

# Direct $CP$ violation in $D$ meson decays

Joachim Brod

in collaboration with Yuval Grossman, Alexander L. Kagan, Jure Zupan

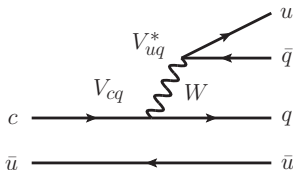


Recontres de Moriond, QCD session  
March 13th, 2012

[arXiv:1111.5000 \[hep-ph\]](https://arxiv.org/abs/1111.5000); [arXiv:1203.xxxx \[hep-ph\]](https://arxiv.org/abs/1203.xxxx)  
see also A. Kagan, talk at FPCP 2011, May 2011

# Introduction

Singly Cabibbo-suppressed (SCS)  $D$ -meson decays  $D^0 \rightarrow \pi^+ \pi^-$ ,  $D^0 \rightarrow K^+ K^-$



$CP$  violation in SCS  $D$ -meson decays is

- sensitive to new physics (NP) in the up-quark sector
- suppressed in the standard model (SM):
  - two-generation dominance
  - loop suppression (penguin amplitudes)
  - GIM mechanism

Naively, expect effects of  $\mathcal{O}\left(\frac{V_{ub}V_{cb}}{V_{us}V_{cs}}\frac{\alpha_s}{\pi}\right) \sim 0.01\%$ .

# Definitions

$$A_f \equiv A(D^0 \rightarrow f) = A_f^T [1 + r_f e^{i(\delta_f - \phi_f)}],$$
$$\bar{A}_f \equiv A(\bar{D}^0 \rightarrow f) = A_f^T [1 + r_f e^{i(\delta_f + \phi_f)}]$$

$r_f$  relative magnitude of subleading (penguin) amplitude with relative strong phase  $\delta_f$ , weak phase  $\phi_f$ .

$$\mathcal{A}_f^{\text{dir}} := \frac{|A_f|^2 - |\bar{A}_f|^2}{|A_f|^2 + |\bar{A}_f|^2} = 2r_f \sin \phi_f \sin \delta_f$$

(Universal) indirect contribution  $\mathcal{A}_f^{\text{ind}}$  cancels to good approximation in

$$\Delta \mathcal{A}_{CP} := \mathcal{A}_{K^+K^-}^{\text{dir}} - \mathcal{A}_{\pi^+\pi^-}^{\text{dir}}$$

# Measurements

First significant measurements of  $CP$  violation in the up-quark sector

LHCb [R. Aaij et al., 1112.0938]:

$$\Delta\mathcal{A}_{CP} = (-0.82 \pm 0.21 \pm 0.11)\%$$

CDF [La Thuile 2012]:

$$\Delta\mathcal{A}_{CP} = (-0.62 \pm 0.21 \pm 0.10)\%$$

leading to new world average [La Thuile 2012]:

$$\Delta\mathcal{A}_{CP} = (-0.67 \pm 0.16)\%$$

- Can it be standard model (SM)?
- Can it be new physics (NP)?
- Can we distinguish NP from SM?

# So, can it be SM?

“There one typically finds asymmetries  $\sim \mathcal{O}(10^{-4})$ , i.e. somewhat smaller than the rough benchmark stated above. Yet  $10^{-3}$  effects are conceivable, and even 1% effects cannot be ruled out completely.”

[D. Benson et al., hep-ex/0309021]

“This would lead to gigantic CP violations, an asymmetry of order 1. This is of course very unlikely [...]”

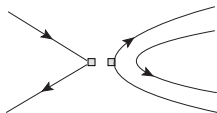
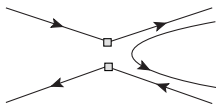
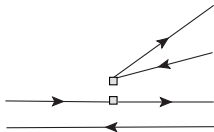
[M. Golden, B. Grinstein, Phys. Lett. B 222]

Can we be more specific?

# SM weak effective Hamiltonian

Integrate out  $M_W$ ,  $m_b$ , evolve down to charm scale  $\mu_c$ , use GIM:

$$H_{\text{eff}}^{\text{SCS}} = \frac{G_F}{\sqrt{2}} \left\{ V_{cs} V_{us}^* \sum_{i=1,2} C_i \left( Q_i^{\bar{s}s} - Q_i^{\bar{d}d} \right) - V_{cb} V_{ub}^* \sum_{i=3}^6 C_i Q_i + C_{8g} Q_{8g} \right\} + \text{h.c.}$$



- Wilson coefficients: perturbative
- Matrix elements: leading power and power corrections in  $1/m_c$
- Estimate tree amplitude  $A^T$  from data
- Relate penguin amplitude  $A^P$  to  $A^T$

## $P/T$ at leading power

Leading power (“Naive factorization” +  $\mathcal{O}(\alpha_s)$  corrections):

$$r_f^{\text{LP}} = \left| \frac{A_f^P(\text{leading power})}{A_f^T(\text{experiment})} \right|$$

$$r_{K^+K^-}^{\text{LP}} \approx (0.01 - 0.02)\%, \quad r_{\pi^+\pi^-}^{\text{LP}} \approx (0.015 - 0.03)\%$$

Expect sign( $\mathcal{A}_{K^+K^-}^{\text{dir}}$ ) =  $-\text{sign}(\mathcal{A}_{\pi^+\pi^-}^{\text{dir}})$  (if  $SU(3)_F$  breaking is not too large).  
Cf. global averages [HFAG]

$$\mathcal{A}_{K^+K^-} = (-0.23 \pm 0.17)\%, \quad \mathcal{A}_{\pi^+\pi^-} = (0.20 \pm 0.22)\%$$

For  $\phi_f = \gamma \approx 67^\circ$  and  $\mathcal{O}(1)$  strong phases

$$\Delta\mathcal{A}_{CP}(\text{leading power}) \sim 4r_f = \mathcal{O}(0.1\%).$$

Order of magnitude below measurement!

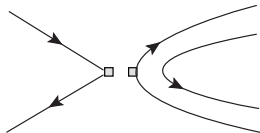
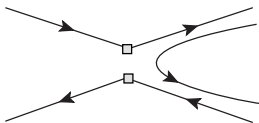
# SM: Large penguin power corrections

From  $SU(3)_F$  fits [Cheng, Chiang, 1001.0987, 1201.0785; Bhattacharya, Gronau, Rosner, 1201.2351; Pirtskhalava, Uttayarat, 1112.5451] we know

$$\mathcal{O}(1) = T_f \sim E_f = \mathcal{O}(1/m_c)$$

Signals breakdown of  $1/m_c$  expansion

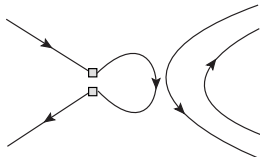
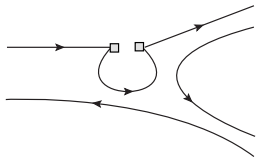
**Power corrections:** look at two specific contributions - insertions of  $Q_4$ ,  $Q_6$





# SM: Large penguin power corrections

Associated penguin contractions of  $Q_1$  cancel scheme and scale dependence



- Single hard gluon exchange leads to “effective Wilson coefficients”  $C_4^{\text{eff}}$  and  $C_6^{\text{eff}}$  depending on the gluon virtuality  $q^2$ .

Setting  $A^T(\text{exp}) = E_f$  in

$$r_f^{\text{PC}} = \left| \frac{A_f^P(\text{power correction})}{A_f^T(\text{experiment})} \right|$$

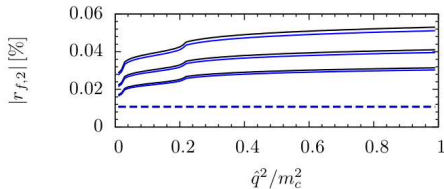
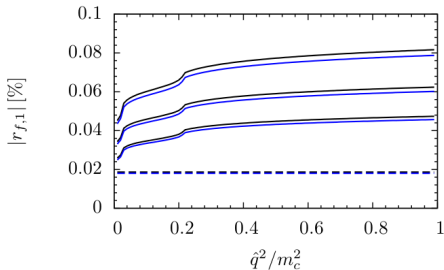
and  $N_c$  counting leads to

$$r_{f,1} \sim 2N_c |V_{cb} V_{ub} C_6^{\text{eff}}| / (C_1 \sin \theta_c),$$

$$r_{f,2} \sim 2|V_{cb} V_{ub} (C_4^{\text{eff}} + C_6^{\text{eff}})| / (C_1 \sin \theta_c).$$

# SM: Large penguin power corrections

$r_{\pi^+\pi^-,i}$  (black) and  $r_{K^+K^-,i}$  (blue) for  $\mu = 1 \text{ GeV}$ ,  $m_c, m_D$



$$\Delta\mathcal{A}_{CP}(P_{f,1}) = \mathcal{O}(0.3\%), \quad \Delta\mathcal{A}_{CP}(P_{f,2}) = \mathcal{O}(0.2\%)$$

$\Rightarrow$  a SM explanation is plausible.

# Uncertainties

- Extraction of annihilation amplitudes  $E_f$  from data
- Neglected contributions to  $E_f$
- $N_c$  counting
- modeling of penguin contraction matrix elements
- Neglected additional penguin contractions

Cumulative uncertainty of a factor of a few; much larger effects are unlikely.

Can we trust it?

## SM: Consistent picture

Another observation: from  $\text{Br}(D^0 \rightarrow K^+ K^-) \approx 2.8 \times \text{Br}(D^0 \rightarrow \pi^+ \pi^-)$

$$|A(D^0 \rightarrow K^+ K^-)| = 1.8 \times |A(D^0 \rightarrow \pi^+ \pi^-)|$$

- Should be the same in  $SU(3)_F$  limit
- Usually interpreted as a sign of large  $\mathcal{O}(1)$   $SU(3)_F$  breaking

But note that

$$|A(D^0 \rightarrow K^- \pi^+)| = 1.15 \times |A(D^0 \rightarrow K^+ \pi^-)|$$

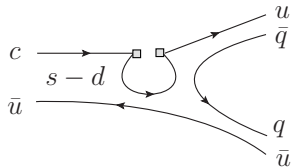
for Cabibbo-favored (CF) decay  $D^0 \rightarrow K^- \pi^+$  and doubly Cabibbo-suppressed (DCS) decay  $D^0 \rightarrow K^+ \pi^-$ .

$$H_{\text{eff}}^{\text{CF}} = \frac{G_F}{\sqrt{2}} V_{cs} V_{ud}^* \sum_{i=1,2} C_i Q_i^{\bar{d}s} + \text{h.c.}$$

# Weak Hamiltonian, written differently

$$T_{KK} = T_{KK}^s + P_{KK}^{T,s} - P_{KK}^{T,d}$$

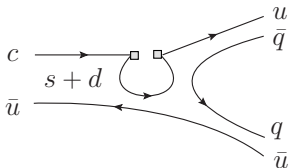
$$T_{\pi\pi} = -T_{\pi\pi}^d + P_{\pi\pi}^{T,s} - P_{\pi\pi}^{T,d}$$



- Broken penguin  $P_{\text{break}}$  violates  $U$  spin ( $s \leftrightarrow d$ )

$$H_{\text{eff}}^{\text{SCS}} = \frac{G_F}{\sqrt{2}} \left\{ (V_{cs} V_{us}^* - V_{cd} V_{ud}^*) \sum_{i=1,2} C_i (Q_i^{\bar{s}s} - Q_i^{\bar{d}d}) / 2 \right.$$

$$\left. - V_{cb} V_{ub}^* \left[ \sum_{i=1,2} C_i (Q_i^{\bar{s}s} + Q_i^{\bar{d}d}) / 2 + \sum_{i=3}^6 C_i Q_i + C_{8g} Q_{8g} \right] \right\} + \text{h.c.}$$



- Penguin  $P$  violates  $CP$

# $U$ -spin decomposition

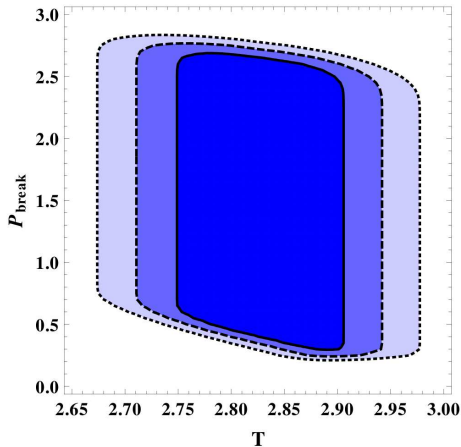
- $D^0 \rightarrow K^- \pi^+, K^+ K^-, \pi^+ \pi^-, K^+ \pi^-$
- Assume nominal  $U$ -spin breaking  $\propto \epsilon_U \sim 0.2 - 0.3$
- **Additional assumption:**  $T = \mathcal{O}(1)$ ,  $P = \mathcal{O}(1/\epsilon)$ , where  $\epsilon \sim 0.2 - 0.3$

For  $\epsilon \sim 0.3$  we have naturally

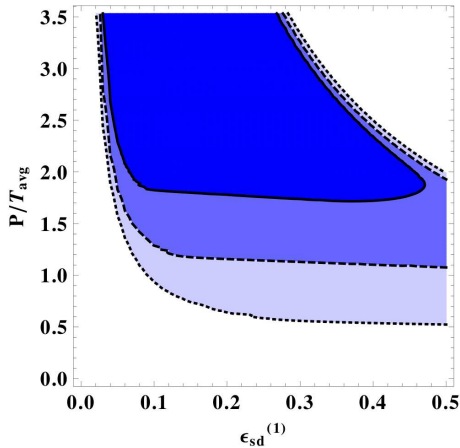
$$r_f = \frac{|V_{cb} V_{ub}|}{|V_{cs} V_{us}|} \frac{P}{T} \sim \frac{|V_{cb} V_{ub}|}{|V_{cs} V_{us}|} \frac{1}{\epsilon} \sim 0.2\%$$

- Right order of magnitude to explain  $\Delta \mathcal{A}_{CP}$
- $P_{\text{break}} = \epsilon_U P \sim \epsilon_U / \epsilon \sim \mathcal{O}(1)$  explains  $\text{Br}(K^+ K^-) = 2.8 \times \text{Br}(\pi^+ \pi^-)$
- Test by performing a fit to branching ratios and  $CP$  asymmetries.

# Fit to data



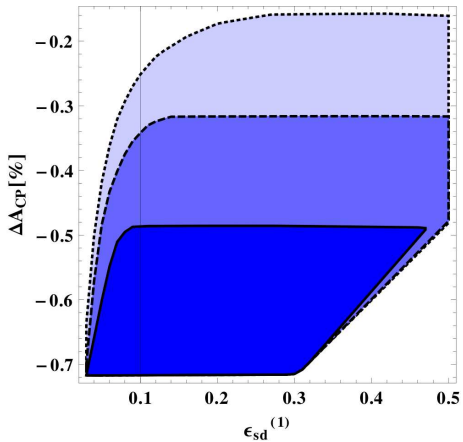
●  $P_{\text{break}} \lesssim T$



● nominal  $\epsilon_U$

●  $P \sim T/\epsilon$

# $\Delta\mathcal{A}_{CP}$ from fit





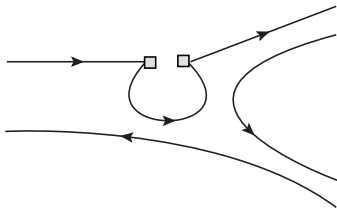
## Relations to other modes

By exchanging the spectator quark,

- $D^+ \rightarrow K^+ \overline{K}^0$

- $D_s^+ \rightarrow \pi^+ K^0$

receive contributions from



$\Rightarrow$  expect direct  $CP$  asymmetries of same order

# NP: viable models

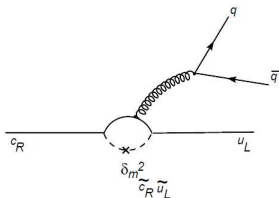
Constraints from  $D$  mixing, Kaon mixing, direct searches ...

- (More) Model-independent operator analysis

[Isidori, Kamenik, Ligeti, Perez 1111.4987]

- Supersymmetric examples ( $Q_{8g} = -g_s/4\pi^2 m_c \bar{u}_L \sigma_{\mu\nu} G^{\mu\nu} c_R$ )

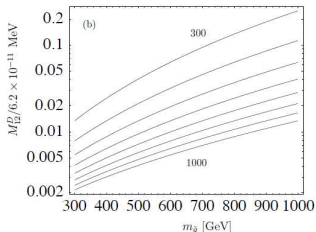
[Grossman, Kagan, Nir hep-ph/0609178; Giudice, Isidori, Paradisi 1201.6204]



[Diagrams by A. Kagan]

- Tree-level exchanges

[Hochberg, Nir 1112.5268; Altmannshofer, Primulando, Yu, Yu 1202.2866]



# How to distinguish NP from SM

NP models that have  $\Delta I = 3/2$  contributions:

- SM tree operators have both  $\Delta I = 1/2$  and  $\Delta I = 3/2$  contributions
- SM penguin operators ( $\propto \sum \bar{q}q, g$ ) have only  $\Delta I = 1/2$  contributions
- E.g.  $D^+ \rightarrow \pi^+\pi^0$  has  $I = 2$  final state  $\Rightarrow$  no SM contribution to  $\mathcal{A}^{\text{dir}}$ .
- Can construct more sophisticated sum rules [Grossman, Kagan, Zupan; work in progress]
- Example: Single scalar exchange could explain both  $\mathcal{A}_{\text{FB}}(t\bar{t})$  and  $\Delta\mathcal{A}_{\text{CP}}$  [Hochberg, Nir 1112.5268]

NP models that have only  $\Delta I = 1/2$  contributions:

- Build models and look for collider signatures. In many cases allowed parameters are close to experimental sensitivity [Altmannshofer, Primulando, Yu, Yu 1202.2866; see also Feldmann, Nandi, Soni 1202.3795]
- Example:  $LR$  contributions to  $Q_{8g}$  in SUSY [Grossman, Kagan, Nir hep-ph/0609178; Giudice, Isidori, Paradisi 1201.6204]

# Conclusion

- Enhanced penguin contributions in the SM can naturally explain both  $\Delta\mathcal{A}_{CP}$  and  $\text{Br}(K^+K^-) = 2.8 \times \text{Br}(\pi^+\pi^-)$  – plausible and consistent
- NP contributions not excluded, viable and testable models exist

# Backup slides

# Definitions

Experiments measure

$$\mathcal{A}_f := \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\overline{D}^0 \rightarrow f)}{\Gamma(D^0 \rightarrow f) + \Gamma(\overline{D}^0 \rightarrow f)} \approx \mathcal{A}_f^{\text{dir}} + \frac{\langle t(f) \rangle}{\tau} \mathcal{A}_f^{\text{ind}}$$

CDF:  $\mathcal{A}_f^{\text{ind}} = (-0.02 \pm 0.22)\%$

# Penguin matrix elements

$$P_{f,1} = \frac{G_F}{\sqrt{2}} V_{cb} V_{ub}^* C_6 \times \langle f | -2(\bar{u}u)_{S+P} \otimes^A (\bar{u}c)_{S-P} | D^0 \rangle$$

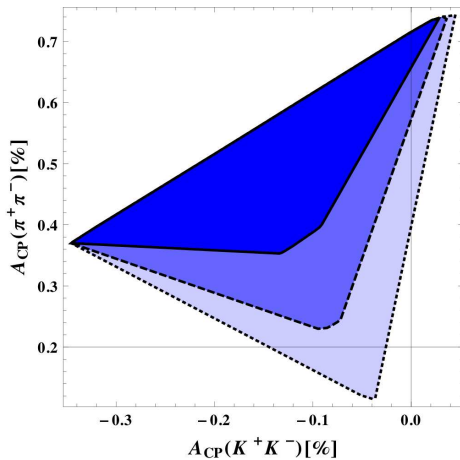
$$P_{f,2} = \frac{G_F}{\sqrt{2}} V_{cb} V_{ub}^* 2(C_4 + C_6) \times \langle f | (\bar{q}_\alpha q_\beta)_{V\pm A} \otimes^A (\bar{u}_\beta c_\alpha)_{V-A} | D^0 \rangle$$

$$C_{4(6)}^{\text{eff}}(\mu, q^2) = C_{4(6)}(\mu) + C_1(\mu) \frac{\alpha_s}{2\pi} \left[ \frac{1}{6} + \frac{1}{3} \log \left( \frac{m_c}{\mu} \right) - \frac{1}{8} G \left( \frac{m_s^2}{m_c^2}, \frac{m_d^2}{m_c^2}, \frac{q^2}{m_c^2} \right) \right]$$

$$\frac{\langle f | (\bar{u}u)_{S+P} \otimes^A (\bar{u}c)_{S-P} | D^0 \rangle}{\langle f | (\bar{s}_\alpha s_\beta - \bar{d}_\alpha d_\beta)_{V-A} \otimes^A (\bar{u}_\beta c_\alpha)_{V-A} | D^0 \rangle} = \mathcal{O}(N_c),$$

$$\frac{\langle f | (\bar{u}_\alpha u_\beta)_{V\pm A} \otimes^A (\bar{u}_\beta c_\alpha)_{V-A} | D^0 \rangle}{\langle f | (\bar{s}_\alpha s_\beta - \bar{d}_\alpha d_\beta)_{V-A} \otimes^A (\bar{u}_\beta c_\alpha)_{V-A} | D^0 \rangle} = \mathcal{O}(1).$$

# CP asymmetries from fit





## $U$ -spin decomposition

$$A(\bar{D}^0 \rightarrow K^+ \pi^-) = V_{cs} V_{ud}^* T(1 - \frac{1}{2} \epsilon'_{1T}),$$

$$A(\bar{D}^0 \rightarrow \pi^+ \pi^-) = \frac{1}{2} (V_{cd} V_{ud}^* - V_{cs} V_{us}^*) (T(1 + \frac{1}{2} \epsilon_{1T}) - P_{\text{break}}(1 - \frac{1}{2} \epsilon_{sd}^{(2)})) \\ - V_{cb}^* V_{ub} (T/2(1 + \frac{1}{2} \epsilon_{1T}) + P(1 - \frac{1}{2} \epsilon_P)),$$

$$A(\bar{D}^0 \rightarrow K^+ K^-) = \frac{1}{2} (V_{cs} V_{us}^* - V_{cd} V_{ud}^*) (T(1 - \frac{1}{2} \epsilon_{1T}) + P_{\text{break}}(1 + \frac{1}{2} \epsilon_{sd}^{(2)})) \\ - V_{cb}^* V_{ub} (T/2(1 - \frac{1}{2} \epsilon_{1T}) + P(1 + \frac{1}{2} \epsilon_P)),$$

$$A(\bar{D}^0 \rightarrow \pi^+ K^-) = V_{cd} V_{us}^* T(1 + \frac{1}{2} \epsilon'_{1T}).$$

# (Barbieri-Giudice-) Fine tuning

