



# Measurement of the strong coupling $\alpha_s$ from the 3-jet rate in $e^+e^-$ annihilation using JADE data

XLVII<sup>th</sup> Rencontres de Moriond: QCD and High Energy Interactions  
La Thuile, 15.03.12

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the JADE Collaboration



# Introduction

- Why study 26+ year old  $e^+e^-$  data?
  - Theory improvements: NLO >3 jets, NNLO, ...
  - MC generators and hadronisation models
- Test QCD calculations for LHC
  - Techniques related, crossing relations
  - Precision tests independent of pp complications
- Because we can!



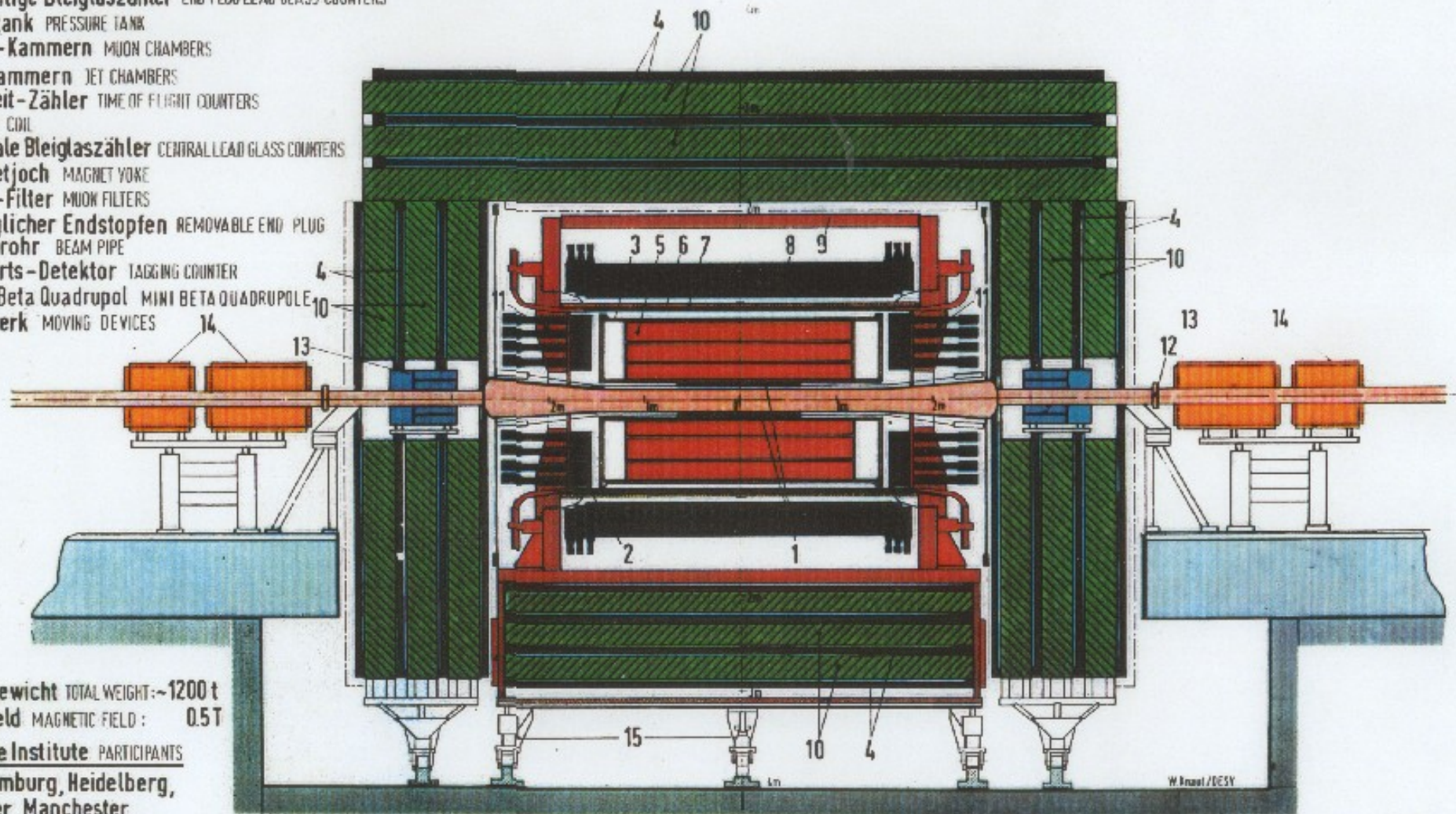
# The JADE experiment

1979 to 1986 at PETRA (DESY)

$\sqrt{s} = 14, 22, 34.6, 35, 38.3, 43.8 \text{ GeV}$

**MAGNETDETEKTOR JADE**  
MAGNET DETECTOR

- 1 Strahlrohrzähler BEAM PIPE COUNTERS
- 2 Endseitige Bleiglaszähler END PLUG LEAD GLASS COUNTERS
- 3 Drucktank PRESSURE TANK
- 4 Myon-Kammern MUON CHAMBERS
- 5 Jet-Kammern JET CHAMBERS
- 6 Flugzeit-Zähler TIME OF FLIGHT COUNTERS
- 7 Spule COIL
- 8 Zentrale Bleiglaszähler CENTRAL LEAD GLASS COUNTERS
- 9 Magnetjoch MAGNET YOKE
- 10 Myon-Filter MUON FILTERS
- 11 Beweglicher Endstopfen REMOVABLE END PLUG
- 12 Strahlrohr BEAM PIPE
- 13 Vorwärts-Detektor TAGGING COUNTER
- 14 Mini-Beta Quadrupol MINI BETA QUADRUPOLE
- 15 Fahrwerk MOVING DEVICES



Gesamtgewicht TOTAL WEIGHT: ~1200 t  
Magnetfeld MAGNETIC FIELD: 0.5T

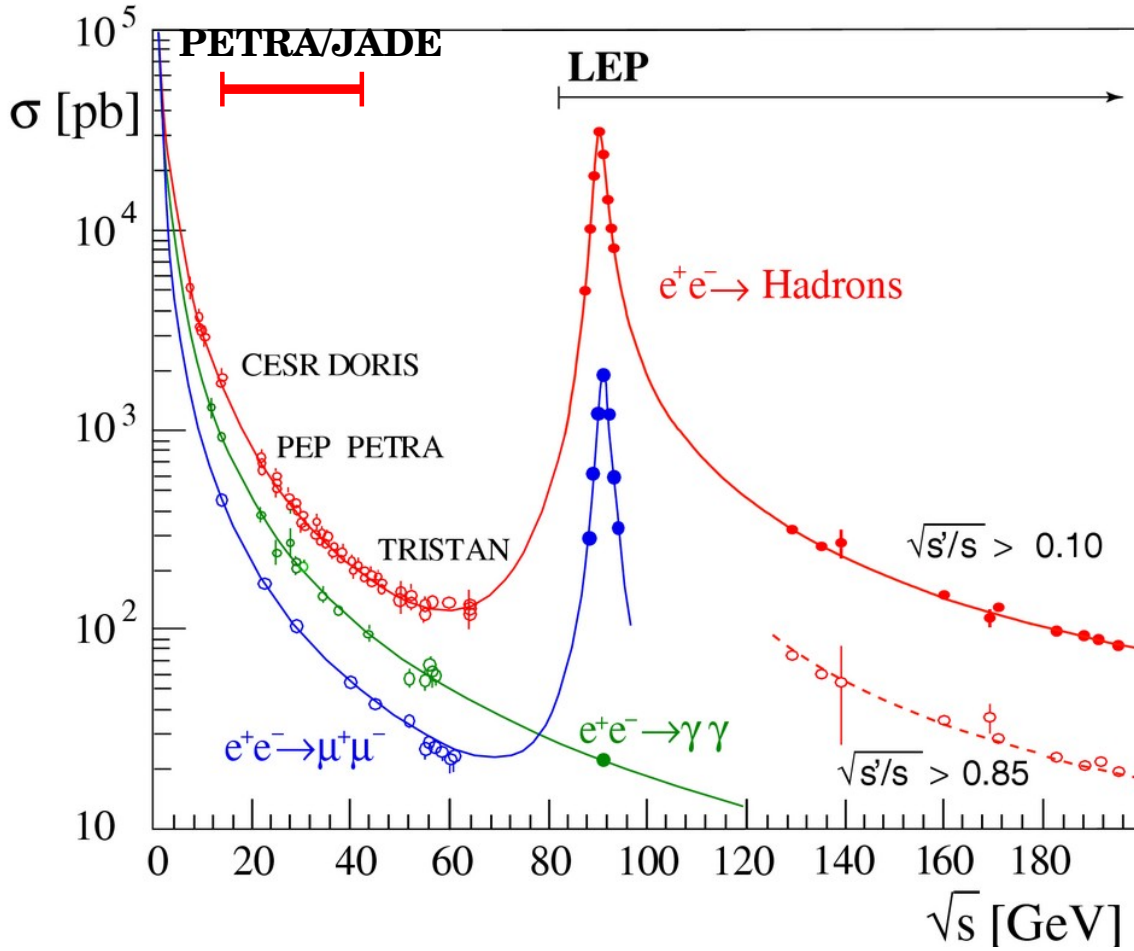
Beteiligte Institute PARTICIPANTS  
DESY, Hamburg, Heidelberg,  
Lancaster, Manchester,  
Rutherford Lab., Tokio

W. Brandl / DESY

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# JADE data



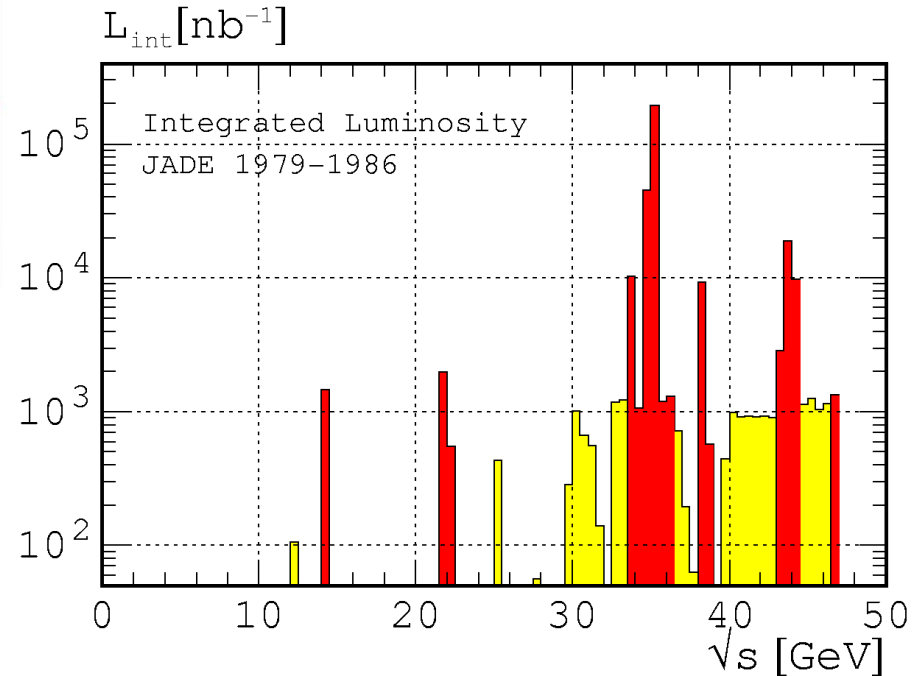
Data samples:

$O(10^3 - 10^4)$  events

Negligible backgrounds after selection

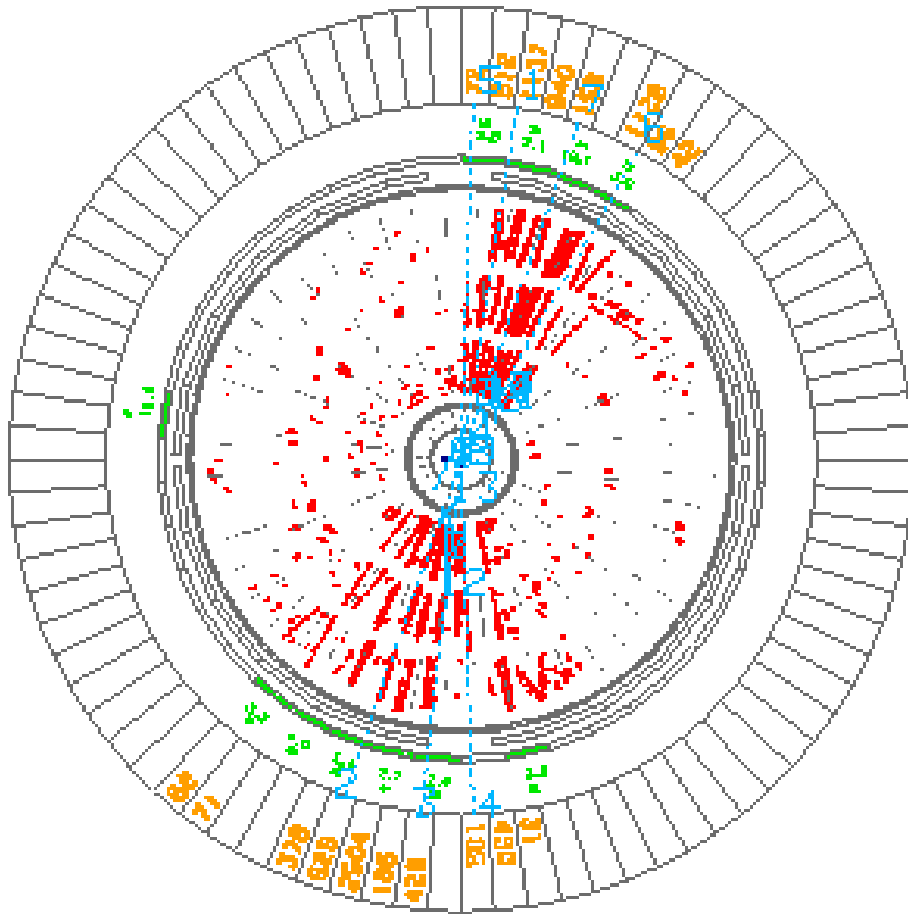
Event selection:  
momentum balance, visible energy,

$N_{ch.}$



# Durham jet clustering algorithm

JADE  $\sqrt{s} = 44 \text{ GeV}$



1) Phase space distances

$$y_{ij} = 2 \min(E_i, E_j)^2 (1 - \cos \theta_{ij}) / s$$

2) Stop when all  $y_{ij} > y_{\text{cut}}$

3) Combine pair with smallest  $y_{ij}$

$$\mathbf{p}_{ij} = \mathbf{p}_i + \mathbf{p}_j$$

4) Remove i and j, add ij, goto 1)

Observable:  $R_3(y_{\text{cut}}, Q) = N_{3\text{-jet}}(y_{\text{cut}}, Q) / N(Q) = \sigma_{3\text{-jet}} / \sigma_{\text{had}}$

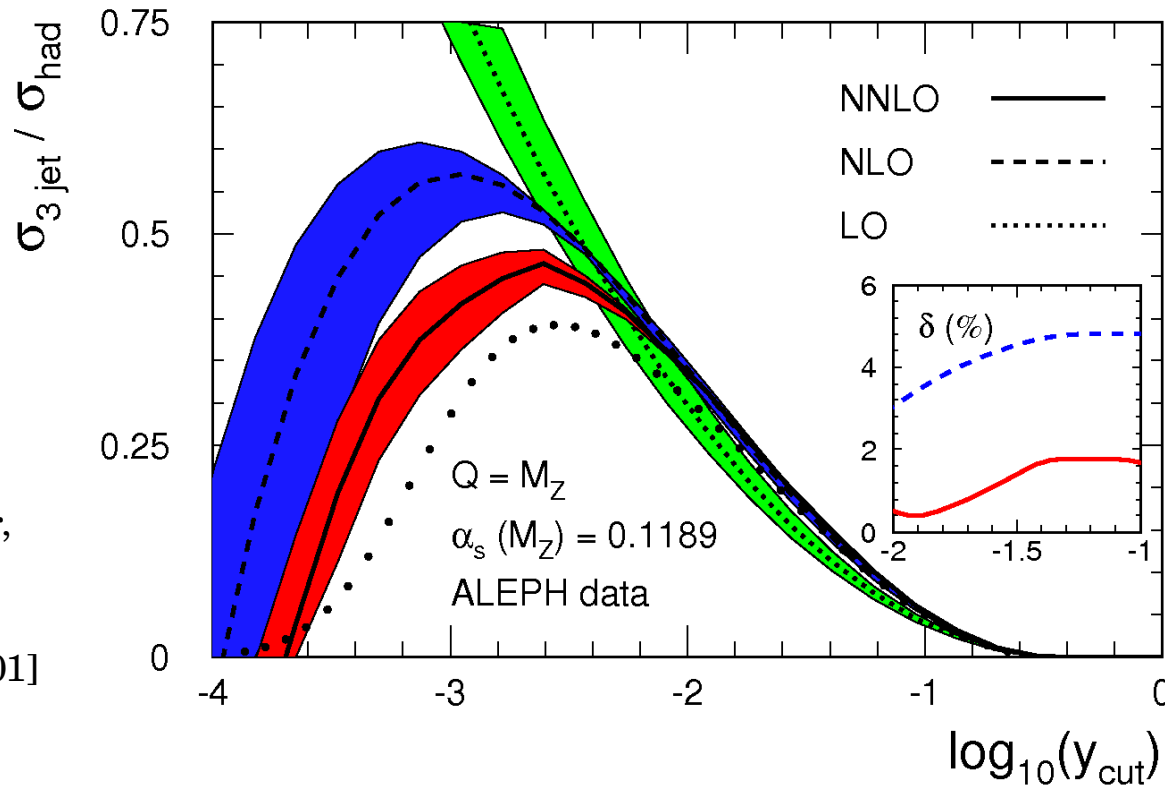


# QCD predictions: fixed order

$$R_{3,\text{NNLO}}(y_{\text{cut}}, Q) = \sigma_{3\text{-jet}} / \sigma_0 = A(y_{\text{cut}}) \underline{\alpha}_S(Q) + B(y_{\text{cut}}) \underline{\alpha}_S^2(Q) + C(y_{\text{cut}}) \underline{\alpha}_S^3(Q)$$

$$\underline{\alpha}_S = \alpha_S / (2\pi); \sigma_0 = \sigma_{\text{had}} / (1 + 2\underline{\alpha}_S + \dots)$$

$A(y_{\text{cut}})$ ,  $B(y_{\text{cut}})$ ,  $C(y_{\text{cut}})$  by numerical integration of QCD ME



Insert: rel. theory uncertainties NLO and NNLO

[Gehrmann-de Ridder, Gehrmann, Glover, Heinrich: Phys. Rev. Lett. 100 (2008) 172001]

# QCD predictions: resummation

E.g.  $\alpha_s \log^2(1/0.01) \approx 0.4$

→  $R_{3,NLLA}$  large for small  $y_{cut}$

Expand known  $R_{3,NLLA}$  to  $O(\alpha_s^3)$ :

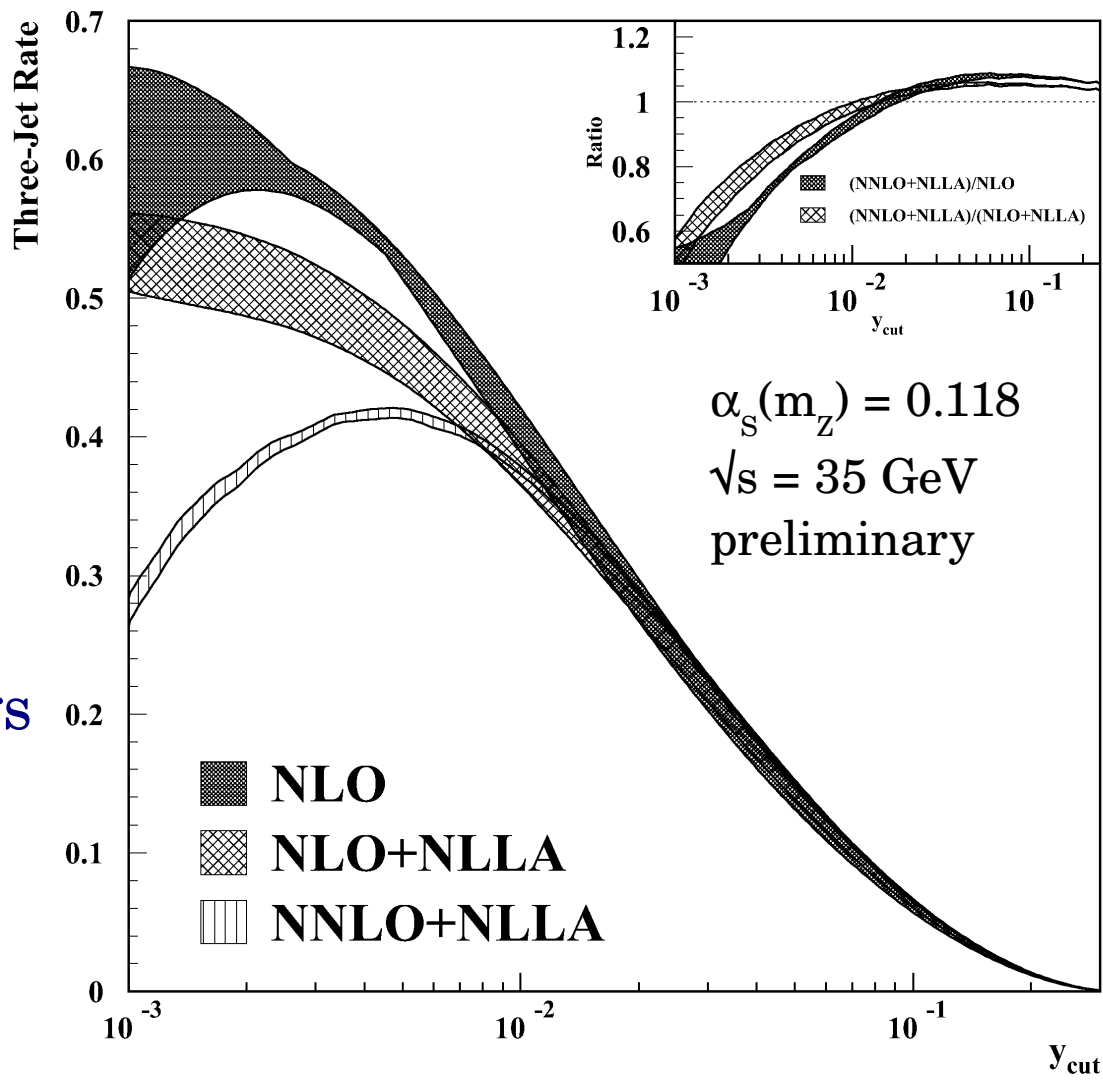
$$L = \log(1/y_{cut})$$

$$R_{3,NLLA,exp.} = \sum_{i=1}^3 \sum_{j=i}^{2i} \alpha_s^i L^j R_{ij}$$

“K-term”: partial subleading logs

R-matching:

$$R_3 = R_{3,NNLO} + R_{3,NNLA} - R_{3,NLLA,exp.}$$



# Data vs MC

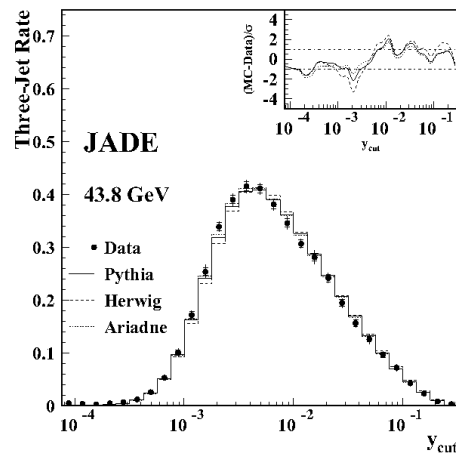
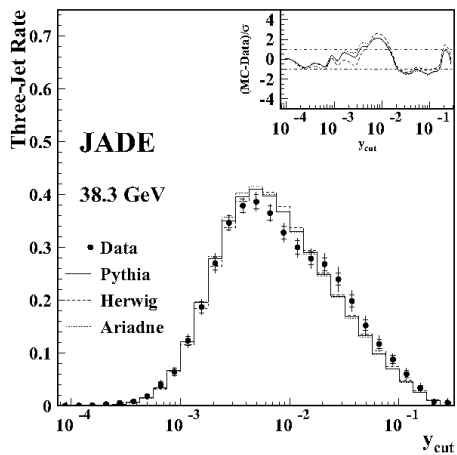
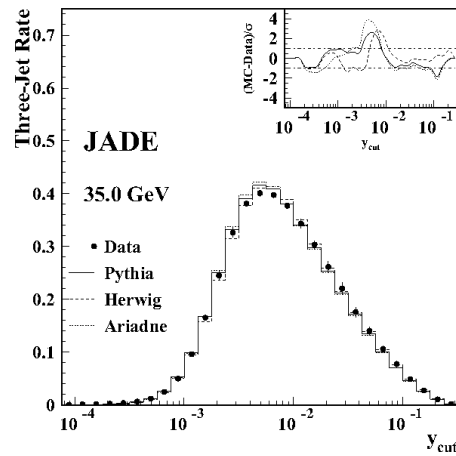
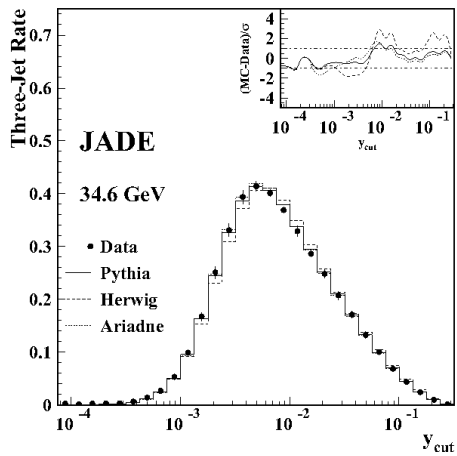
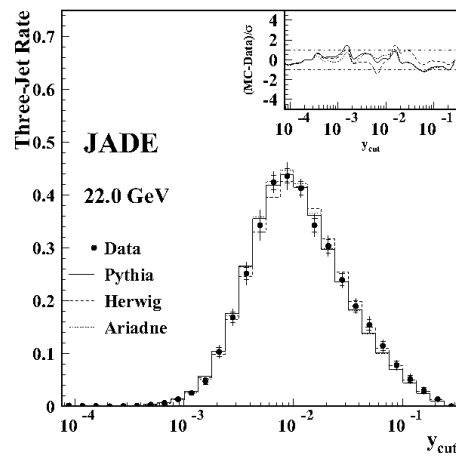
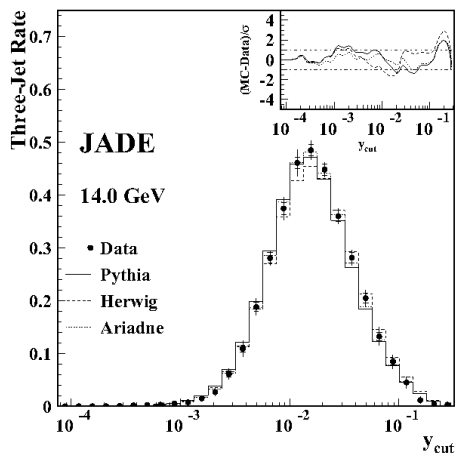
Data corrected to hadron-level,  
 $b\bar{b}$  contribution subtracted

PYTHIA 5.7, HERWIG 6.2,  
 ARIADNE 4.11

LL+LO, tuned to OPAL@LEP 1

Good description of low energy  
 data with OPAL tune

MCs ok for experimental  
 and hadronisation corrections



preliminary



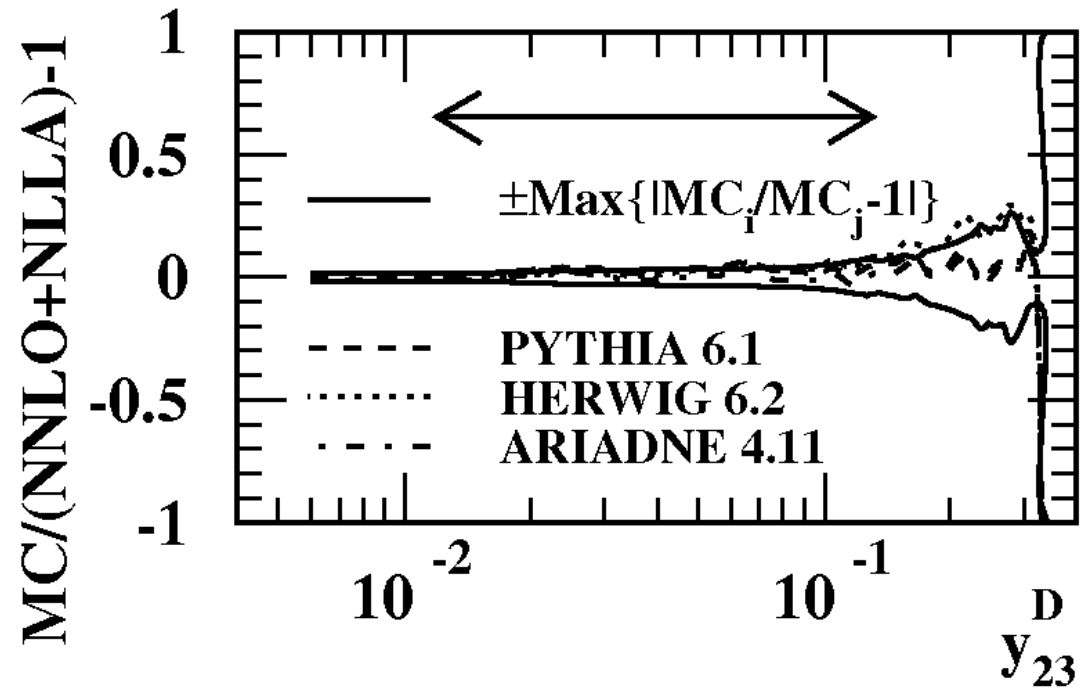


# Hadronisation corrections

Compare MC parton-level (after parton shower) to hadron-level (particle level)

Check consistency MC LO+LL parton-level with theory

NNLO+NLLA parton-level by OPAL:



Consistent within differences between MCs, covered by hadronisation correction systematic uncertainty

[OPAL: Eur. Phys. J. C71 (2011) 1733]

# R<sub>3</sub> fits

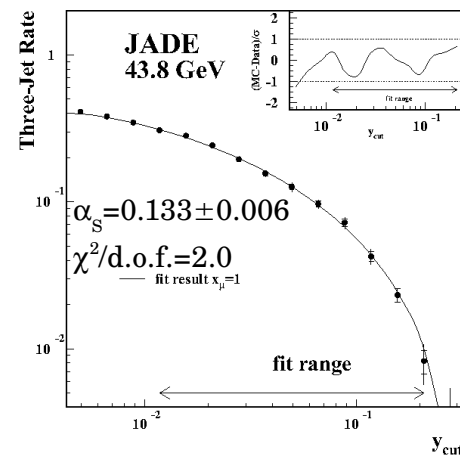
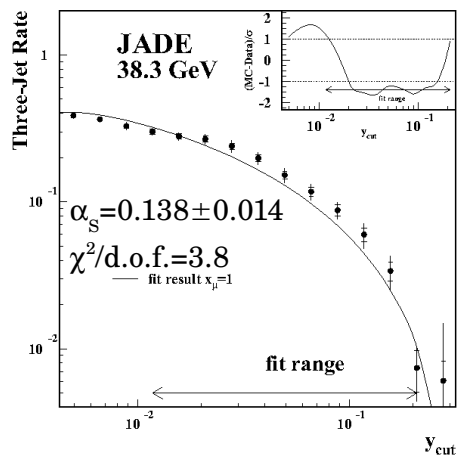
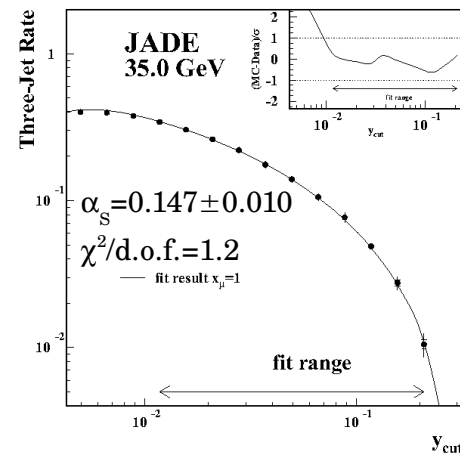
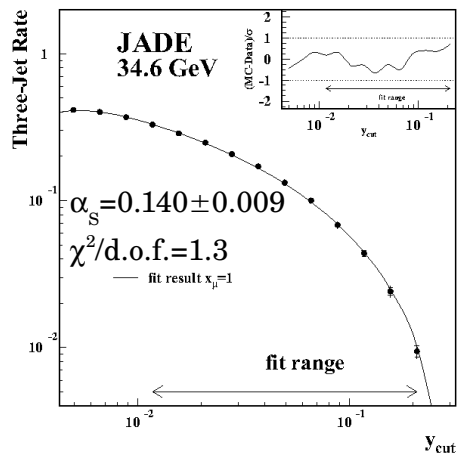
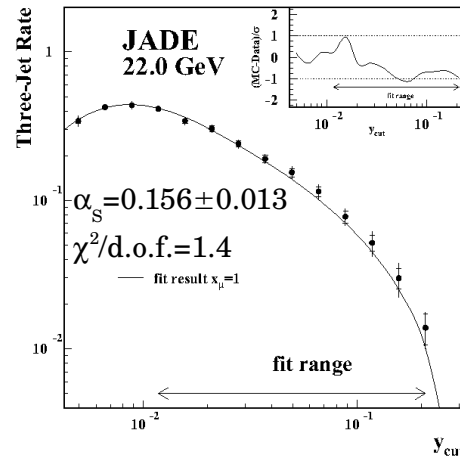
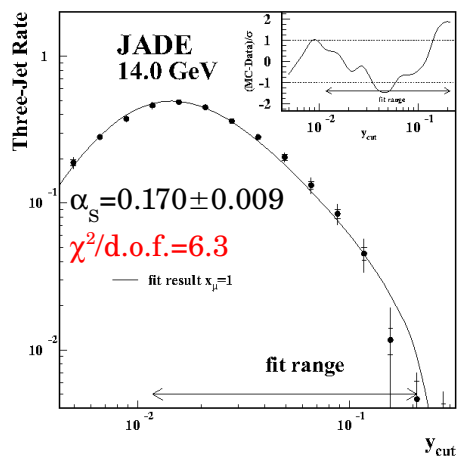
## NNLO+NLLA

Fit ranges: exp. and had. corrections stable and “small”

Incl. point-to-point correlations,  $\chi^2$  from stat. errors only,  $1.3 < \chi^2/\text{d.o.f.} < 3.8$  (except 14 GeV)

Combine results 22 to 44 GeV:

$$\alpha_S(m_Z) = 0.1199 \pm 0.0010_{\text{stat.}} \pm 0.0021_{\text{exp.}} \pm 0.0054_{\text{had.}} \pm 0.0007_{\text{theo.}}$$



preliminary



# Systematics

- **Experimental**
  - Vary event selection cuts
  - Tracks + ECAL clusters vs “energy flow”
  - PYTHIA vs HERWIG exp. corrections
  - JADE detector calibration versions
  - Vary  $b\bar{b}$  subtraction
  - Vary fit range
- **Hadronisation**
  - PYTHIA vs HERWIG vs ARIADNE
- **Theory**
  - Renormalisation scale factor  $0.5 < x_{\mu} < 2.0$



# Cross checks

Renormalisation scale:

Fit with  $x_\mu$  free:  $x_\mu = O(1)$

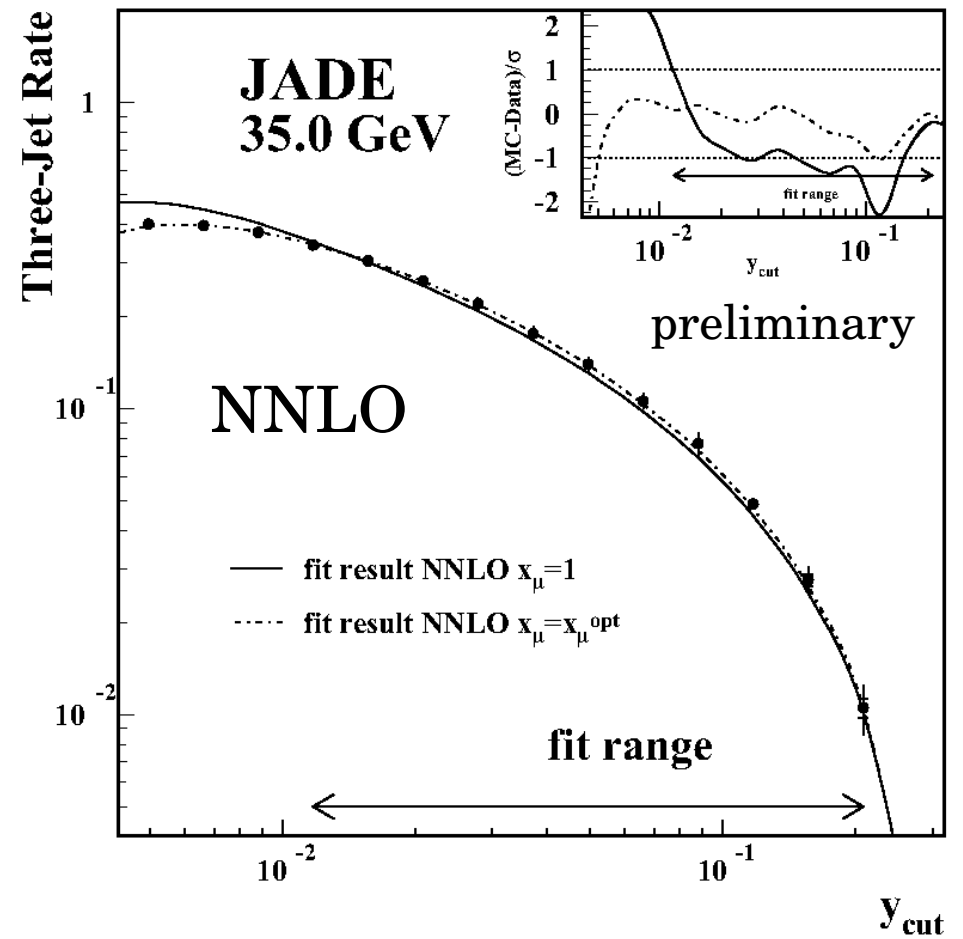
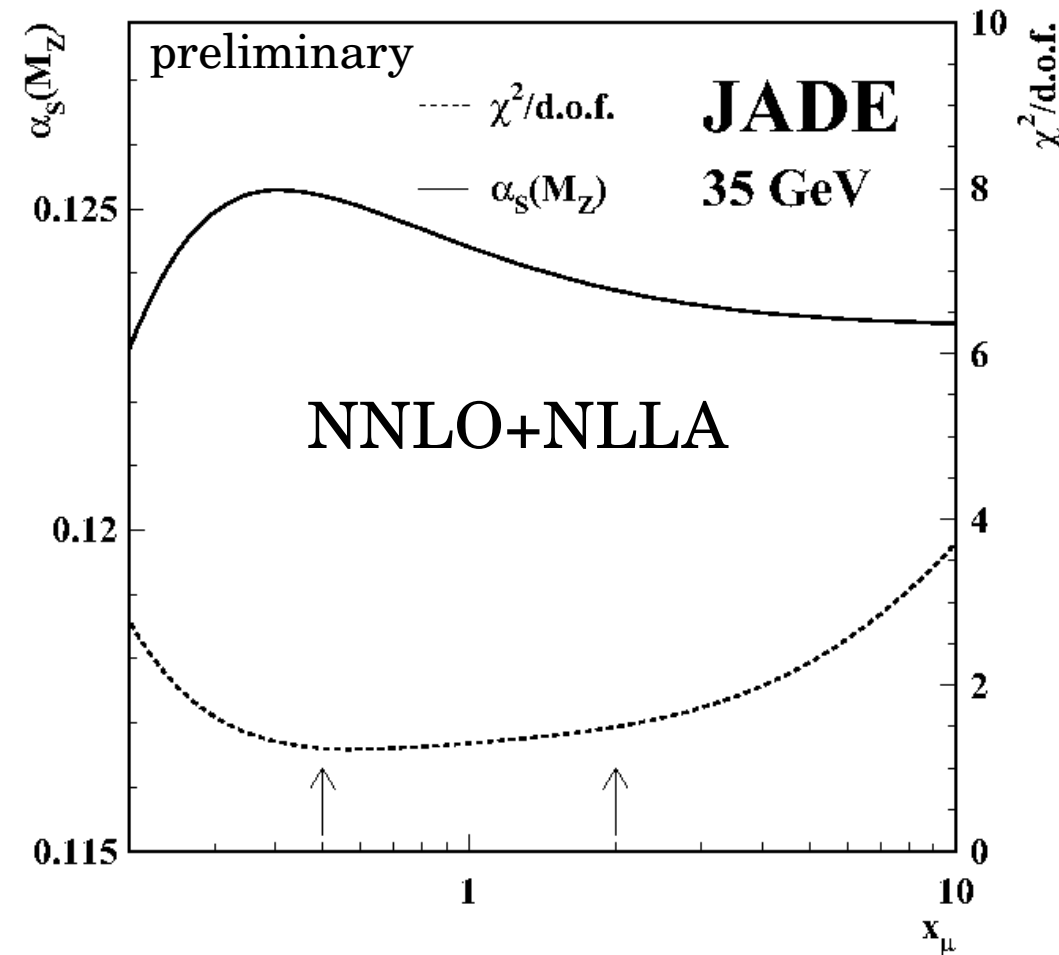
Essentially same result for  $\alpha_s(m_Z)$

NNLO only fit:

Slope not fully described

Sensitive to fit range

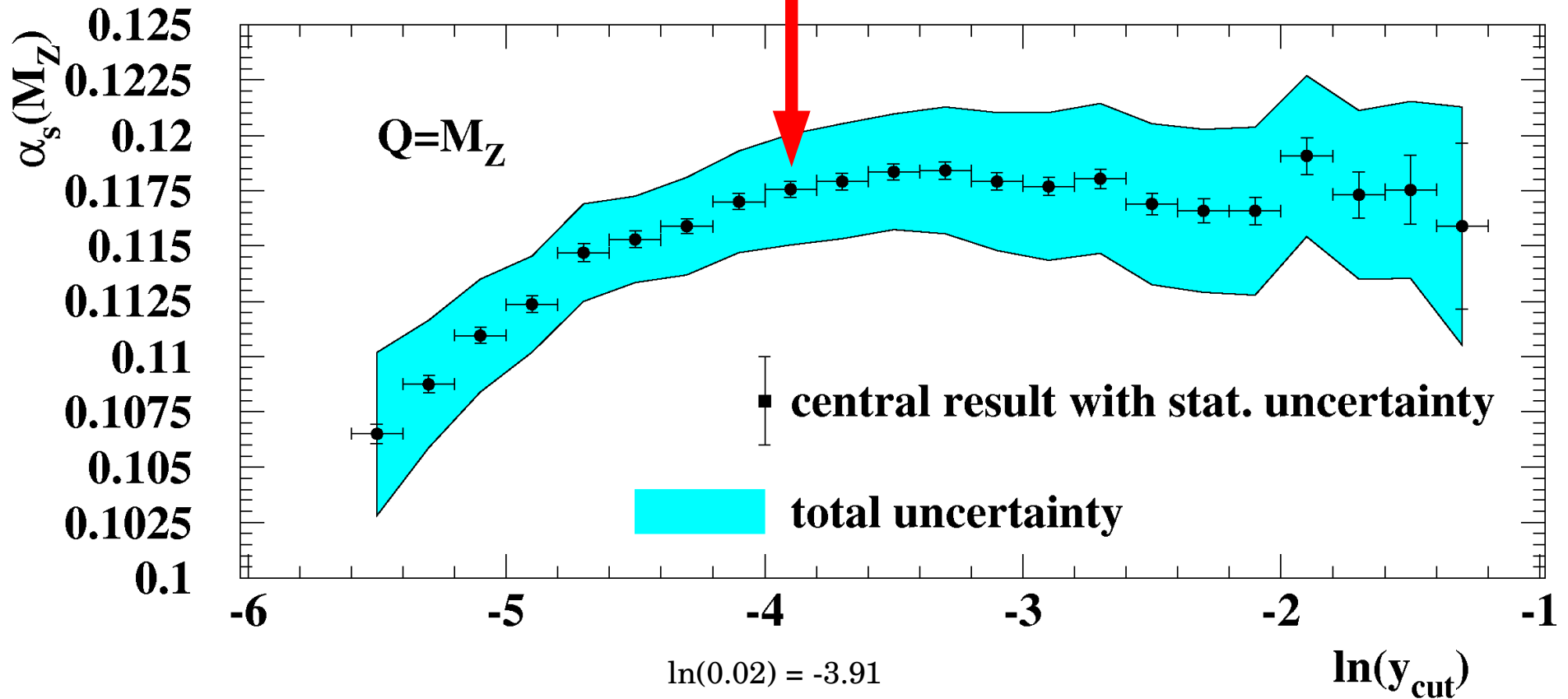
Scale uncertainty larger





# DG<sup>3</sup>HS/ALEPH Result

NNLO only, result at single point  $y_{cut} = 0.02$



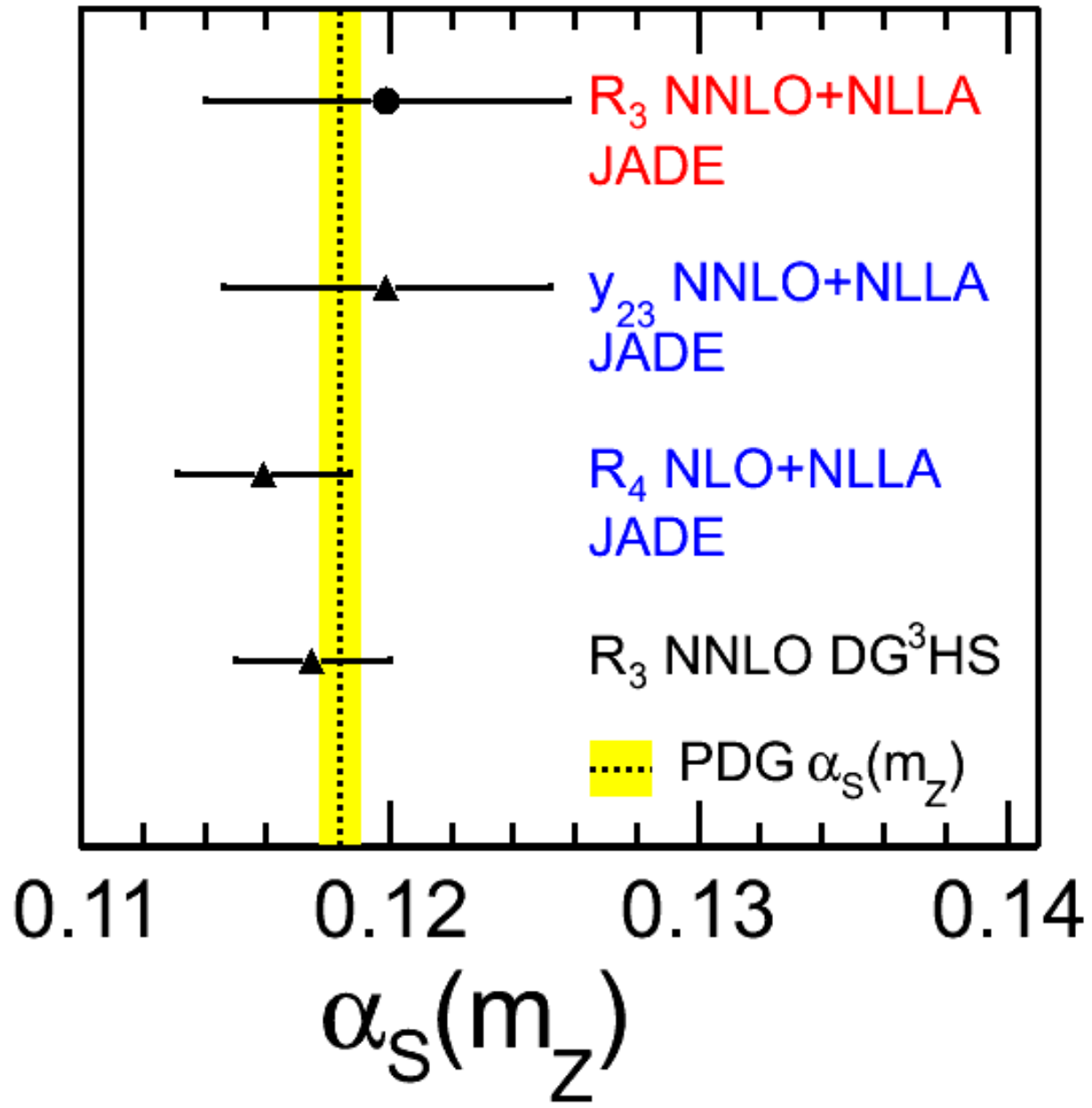
$$\alpha_s(m_Z) = 0.1175 \pm 0.0004_{stat.} \pm 0.0019_{exp.} \pm 0.0006_{had.} \pm 0.0014_{theo.}$$

Slope problem visible

[Dissertori et al.: Phys. Rev. Lett. 104 (2010) 072002]



# Comparison to previous results

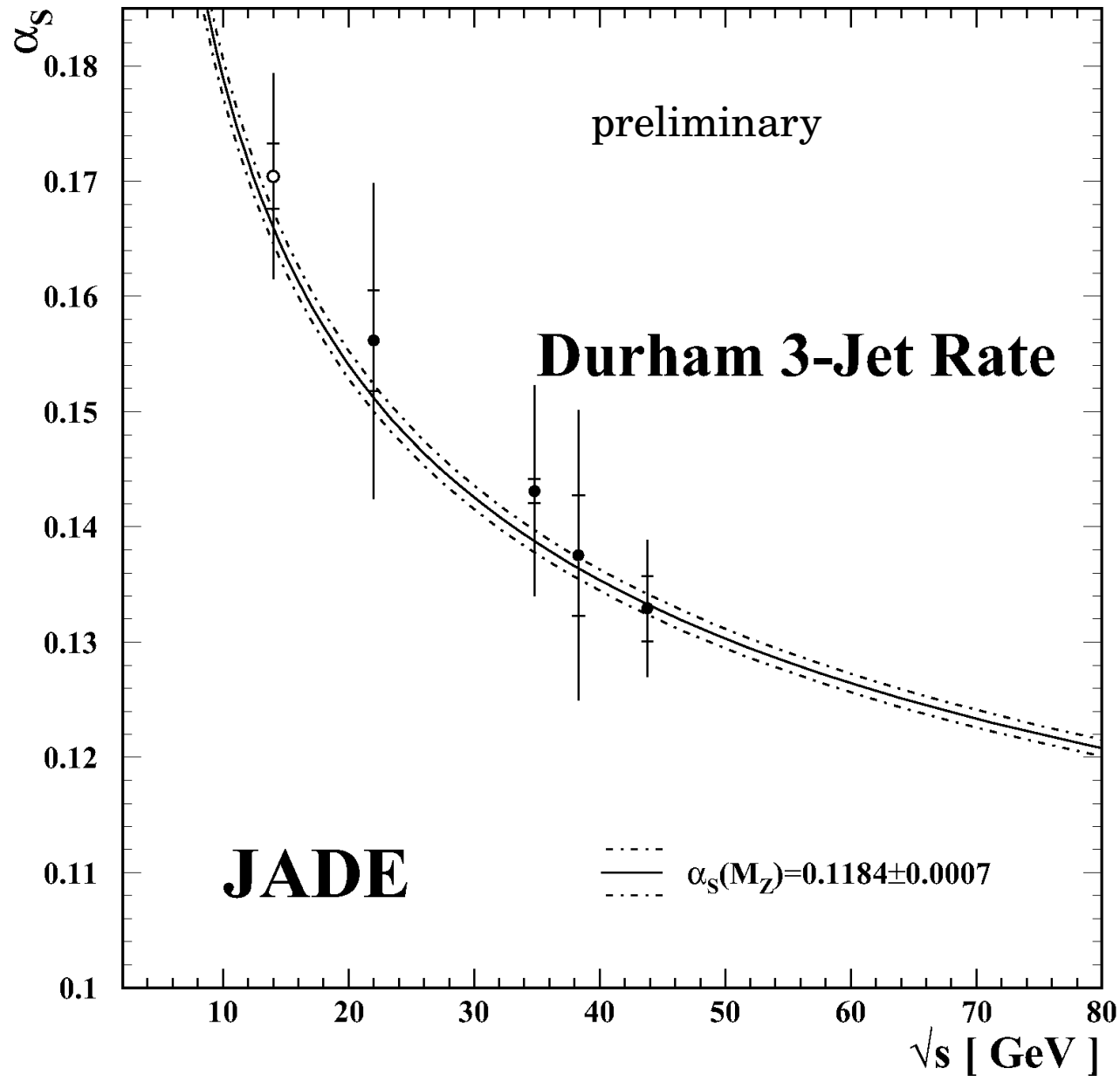


Result consistent with:

- previous JADE
- DG<sup>3</sup>HS/ALEPH
- PDG



# Running coupling



Confirm QCD running coupling prediction

14 GeV analysis (not in average) still consistent

Prediction using PDG world average



# Summary

- First  $\alpha_s$  from  $R_3$  with NNLO+NLLA QCD
  - $\alpha_s(m_Z) = 0.1199 \pm 0.0010_{\text{stat.}} \pm 0.0021_{\text{exp.}} \pm 0.0054_{\text{had.}} \pm 0.0007_{\text{theo.}}$
- Slope of  $R_3(y_{\text{cut}})$  not fully described in NNLO
  - Ok within errors with NNLO+NLLA
- Had. uncertainties dominate
  - LEP data
  - Better had. models (power corrections)?
- More new results from old data possible!