

# CLEO RESULTS ON CHARM LEPTONIC AND SEMILEPTONIC DECAYS

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## 1 Introduction

Here I will review a small selection of recent CLEO results on purely leptonic and semileptonic decays mostly of the  $D_s^+$  meson. In leptonic decays the quark and antiquark in the meson annihilate via a virtual  $W$  that materializes as a lepton ( $\ell$ ) anti-neutrino pair. To lowest order, the decay width is given by

$$\Gamma(P \rightarrow \ell\nu) = \frac{G_F^2}{8\pi} f_P^2 m_\ell^2 M_P \left(1 - \frac{m_\ell^2}{M_P^2}\right)^2 |V_{q_1 q_2}|^2, \quad (1)$$

where  $M_P$  is the  $P$  mass,  $m_\ell$  is the  $\ell$  mass,  $V_{q_1 q_2}$  is the Cabibbo-Kobayashi-Maskawa (CKM) matrix element between the constituent quarks  $q_1 \bar{q}_2$  in  $P$ , and  $G_F$  is the Fermi coupling constant. The parameter  $f_P$  is the decay constant, the quantity to be measured or calculated, that is related to the wave-function overlap of the quark and antiquark.

## 2 Leptonic Decays

Near 4.170 GeV in center-of-mass energy  $e^+e^-$  collisions produce  $D_s D_s^*$  pairs with about a 1 nb cross-section. The presence of the  $D_s^* \rightarrow \gamma D_s$  transition makes the analysis of  $D_s^+$  decays somewhat more complicated than studies at 3.770 GeV where  $D^+ D^-$  and  $D^0 \bar{D}^0$  pairs are produced.

To study  $D^+$  decays we fully reconstruct a  $D^-$  and then we use the conservation of energy and momentum to infer the presence of a missing neutrino in  $D^+ \rightarrow \ell^+ \nu$  (leptonic) or  $D^+ \rightarrow h \ell^+ \nu$  (semileptonic) decays. This is done by calculating the missing mass squared as

$$\text{MM}^2 = (E_{\text{beam}} - E_{\mu^+})^2 - (-\mathbf{p}_{D^-} - \mathbf{p}_{\mu^+})^2, \quad (2)$$

here  $E_{\text{beam}}$  is the beam energy,  $\mathbf{p}_{D^-}$  is the three-momentum of the fully reconstructed  $D^-$ , and  $E_{\mu^+}(\mathbf{p}_{\mu^+})$  is the energy (momentum) of the  $\mu^+$  candidate.  $\text{MM}^2$  peaks at zero for a missing  $\nu$ .

To reconstruct  $D^-$  tags we require that the tag candidates have a measured energy consistent with the beam energy, and have a “beam constrained mass,”  $m_{BC}$ , consistent with the  $D^-$  mass, where  $m_{BC} = \sqrt{E_{\text{beam}}^2 - (\sum_i \mathbf{p}_i)^2}$ , and  $i$  runs over all the final state particles three-momenta.

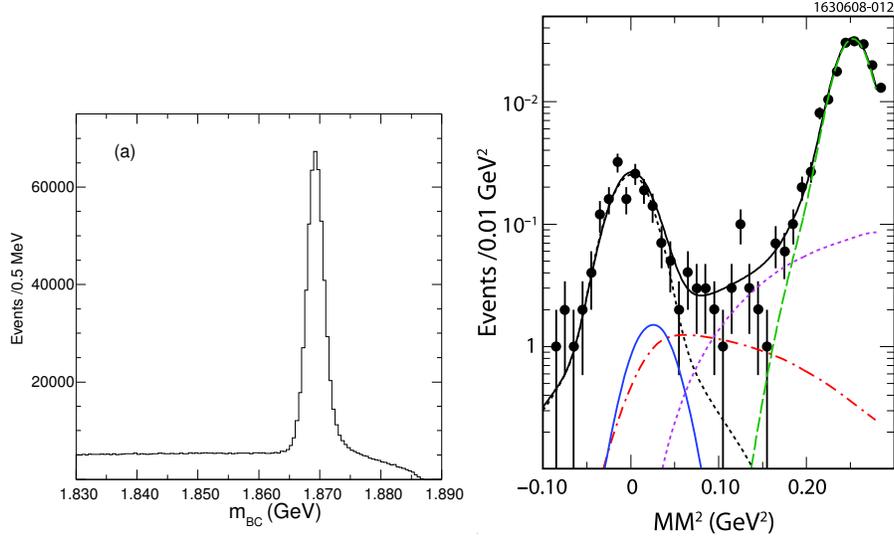


Figure 1: (a) The beam-constrained mass distributions summed over  $D^-$  decay candidates in the final states:  $K^+\pi^-\pi^-$ ,  $K^+\pi^-\pi^-\pi^0$ ,  $K_s\pi^-$ ,  $K_s\pi^-\pi^-\pi^+$ ,  $K_s\pi^-\pi^0$  and  $K^+K^-\pi^-$ . (b) Fit to the  $MM^2$ . Data are points with error bars. The black (dashed) curve centered at zero shows the signal  $\mu^+\nu$  events. The dot-dashed (red) curve that peaks around  $0.05 \text{ GeV}^2$  shows  $D^+ \rightarrow \tau^+\nu$ ,  $\tau^+ \rightarrow \pi^+\bar{\nu}$ . The solid (blue) Gaussian shaped curve centered on the pion-mass squared shows residual  $\pi^+\pi^0$ . The dashed (purple) curve that falls to zero around  $0.03 \text{ GeV}^2$  is the sum of all the other background components, except the  $\bar{K}^0\pi^+$  tail which is shown by the long-dashed (green) curve that peaks up at  $0.25 \text{ GeV}^2$ . The solid (black) curve is the sum of all the components.

Fig. 1(a) shows the  $m_{BC}$  distribution summed over all the decay modes we use for tagging. There are  $460,055 \pm 787$  plus  $89,472$  backgrounds. The fit to the  $MM^2$  distribution shown in Fig. 1(b) contains separate shapes for signal,  $\pi^+\pi^0$ ,  $\bar{K}^0\pi^+$ ,  $\tau^+\nu$  ( $\tau^+ \rightarrow \pi^+\bar{\nu}$ ), and a background shape describing three-body decays. Here we constrain the ratio of the  $\tau^+\nu/\mu^+\nu$  components to the SM ratio of 2.65. We also veto events with an extra neutral energy cluster  $> 250 \text{ MeV}$  which removes most  $\pi^+\pi^0$  events. The normalizations of the signal,  $\bar{K}^0\pi^+$ , and 3-body background shapes are allowed to float. The final result, including radiative corrections is <sup>1</sup>

$$f_{D^+} = (206.7 \pm 8.5 \pm 2.5) \text{ MeV} . \quad (3)$$

For  $D_s^+$  studies we first cut on the the invariant mass of the decay products of  $D_s^-$  tag candidates shown in Fig. 2(a), then detect an additional photon candidate from the  $D_s^*$  decay, and construct

$$MM^{*2} = (E_{\text{CM}} - E_{D_s} - E_\gamma)^2 - (\mathbf{p}_{\text{CM}} - \mathbf{p}_{D_s} - \mathbf{p}_\gamma)^2, \quad (4)$$

where  $E_{\text{CM}}$  ( $\mathbf{p}_{\text{CM}}$ ) is the center-of-mass energy (momentum),  $E_{D_s}$  ( $\mathbf{p}_{D_s}$ ) is the energy (momentum) of the fully reconstructed  $D_s^-$  tag, and  $E_\gamma$  ( $\mathbf{p}_\gamma$ ) is the energy (momentum) of the additional photon. In performing this calculation we use a kinematic fit that constrains the decay products of the  $D_s^-$  to the known  $D_s$  mass and conserves overall momentum and energy. All photon candidates in the event are tried, except for those that are decay products of the  $D_s^-$  tag candidate. Regardless of whether or not the photon forms a  $D_s^*$  with the tag, for real  $D_s^*D_s$  events the missing mass-squared  $MM^{*2}$ , recoiling against the photon and the  $D_s^-$  tag should peak at the  $D_s^+$  mass-squared.

The  $MM^{*2}$  distributions for events in the  $D_s^-$  invariant mass signal region ( $\pm 17.5 \text{ MeV}$  from the  $D_s$  mass) are shown in Fig. 2(b). In order to find the number of tags used for further analysis we perform a two-dimensional binned maximum likelihood fit of the  $MM^{*2}$  distribution and the invariant mass distribution in the interval  $\pm 60 \text{ MeV}$  from the  $D_s$  mass and  $3.50 < MM^{*2} < 4.25 \text{ GeV}^2$ . The background has two components, both described by 5th order Chebyshev polynomials; the first comes from the background under the invariant mass peak, defined by

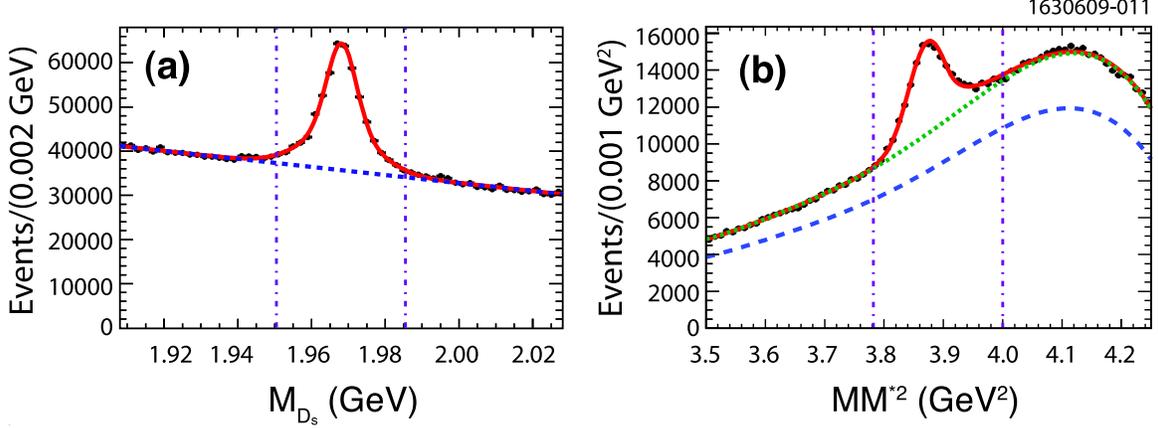


Figure 2: (a) Invariant mass of  $D_s^-$  candidates summed over the decay modes:  $K^+K^-\pi^-$ ,  $K_sK^-$ ,  $\eta\pi^-$ ,  $\eta'\pi^-$ ,  $K^+K^-\pi^-\pi^0$ ,  $\pi^+\pi^-\pi^-$ ,  $K^{*0}K^-$ ,  $\eta\rho^-$ , and fit to a two-Gaussian signal shape plus a linear background. No  $MM^{*2}$  cut has been applied. (b) The  $MM^{*2}$  distribution. The curves show a Crystal Ball function for signal and two 5th order Chebyshev background functions; the dashed curve shows the background from fake  $D_s^-$  tags, while the dotted curve in (b) shows the sum of the backgrounds from multiple photon combinations and fake  $D_s^-$  tags. The vertical dashed lines in (a) and (b) show the region of events selected for further analysis.

the sidebands, and the second is due to multiple photon combinations. In both cases we allow the parameters to float. We find a total of  $43859 \pm 936 \pm 877$  signal events in the interval  $3.782 < MM^{*2} < 4.000 \text{ GeV}^2$  and having an invariant mass within  $\pm 17.5 \text{ MeV}$  of the  $D_s$  mass.

With these tag samples CLEO measured the  $D_s^+ \rightarrow \mu^+\nu$  and  $\tau^+\nu$  final states with  $\tau^+ \rightarrow \pi^+\nu$  and  $\rho^+\nu$ . The  $\tau^+ \rightarrow e^+\nu\bar{\nu}$  was measured using a sub-set of invariant mass tags only. Here the sum of all of the energy deposited in the electromagnetic calorimeter,  $E_{\text{extra}}$ , that is not associated with either the tag or the  $\tau^+$  decay is used as an additional discriminant; for signal events  $E_{\text{extra}}$  should be zero.

The  $\tau^+ \rightarrow \rho^+\nu$  analysis is quite novel. Here some backgrounds peak while the signal shape, that is extremely well known, is rather flat.  $E_{\text{extra}}$  is also used in this analysis. The  $MM^2$  distribution computed from a  $D_s^-$  tag, a photon and a  $\rho^+$  is shown on Fig. 3. A clear excess of signal events is present. A summary of measurements of  $f_{D_s^+}$  by several groups are listed in Table 1.<sup>1</sup>

The decay constant average for  $f_{D_s^+}$  is  $(257.5 \pm 6.1) \text{ MeV}$ . Two unquenched lattice QCD calculations using 3 light fermion loops (unquenched) are available.<sup>7</sup> HPQCD now quotes a value of  $(247 \pm 2) \text{ MeV}$ , a  $2\sigma$  change from their published value of  $(241 \pm 3) \text{ MeV}$ . The updated Fermilab/MILC result is  $(261.4 \pm 7.7 \pm 5.0) \text{ MeV}$ . They also predict  $f_{D_+} = 220.3 \pm 8.0 \pm 4.3) \text{ MeV}$ . Thus these preliminary theoretical results are in agreement with the data.

### 3 Semileptonic Decays

CLEO has observed  $D_s^+ \rightarrow f_0(980)e^+\nu$ ;  $f_0 \rightarrow \pi^+\pi^-$ , measured the form-factor as a function of  $q^2$ , and determined the mass and width of the  $f_0$ , parameters that are not well known.<sup>8</sup> The rate

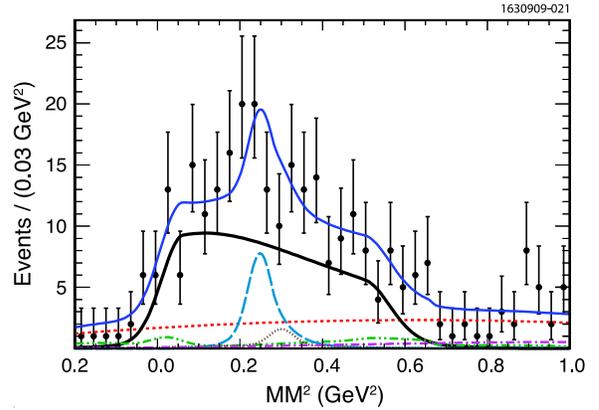


Figure 3: Fit to the data (points) for  $E_{\text{extra}} < 0.1 \text{ GeV}$ . The various components are signal (thick solid line),  $\eta\rho^+$  (dotted), fake  $D_s^-$  (dashed),  $K^0\pi^+\pi^0$  (long dash), sum of  $\pi^+\pi^0\pi^0$ ,  $\eta\pi^+$ ,  $\phi\pi^+$ ,  $\tau^+ \rightarrow (\pi^+ + \pi^+\pi^0\pi^0)\bar{\nu}$ ,  $\mu^+\nu$ , and  $X\mu^+\nu$  (dash-dot-dot), and other backgrounds (dashed-dot). The thinner solid curve shows the total.

Table 1: Experimental results for  $\mathcal{B}(D_s^+ \rightarrow \mu^+\nu)$ ,  $\mathcal{B}(D_s^+ \rightarrow \tau^+\nu)$ , and  $f_{D_s^+}$ .

Experiment	Mode	$\mathcal{B}$	$f_{D_s^+}$ (MeV)
CLEO-c <sup>2</sup>	$\mu^+\nu$	$(5.65 \pm 0.45 \pm 0.17) \times 10^{-3}$	$257.6 \pm 10.3 \pm 4.3$
Belle <sup>3</sup>	$\mu^+\nu$	$(6.38 \pm 0.76 \pm 0.57) \times 10^{-3}$	$274 \pm 16 \pm 12$
Average	$\mu^+\nu$	$(5.80 \pm 0.43) \times 10^{-3}$	$261.5 \pm 9.7$
CLEO-c <sup>2</sup>	$\tau^+\nu (\pi^+\bar{\nu})$	$(6.42 \pm 0.81 \pm 0.18) \times 10^{-2}$	$278.0 \pm 17.5 \pm 3.8$
CLEO-c <sup>4</sup>	$\tau^+\nu (\rho^+\bar{\nu})$	$(5.52 \pm 0.57 \pm 0.21) \times 10^{-2}$	$257.8 \pm 13.3 \pm 5.2$
CLEO-c <sup>5</sup>	$\tau^+\nu (e^+\nu\bar{\nu})$	$(5.30 \pm 0.47 \pm 0.22) \times 10^{-2}$	$252.6 \pm 11.2 \pm 5.6$
BaBar <sup>6</sup>	$\tau^+\nu (e^+\nu\bar{\nu})$	$(4.54 \pm 0.53 \pm 0.40 \pm 0.28) \times 10^{-2}$	$233.8 \pm 13.7 \pm 12.6$
Average	$\tau^+\nu$	$(5.58 \pm 0.35) \times 10^{-2}$	$255.5 \pm 7.5$
Average	$\mu^+\nu + \tau^+\nu$		$257.5 \pm 6.1$

and form-factor for  $D_s^+ \rightarrow \phi e^+\nu$  was also measured. The ratio of these two rates at  $q^2$  of zero was predicted<sup>9</sup> to be similar to that of  $\Gamma(B_s \rightarrow J/\psi f_0) / \Gamma(B_s \rightarrow J/\psi \phi)$ .

Figure 4 shows the  $q^2$  distributions. The  $\phi e^+\nu$  channel is fit using the form factors determined by the BaBar collaboration letting the normalization float.<sup>10</sup> For  $f_0 e^+\nu$  a simple pole model is used:  $|f_+(q^2)| = 1/(1 - q^2/M_{\text{pole}}^2)$ , resulting in  $M_{\text{pole}} = (1.7_{-0.7}^{+4.5} \pm 0.2)$  GeV. Using the fits we find that at  $q^2$  of zero the  $f_0/\phi$  yield is  $(42 \pm 011)\%$ .

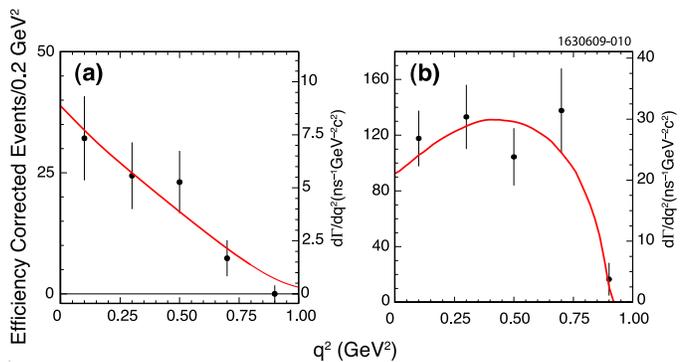


Figure 4: The  $q^2$  distributions for (a)  $D_s^+ \rightarrow f_0 e^+\nu$  (b)  $D_s^+ \rightarrow \phi e^+\nu$ . The fits are described in the text.

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