
Quadratic sensitivity of the Higgs
mass due to Fayet-Iliopoulos
terms in five dimensions

Stefan Groot Nibbelink

University Bonn

collaboration with

D. Ghilencea, H.P. Nilles, M. Olechowski

based on:

Nucl. Phys. B619 (2001) 373, B619 (2001) 385

hep-th/0203055

and work in progress...

Motivation:

Extra dimensions:

- why 4 dimensions?
- String and M-theory
- D-branes

Supersymmetry:

- no fine-tuning
- very restrictive
- non-perturbative

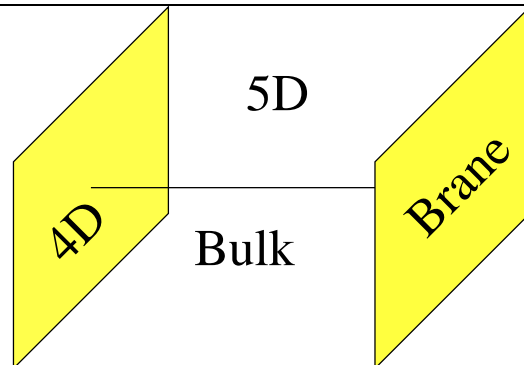
Experimental opportunities:

- Newton's law
- KK excitations
- running coupling
- small M_P

Plan of Talk:

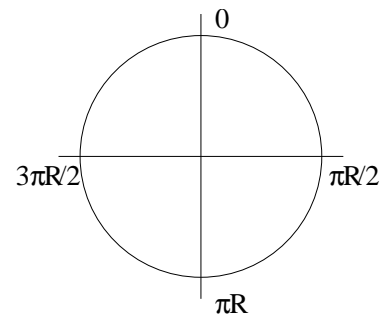
- Barbieri-Hall-Nomura Model
- Theoretical concerns
- Fayet-Iliopoulos contributions
- Conclusion / outlook

5 dimensional theory with boundaries



The $S^1/\mathbb{Z}_2 \times \mathbb{Z}_2$ orbifold bulk:

- “ $N = 1$ 5D supersymmetry”
- boundary conditions
- even/odd Fourier modes



Bulk fields:

Vector Multiplet:

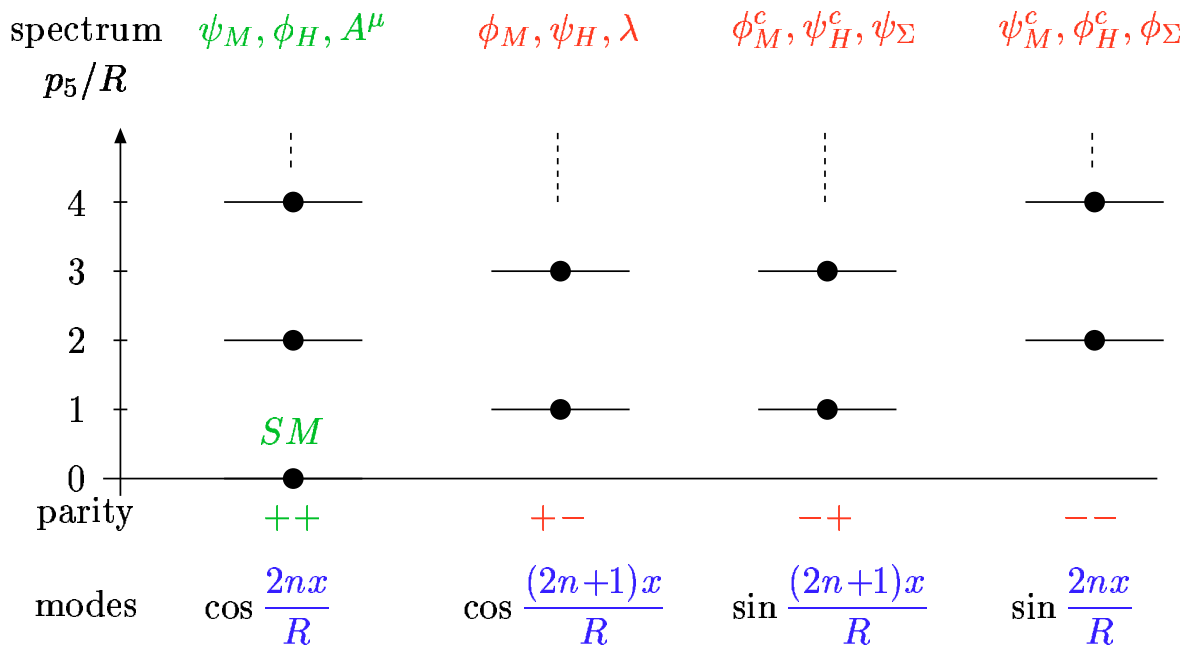
- gauge field A_μ, A_5
- gauginos λ^1, λ^2
- real scalar Φ

Hyper Multiplet:

- complex scalars ϕ, ϕ^c
- chiral fermions ψ, ψ^c

Barbieri-Hall-Nomura SM Model

Compactify a **5D $N = 1$ supersymmetric** field theory on $S^1/\mathbb{Z}_2 \times \mathbb{Z}'_2$ with **radius R** to obtain the **effective 4D field theory**, which has the **low energy spectrum** of the **Standard Model** Barbieri,Hall,Nomura '00.



SM in 4D :

ψ_M quarks/leptons ϕ_H higgs A^μ gauge fields

It was claimed that in this model the **Higgs mass** is finite and equal to **127 ± 8 GeV** based on a **one loop** calculation.

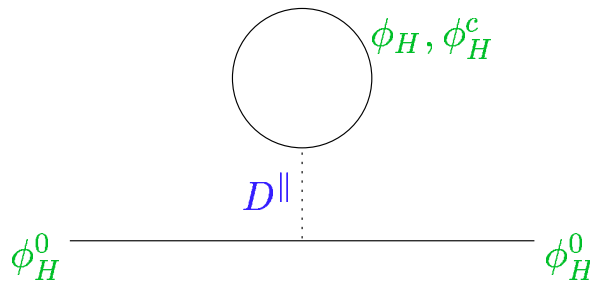
Some concerns

Questions concerning the physics of Kaluza-Klein theories:

- Can we make sense of infinitely many fields?
 - is KK theory “better” behaved than the low-energy its theory? Ghilencea, Nilles '01
 - What does “KK regularization” mean?
- Effective 4D theory versus 5D theory?
 - what (super)symmetries survive compactification?
 - 5D theory is not renormalizable?
 - what happens in the limit $R \rightarrow \infty$?

Quadratically divergent Fayet-Iliopoulos term

The **tadpole** of the **auxiliary** D^\parallel field has a **quadratic divergence** that filters into the **Higgs mass parameter**



$$\xi = g \int \frac{d^4 p_4}{(2\pi)^4} \left\{ \sum_{n \geq 0} \frac{1}{p_4^2 + (2n)^2 R^{-2}} - \sum_{n \geq 1} \frac{1}{p_4^2 + (2n)^2 R^{-2}} \right\}$$

Only the **zero mode** contribution survives [Ghilencea,GN,Nilles '01](#) so that we get a **4 dimensional** divergence:

$$\xi = g \int \frac{d^4 p_4}{(2\pi)^4} \frac{1}{p_4^2} \propto \Lambda^2$$

This result is **independent** of **radius** R . Hence, also holds in the **decompactification limit** $R \rightarrow \infty$!

The Higgs mass is quadratically sensitive to a high scale due to Fayet-Iliopoulos terms

- only the zero mode bosons in the loop contribute,
- this is independent of the radius R ,
- and very similar SM situation.

The FI terms have an interesting structure over the 5th dimension

- they localize on the branes, [Scrucca, Serone Silvestrini, Zwirner, '01](#)
- this can lead to localization of charged bulk fields to branes, [GN, Nilles, Olechowski, '02](#)
- which may change the phenomenology of such models...