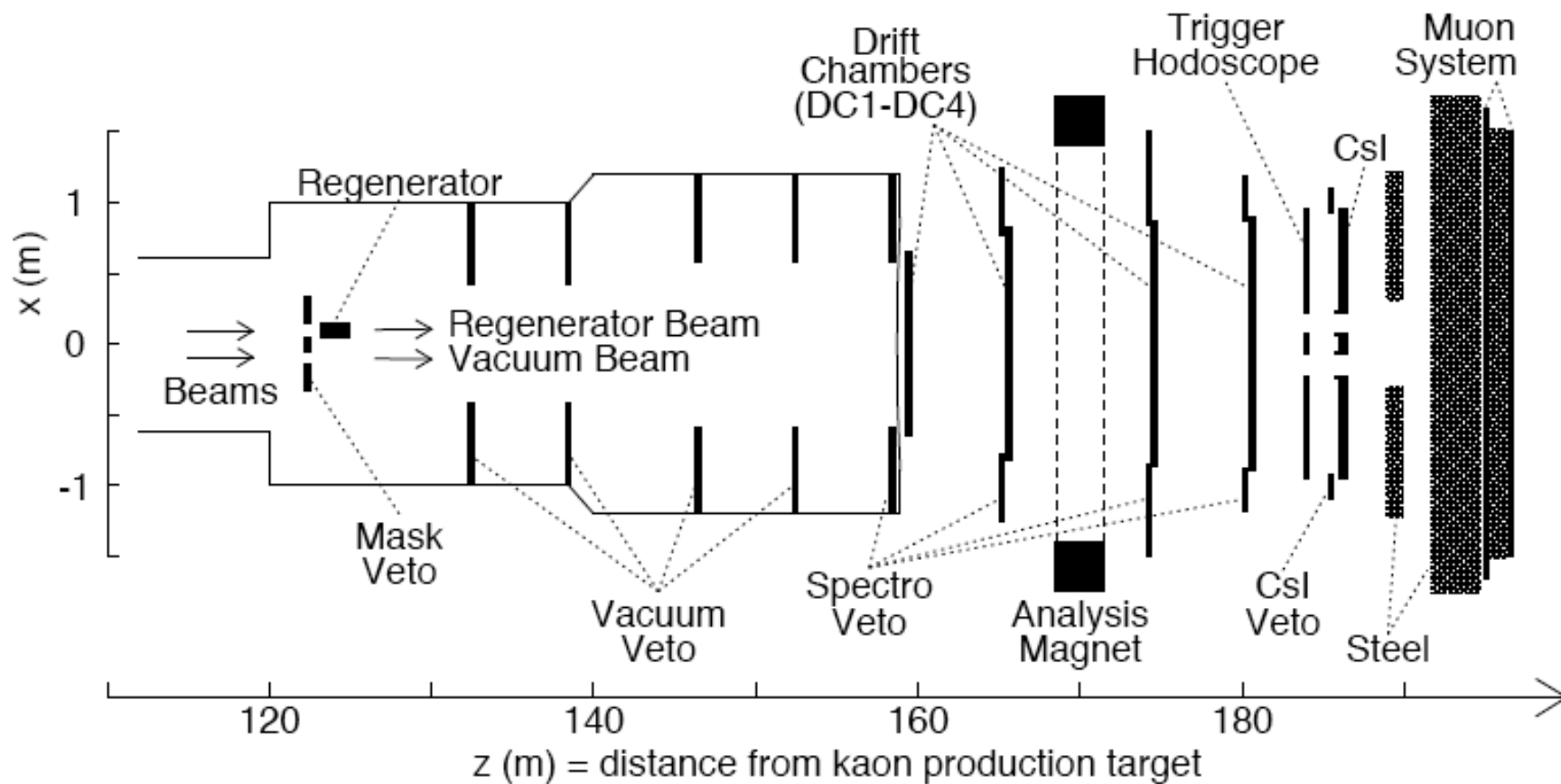
$$\frac{a_1}{a_2} = [-0.744 \pm 0.022(stat) \pm 0.032(syst)] (GeV)^2$$

$$|g_{CR}| = 0.163 \pm 0.017(stat) \pm 0.023(syst)$$

$$\frac{|g_{E1}|}{|g_{M1}|} < 0.04 (90\% CL)$$

Preliminary
Results

KTeV detector (E832)



$$\sigma(p)/p \sim [1.7 \oplus (p/14\text{GeV})] \times 10^{-3}$$

$$0.043 X_0 = 0.021 \Lambda_0 \text{ upstream of CsI}$$

$$\sigma(E)/E \sim [4 \oplus 20/\sqrt{E}] \times 10^{-3}$$

$$\pi \text{ punchthrough} = (1.0 \pm 0.1) \times 10^{-4} p(\text{GeV})$$