

Dark Energy

Federico Piazza



Nobel Prize in Physics 2011



Photo: Roy Kaltschmidt. Courtesy: Lawrence Berkeley National Laboratory

Saul Perlmutter



Photo: Belinda Pratten, Australian National University

Brian P. Schmidt



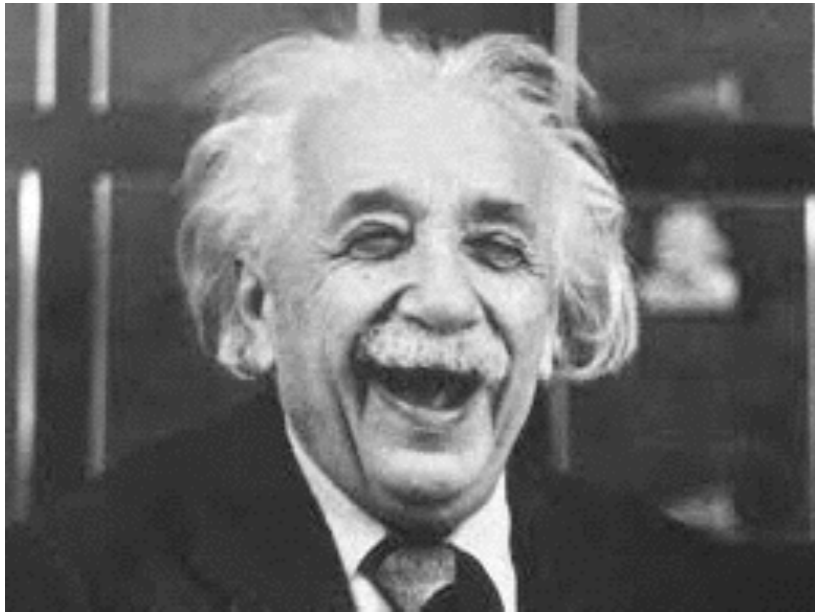
Photo: Homewood Photography

Adam G. Riess



The Universe is accelerating!

Why?!



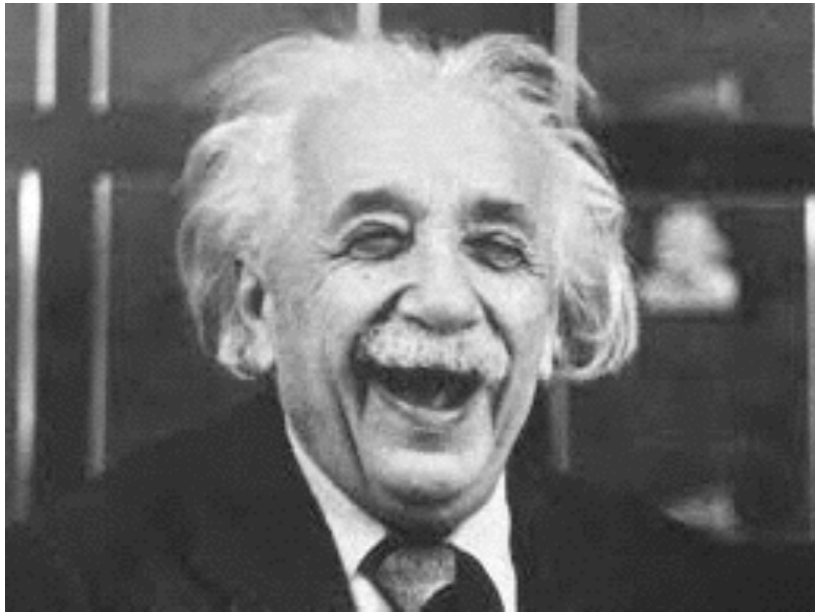
Λ CDM



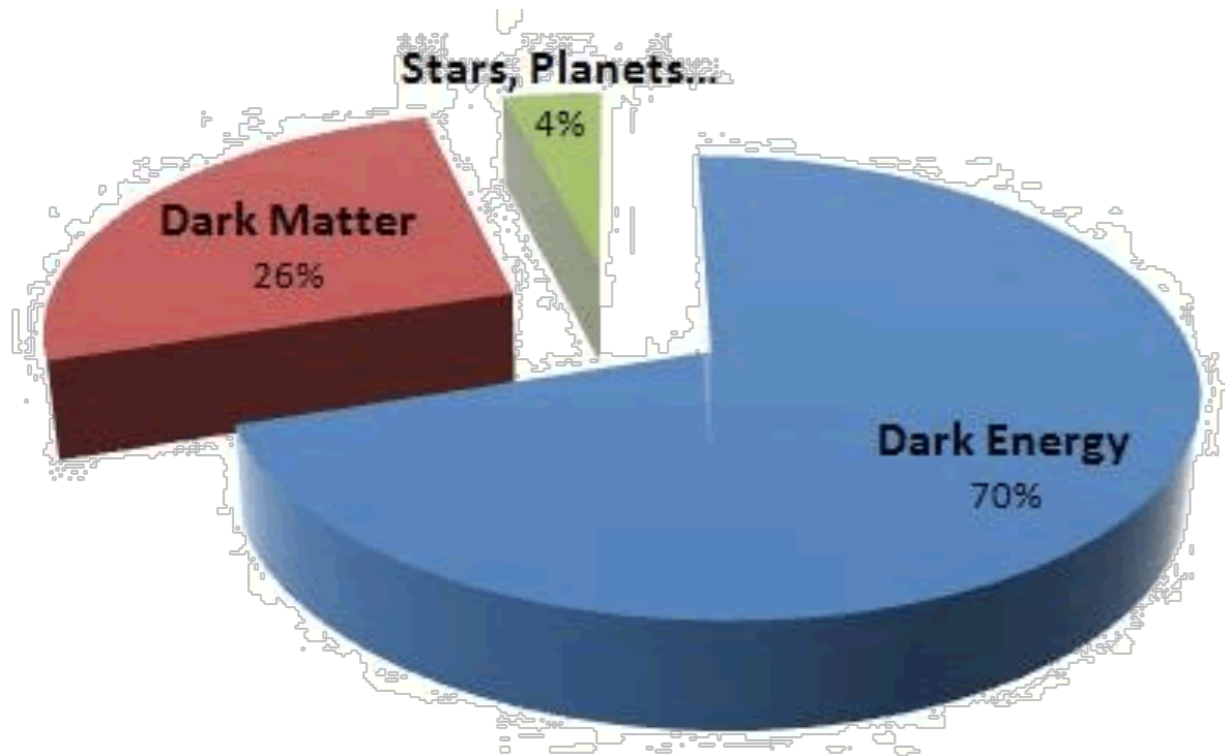
$g_{\mu\nu} + \text{STUFF}$



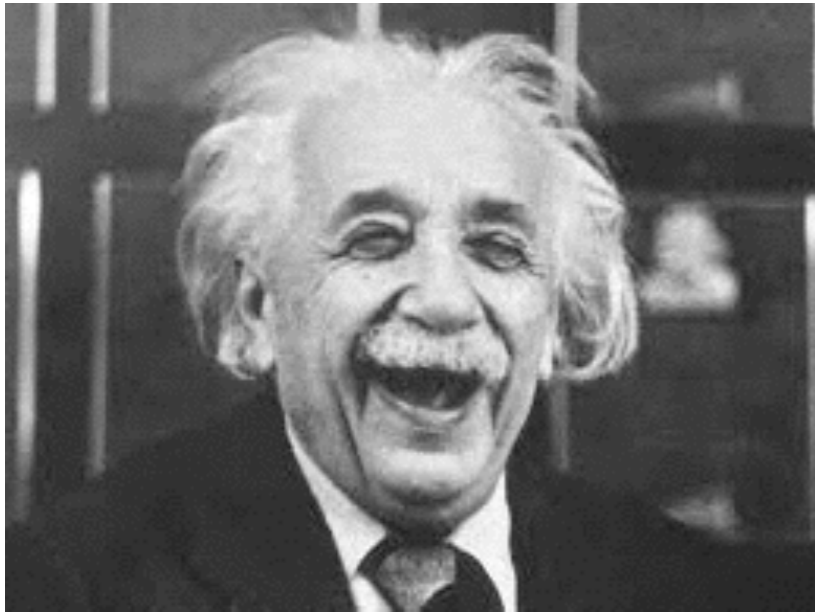
Other fundamental ingredients?



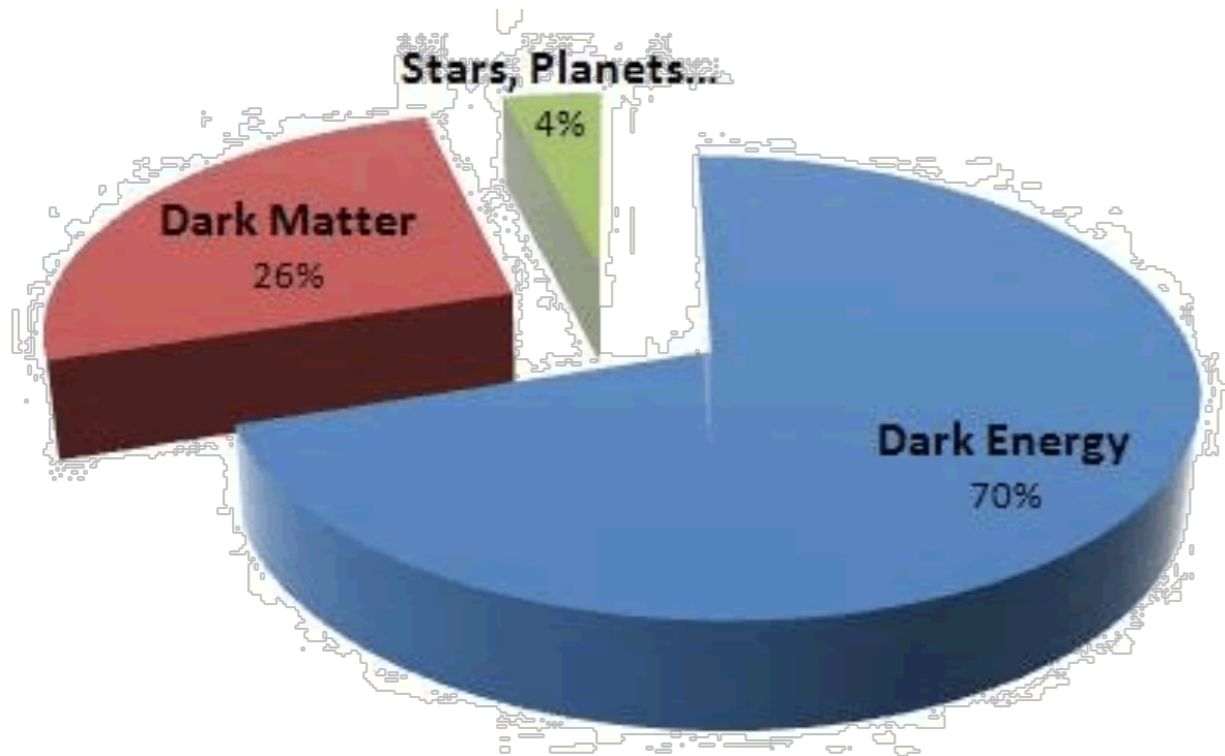
Λ CDM



Λ CDM cosmology

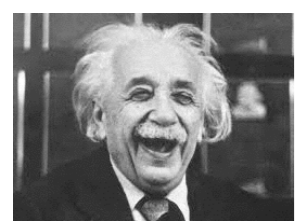


Λ CDM



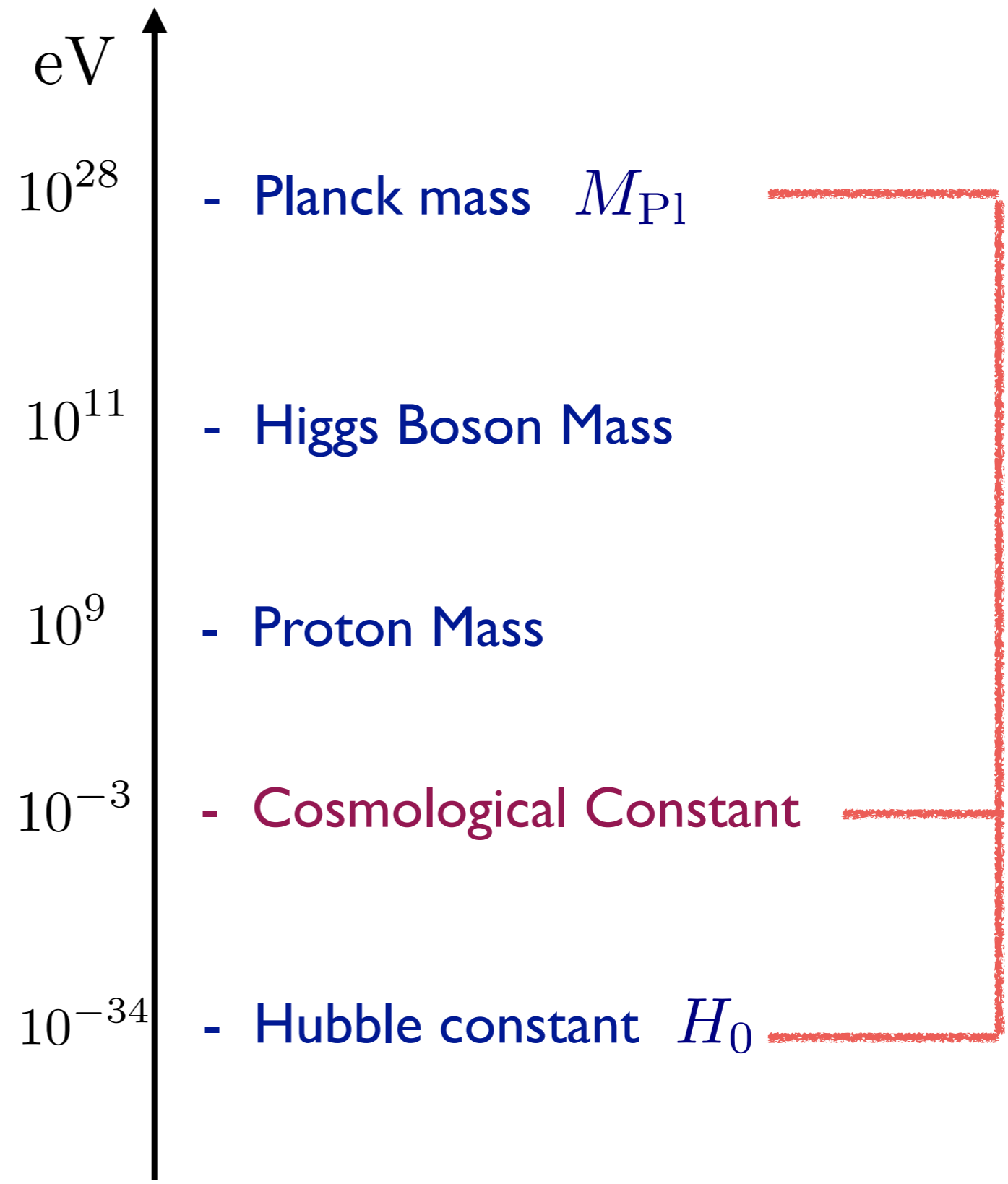
$$\Lambda \sim (10^{-3} eV)^4$$

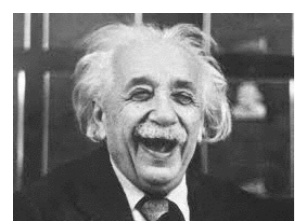
Λ CDM cosmology



$$(c = 1, \hbar = 1)$$

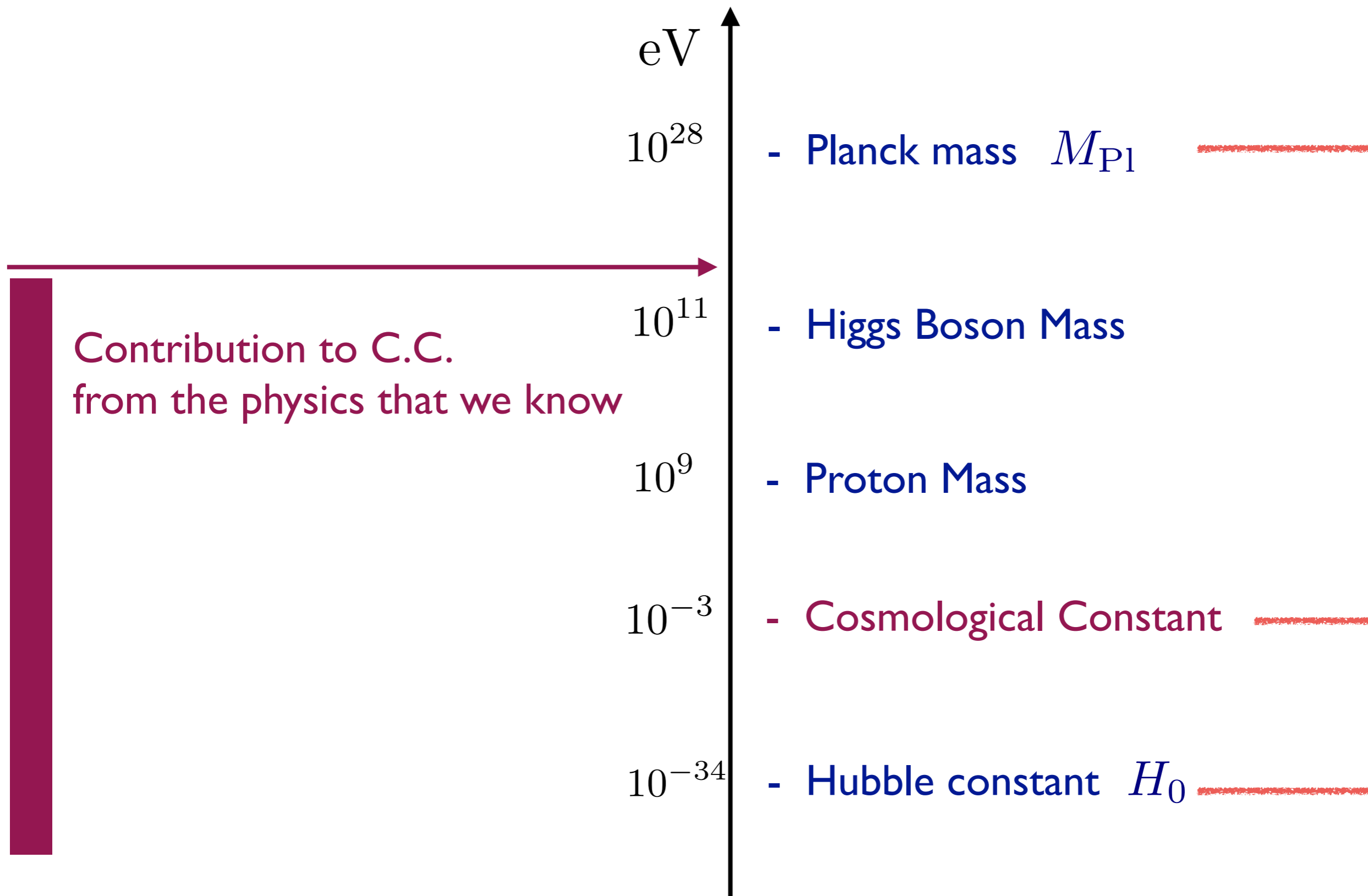
The size of the Cosmological Constant





$$(c = 1, \hbar = 1)$$

The size of the Cosmological Constant



Contribution to C.C.
from the physics that we know

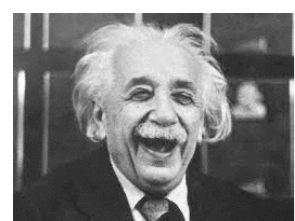
- Planck mass M_{Pl}

- Higgs Boson Mass

- Proton Mass

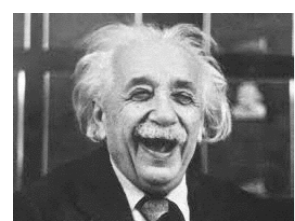
- Cosmological Constant

- Hubble constant H_0



Renounce to naturalness?

Usually, it works! (Ex: pion mass split, neutral kaons)

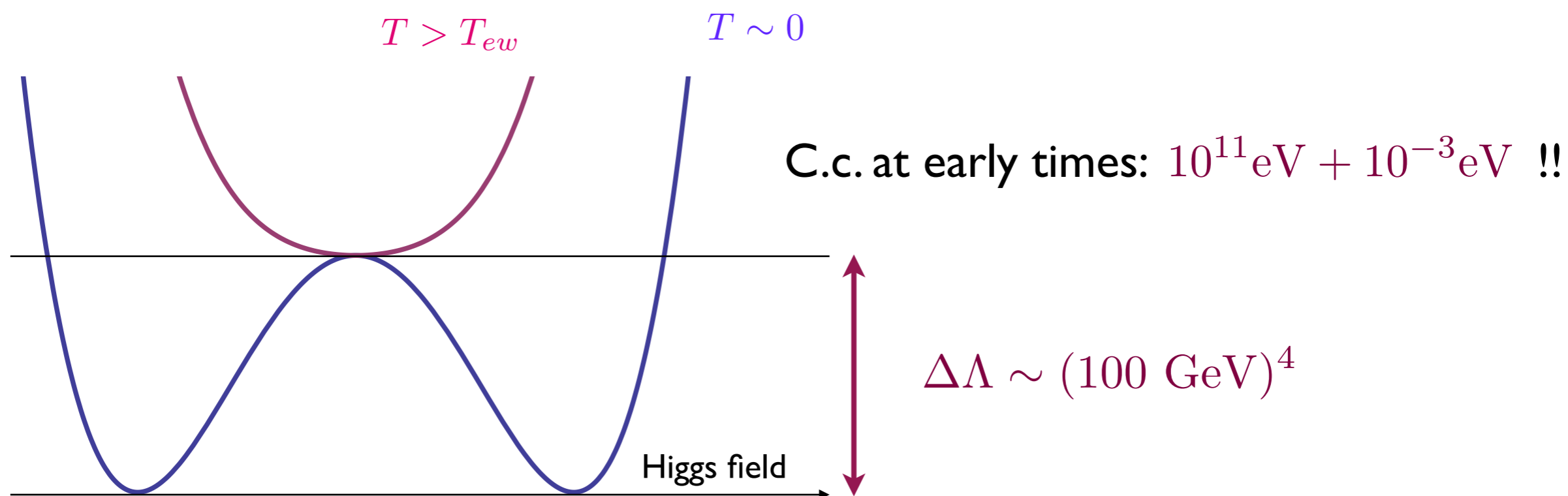


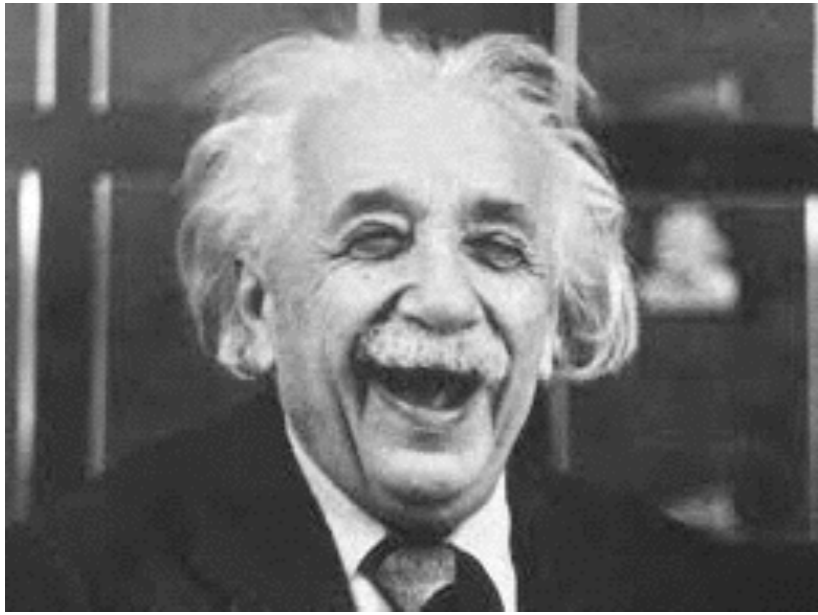
Renounce to naturalness?

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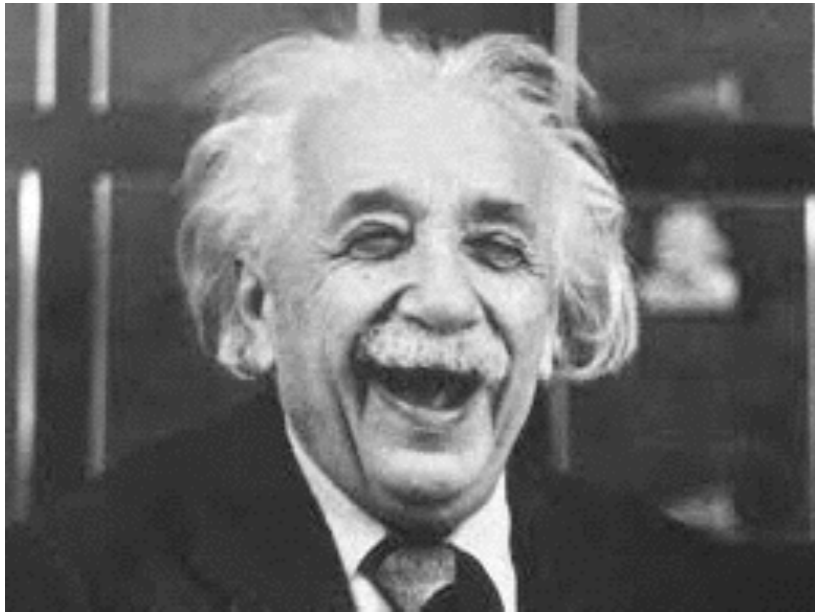
A puzzling value anyway...

EW phase transition





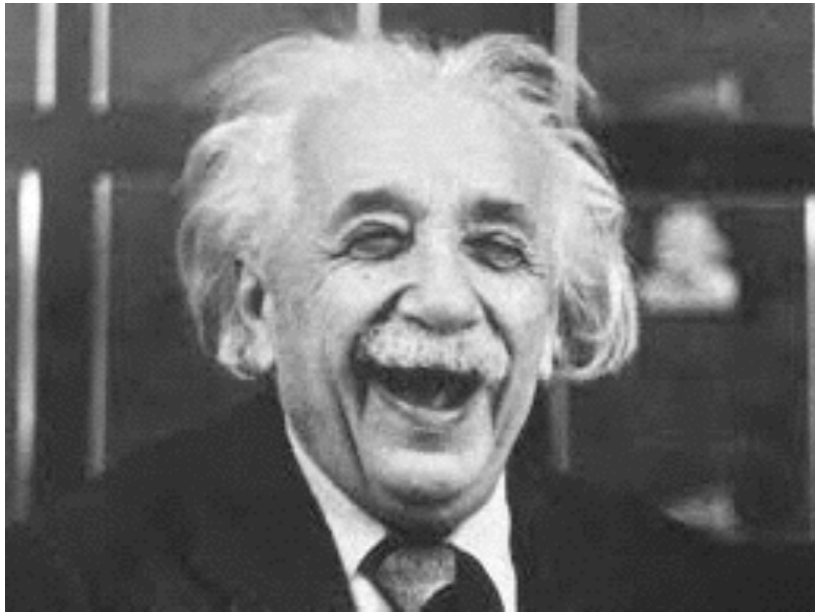
Λ CDM



Λ CDM

The only consistent
low energy theory for
a massless spin-two field $g_{\mu\nu}$.





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The skeleton of MG: Minkowski theory

- Poincaré invariant theory
- Fields in some representation of Lorentz group
- Boosts **spontaneously** broken
- Unbroken translations and rotations



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- Boosts **spontaneously** broken
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$$\left\{ \begin{array}{l} \bar{P}^\mu \\ \bar{J}^i \end{array} \right. \quad \begin{array}{l} \text{translations} \\ \text{rotations} \end{array}$$

$$[\bar{J}_i, \bar{P}_j] = i\epsilon_{ijk} \bar{P}_k$$

$$[\bar{J}_i, \bar{J}_j] = i\epsilon_{ijk} \bar{J}_k$$

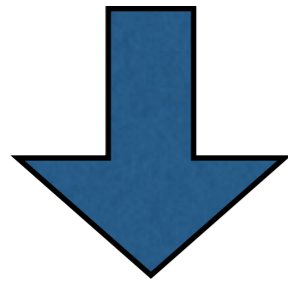


Classifying Condensed Matter

Full Symmetry group: Poincaré

$\left\{ \begin{array}{l} P^\mu \\ J^i \\ K^i \end{array} \right.$ translations
rotations
boosts

+ internal 'Q' symmetries



$\left\{ \begin{array}{l} \bar{P}^\mu \\ \bar{J}^i \end{array} \right.$ translations
rotations

$$[\bar{J}_i, \bar{P}_j] = i\epsilon_{ijk} \bar{P}_k$$

$$[\bar{J}_i, \bar{J}_j] = i\epsilon_{ijk} \bar{J}_k$$



Classifying Condensed Matter

Ex:

$$\begin{cases} \bar{H} & = H - \mu Q \\ \bar{P}^i & = P^i \\ \bar{J}^i & = J^i \end{cases}$$

internal symmetry: $U(1)$

Superfluid

1 Goldstone

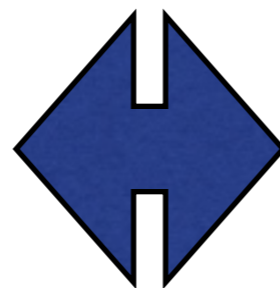
$$\langle \phi(x) \rangle = \mu t$$



Classifying Condensed Matter

System	Modified generators			# G.B.	Internal symmetries	Extra spacetime symmetries
	P_t	P_i	J_i			
1. type-I framid				3		
2. type-I superfluid	✓			1	$U(1)$	
3. type-I galileid		✓		1		Gal (3+1,1) ⁴
4. type-II framid			✓	6	$SO(3)$	
5. type-II galileid	✓	✓		1		Gal (3+1,1) ⁴
6. type-II superfluid	✓		✓	4	$SO(3) \times U(1)$	
7. solid		✓	✓	3	$ISO(3)$	
8. supersolid	✓	✓	✓	4	$ISO(3) \times U(1)$	

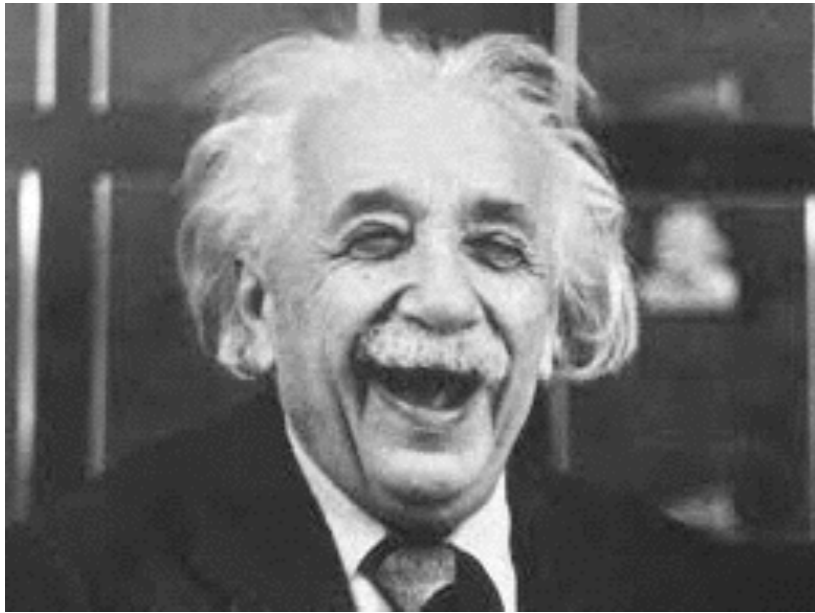
Condensed matter



Cosmology/modified gravity

superfluids
solids
framids

shift-symmetric scalar
solid inflation
Einstein aether



Λ CDM

The only consistent low energy theory for a massless spin-two field $g_{\mu\nu}$.



$g_{\mu\nu} + \text{STUFF}$



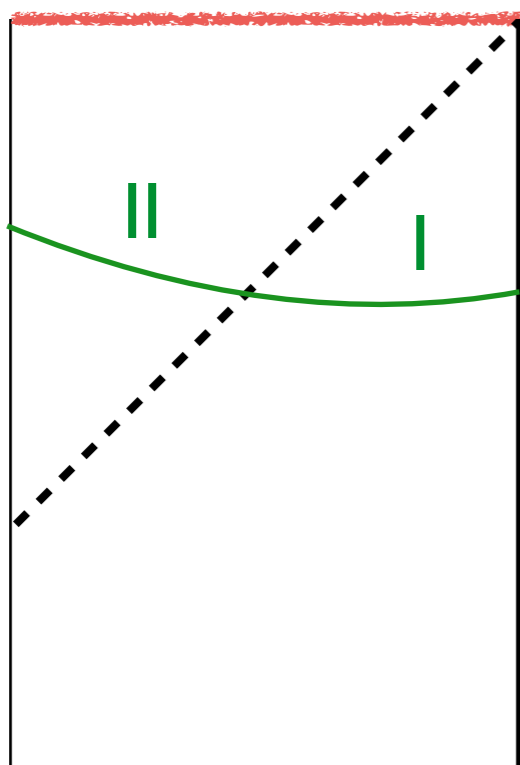
Other fundamental ingredients?



Where could the EFT 'mantra' be wrong?

Quantum gravity: not necessarily confined to the UV

BH in AdS



CFT

$$\mathcal{H} = \mathcal{H}_I \otimes \mathcal{H}_{II}$$

Inside dof: duplicate of those outside

Papadodimas, Raju, 2012-2016

'ER=EPR'

Entanglement defines (and generalizes) spacetime

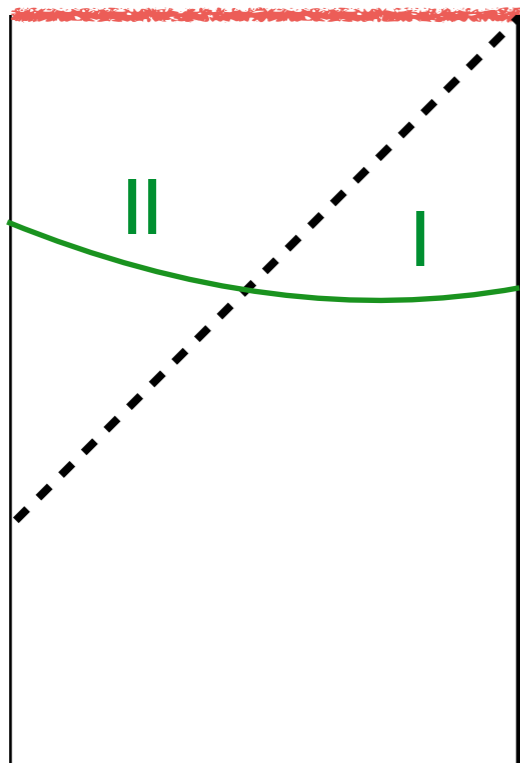
Susskind, Maldacena, 2013



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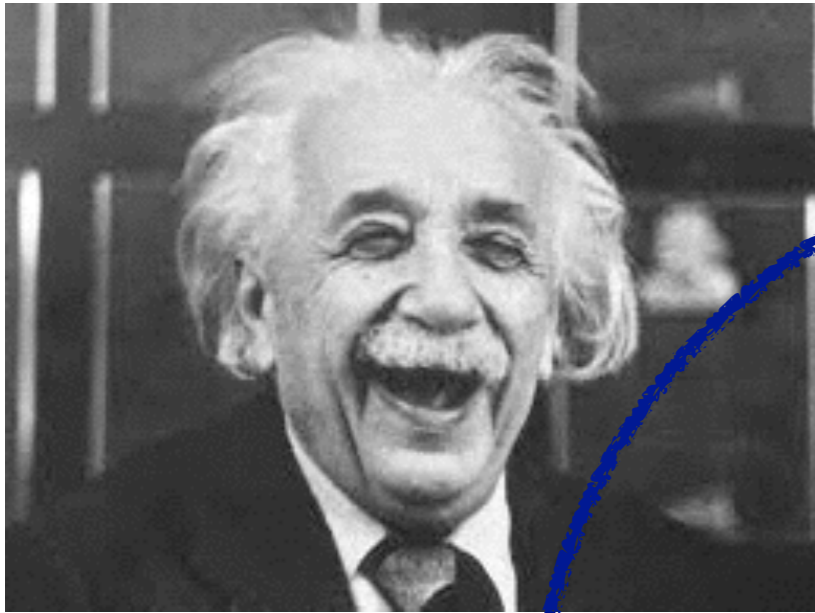
Papadodimas, Raju, 2012-2016

'ER=EPR'

Entanglement defines (and generalizes) spacetime

Susskind, Maldacena, 2013

In cosmology these effects are expected to be small



Λ CDM

EFT of DE

+ a scalar field ϕ

$g_{\mu\nu} + \text{STUFF}$



Other fundamental ingredients?



The effective field theory (EFT) of dark energy

- Most general description of **1 scalar degree of freedom** added to GR
- Matter universally coupled (Weak equivalence principle)
- **Cosmological perturbations** as the relevant objects of the theory
- **Background** (0th order) and **perturbation** (linear and +) sectors
- Good parameter space to constrain with data (see **Planck 2015**)

Unitary gauge in Cosmology (technical detour)

The Effective Field Theory of Inflation (Creminelli et al. '06, Cheung et al. '07)

Main idea: scalar degrees of freedom are 'eaten' by the metric. Ex:

$$\phi(t, \vec{x}) \rightarrow \phi_0(t) \quad (\delta\phi = 0) \quad -\frac{1}{2}\partial\phi^2 \rightarrow -\frac{1}{2}\dot{\phi}_0^2(t) g^{00}$$



The Action

$$\begin{aligned}
 S = & \int d^4x \sqrt{-g} \frac{M^2(t)}{2} \left[R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} \right. \\
 & \left. + \mu_2^2(t)(\delta g^{00})^2 - \mu_3(t) \delta K \delta g^{00} + \epsilon_4(t) \left(\delta K^\mu{}_\nu \delta K^\nu{}_\mu - \delta K^2 + \frac{R^{(3)} \delta g^{00}}{2} \right) + \dots \right]
 \end{aligned}$$

The Action

Background (expansion history)

$$\begin{aligned}
 S = \int d^4x \sqrt{-g} & \frac{M^2(t)}{2} \left[R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} \right. \\
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only affect perturbations

Complete background separation

$$S = \int d^4x \sqrt{-g} \frac{M^2(t)}{2} \left[R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} \right. \\ \left. + \mu_2^2(t)(\delta g^{00})^2 - \mu_3(t)\delta K\delta g^{00} + \epsilon_4(t) \left(\delta K^\mu_\nu \delta K^\nu_\mu - \delta K^2 + \frac{R^{(3)}\delta g^{00}}{2} \right) + \dots \right]$$

$$\lambda(t), \mathcal{C}(t), \mu(t) \equiv \frac{d \ln M^2(t)}{dt}$$

 $\bar{w}(t)$

Expansion History

 $\mu(t)$
 $\mu_3(t)$
 $\epsilon_4(t)$
 $\mu_2^2(t)$

Growth rate, lensing etc.

Unconstrained

Complete background separation

$$S = \int d^4x \sqrt{-g} \frac{M^2(t)}{2} \left[R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} + \mu_2^2(t)(\delta g^{00})^2 - \mu_3(t)\delta K\delta g^{00} + \epsilon_4(t) \left(\delta K^\mu_\nu \delta K^\nu_\mu - \delta K^2 + \frac{R^{(3)}\delta g^{00}}{2} \right) + \dots \right]$$

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Expansion History

$\mu(t)$

$\mu_3(t)$

$\epsilon_4(t)$

$\mu_2^2(t)$

Growth rate, lensing etc.

Unconstrained

Alternatively

$\alpha_K(t), \alpha_M(t), \alpha_B(t), \alpha_T(t)$

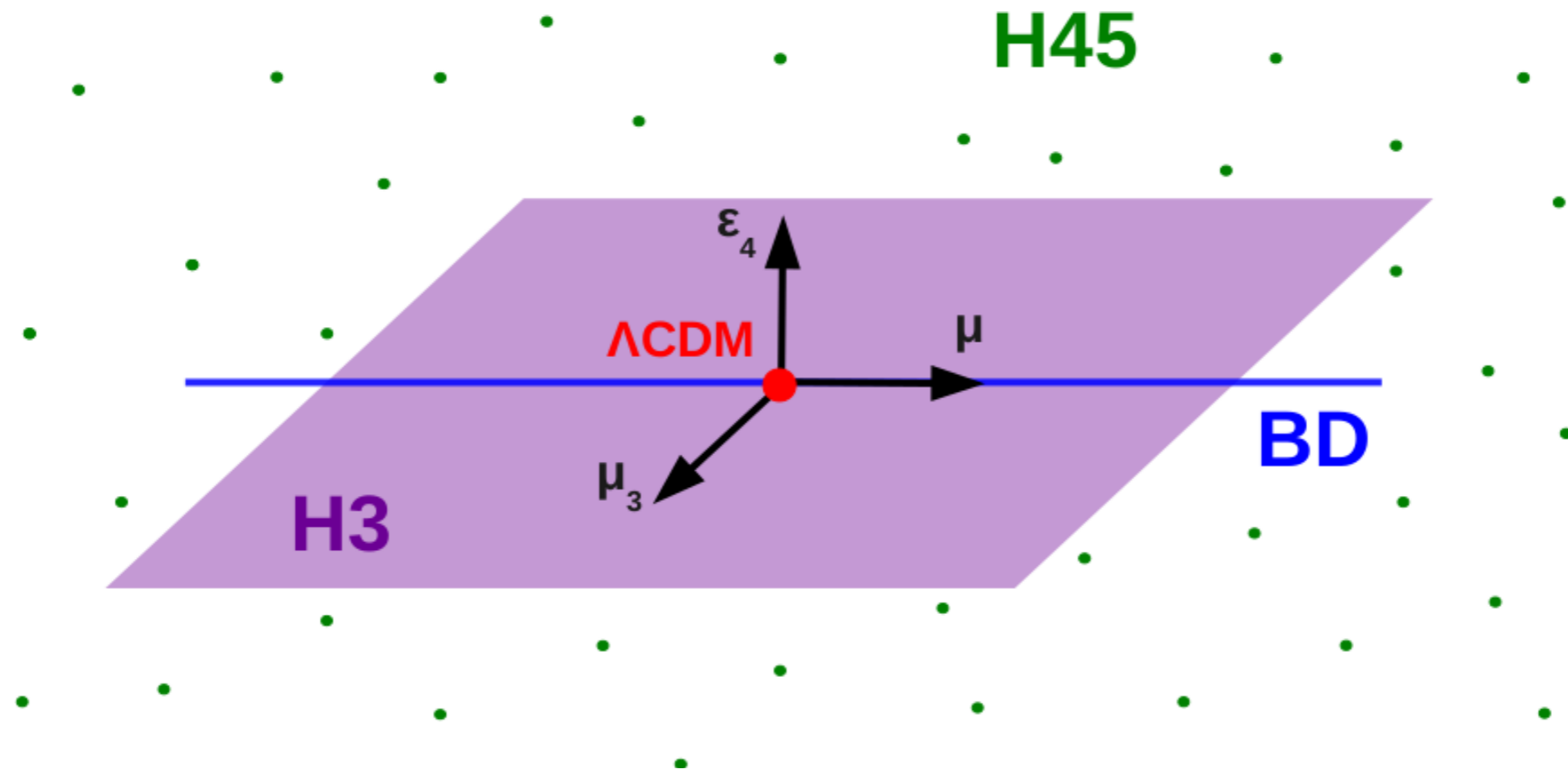
Bellini, Sawicki '14

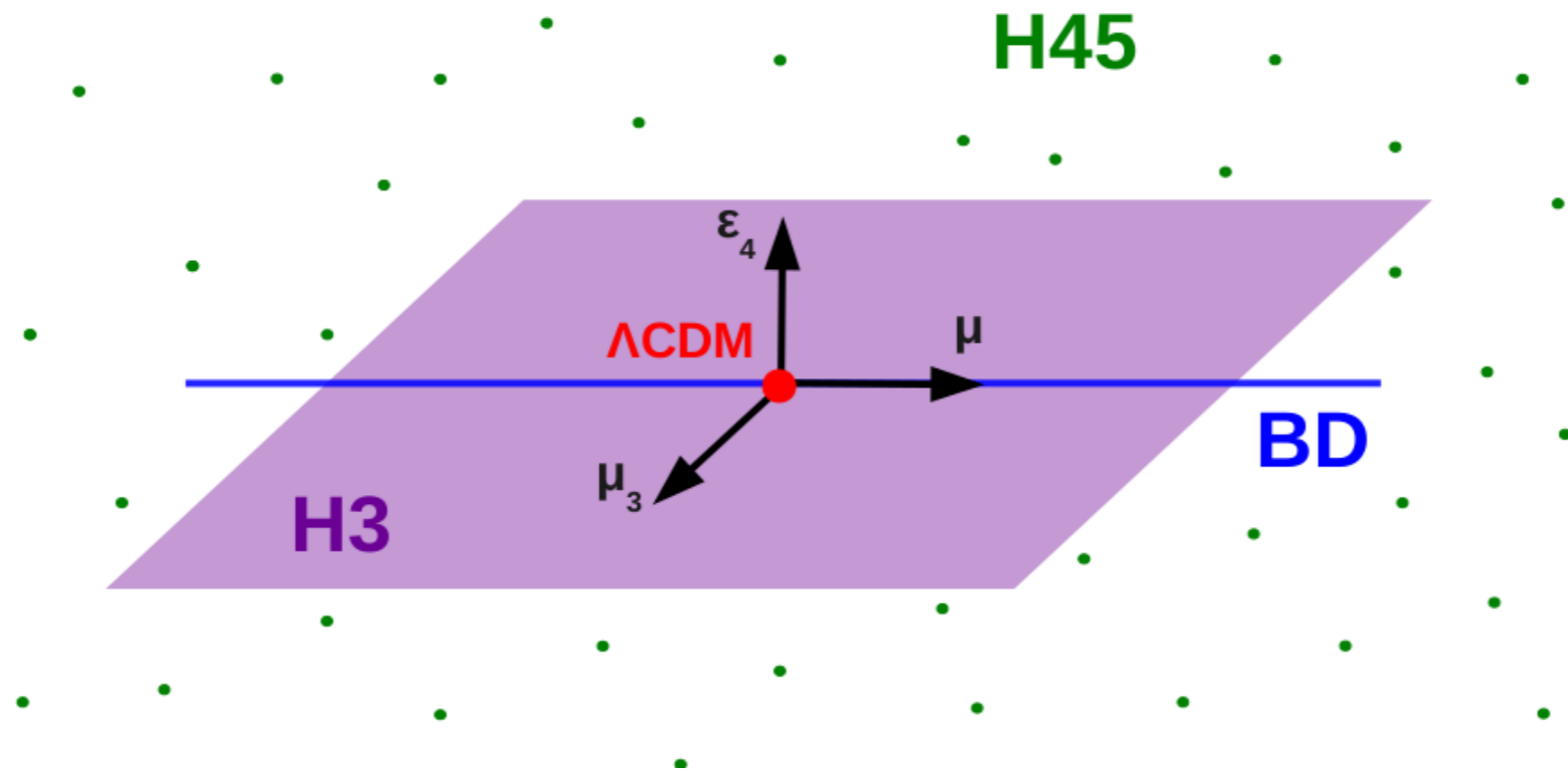
Gleyzes, Langlois, F.P., Vernizzi '14

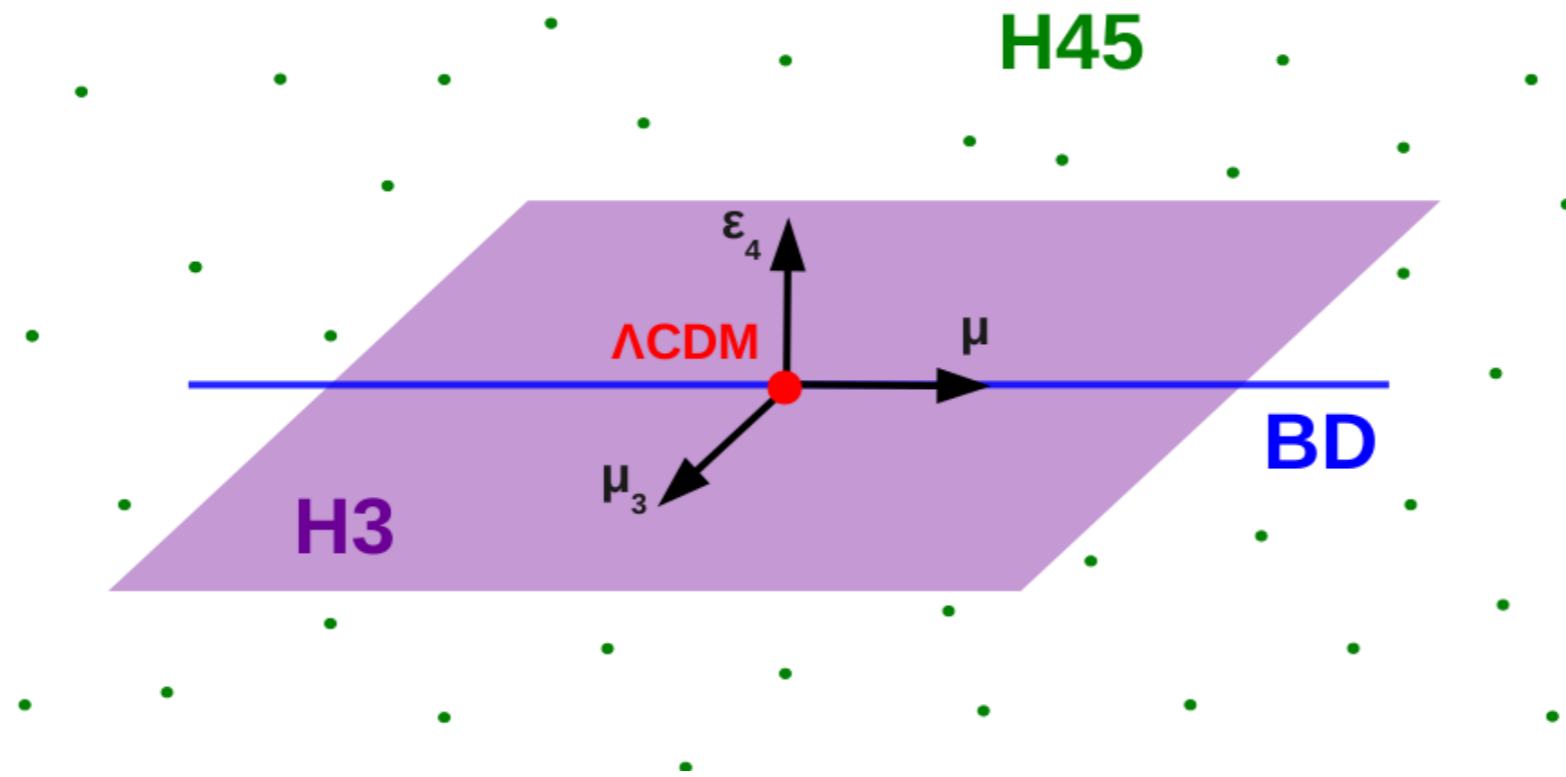
Gleyzes, Langlois, Vernizzi '14

The space of modified gravity

$$S = \int d^4x \sqrt{-g} \frac{M^2(t)}{2} \left[R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} + \mu_2^2(t)(\delta g^{00})^2 - \mu_3(t)\delta K\delta g^{00} + \epsilon_4(t) \left(\delta K^\mu_\nu \delta K^\nu_\mu - \delta K^2 + \frac{R^{(3)}\delta g^{00}}{2} \right) + \dots \right]$$



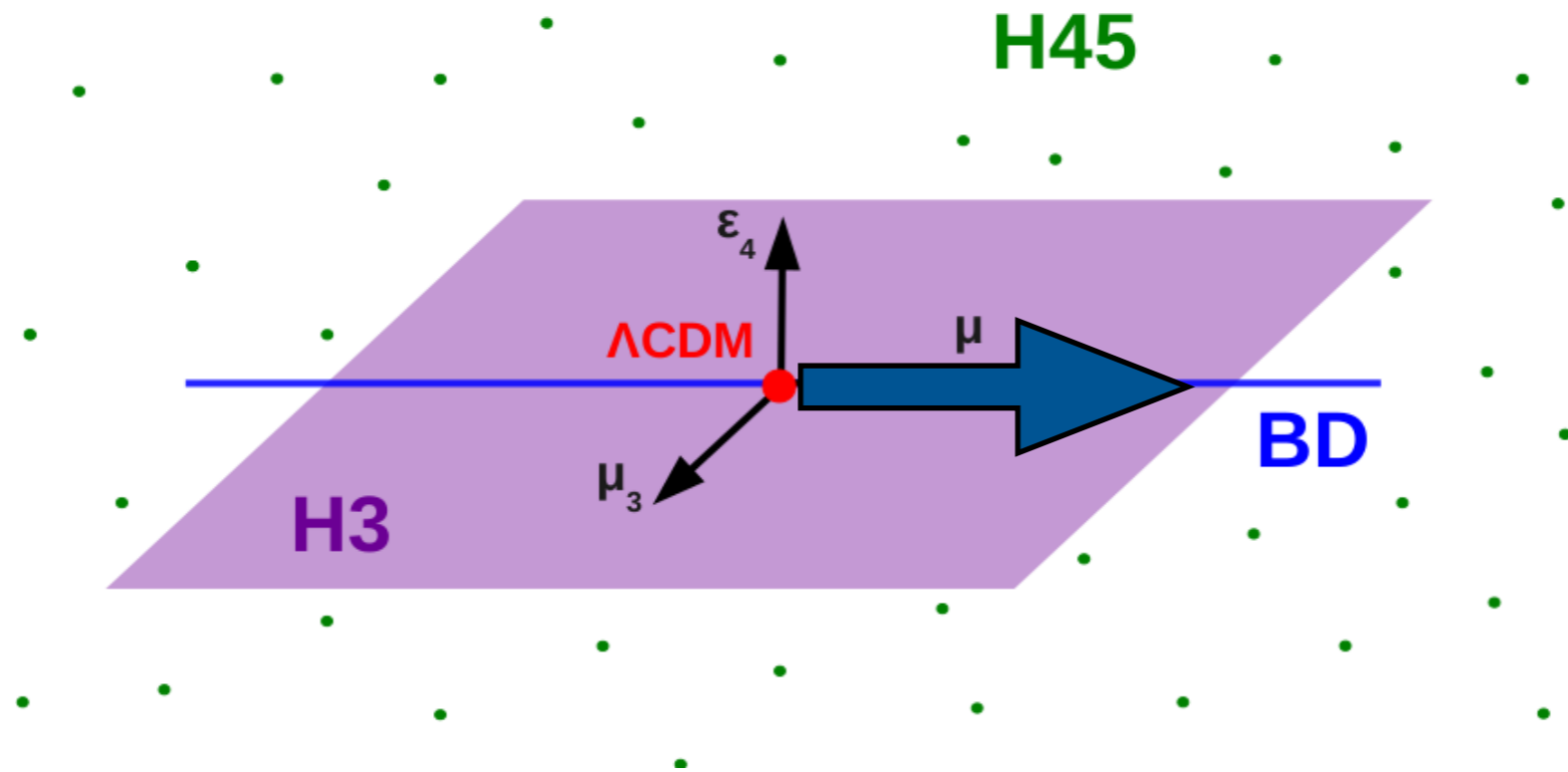




Quintessence
k-essence
etc.

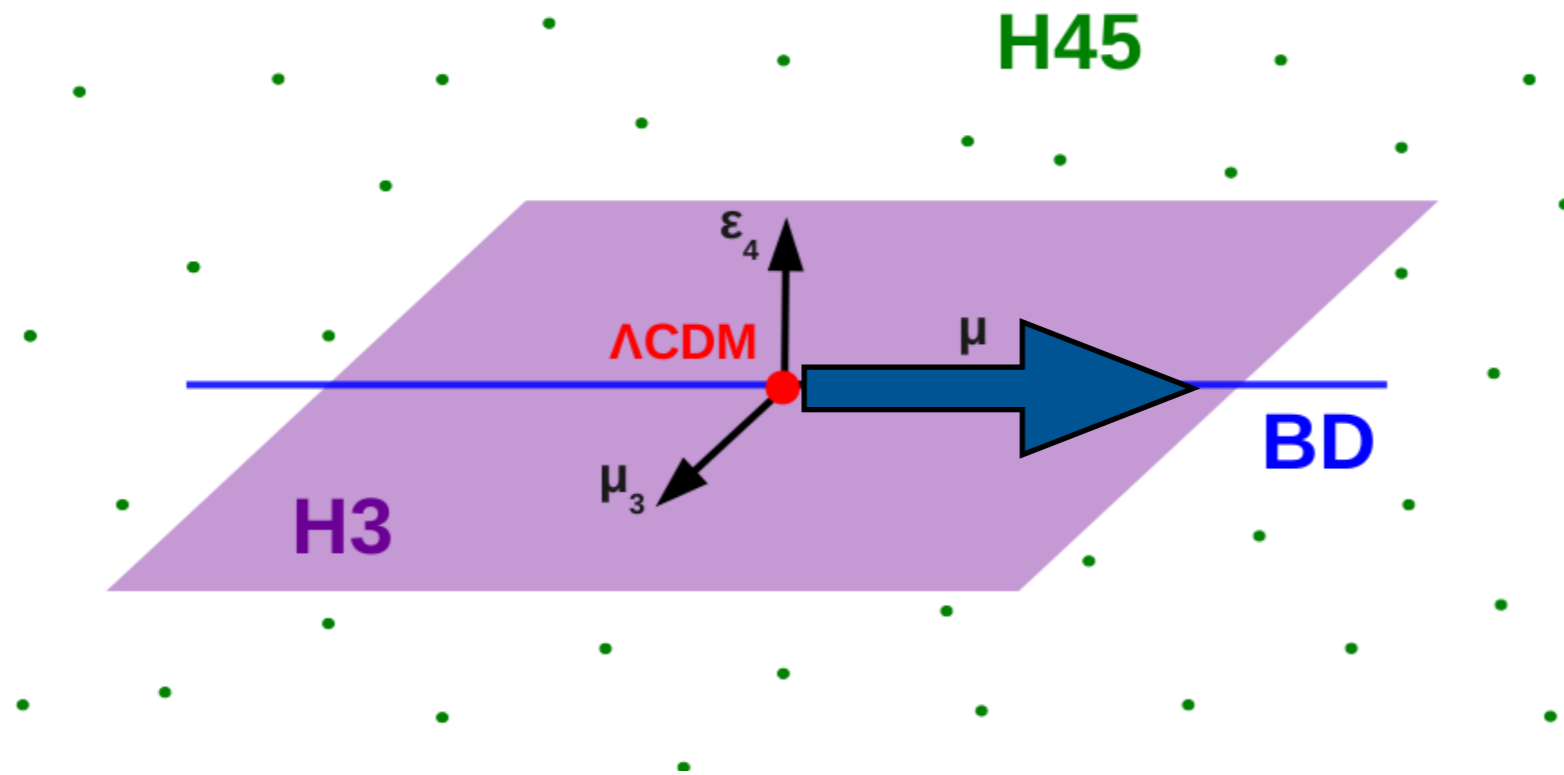
Minimally coupled

$(w \neq -1)$



The μ direction (Brans-Dicke, $F(R)$ theories etc.)

$$\mu \equiv \frac{d \log M^2}{dt}$$



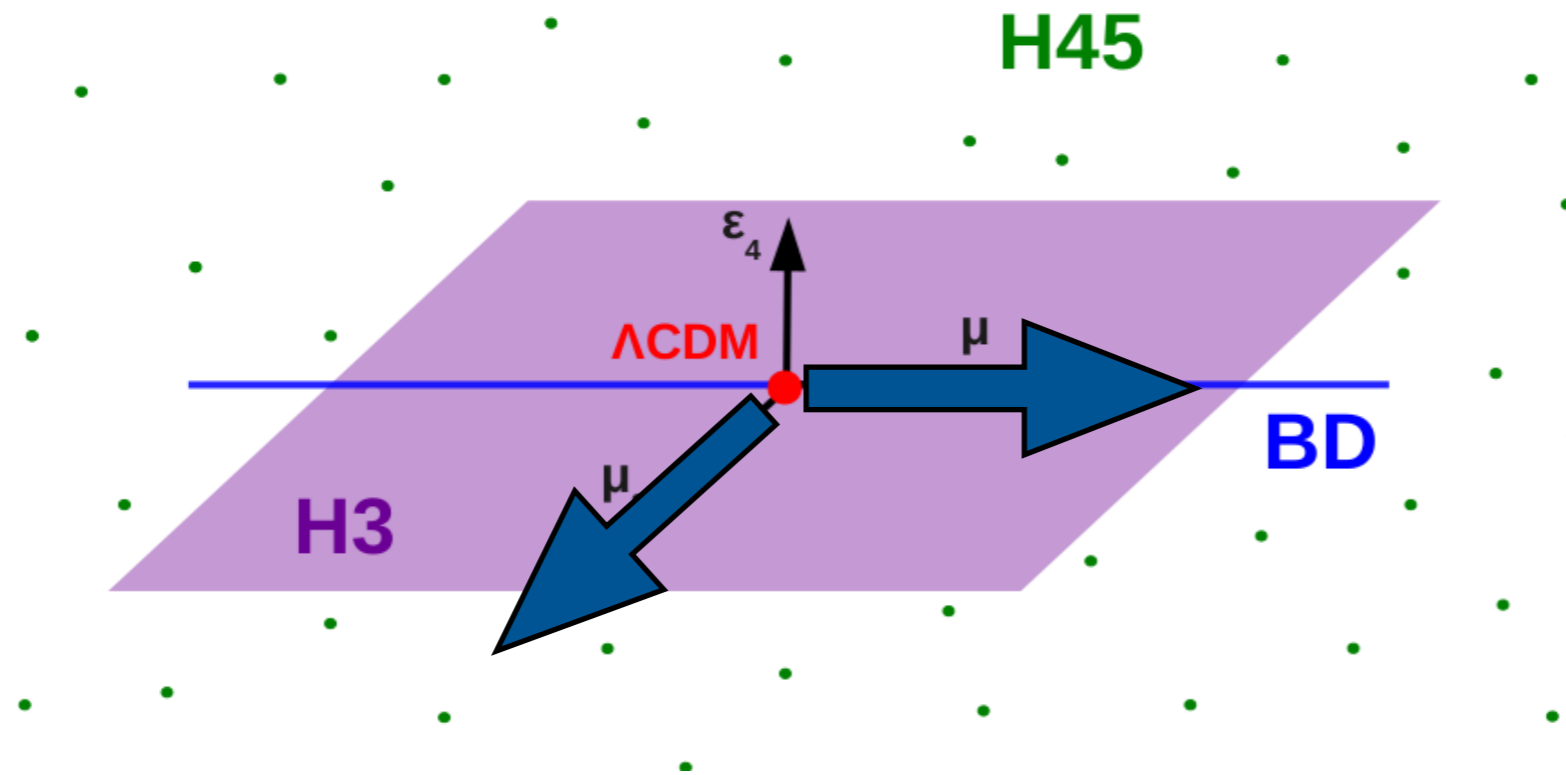
The μ direction (Brans-Dicke, F(R) theories etc.)

$$\mu \equiv \frac{d \log M^2}{dt}$$

self-acceleration

$$H^2 = \frac{1}{3M^2(t)} [\rho_m(t) + \rho_{DE}(t)]$$

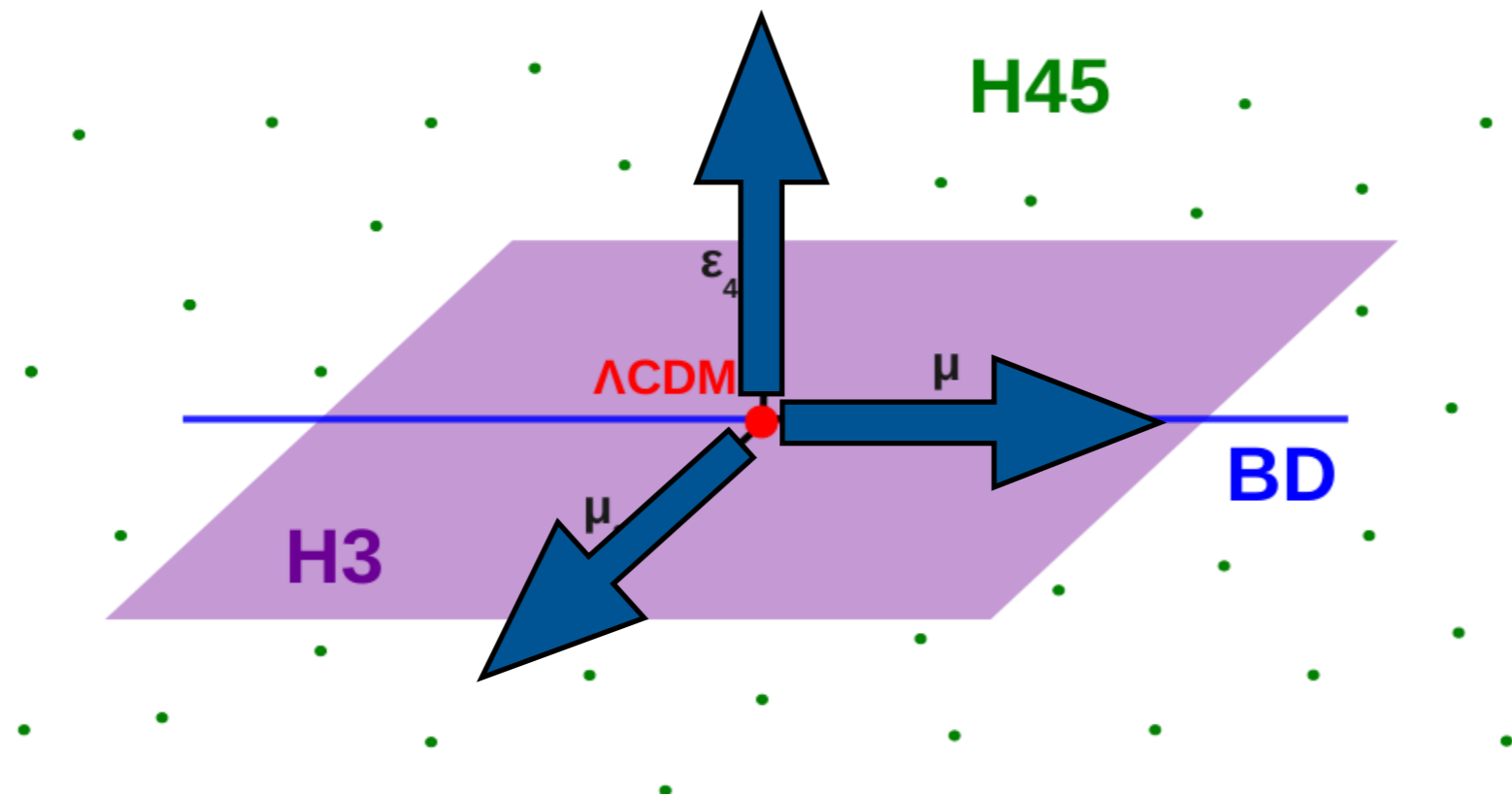
‘normal’ negative pressure



The μ_3 direction

“Galilean Cosmology” (Chow and Khoury, 2009)

Galileon 3/ Horndeski 3



“Generalized Galileons” (\equiv Horndeski)

(Deffayet et al., 2011)

$$\mathcal{L}_2 = A(\phi, X) ,$$

$$\mathcal{L}_3 = B(\phi, X)\square\phi ,$$

$$\mathcal{L}_4 = C(\phi, X)R - 2C_{,X}(\phi, X) [(\square\phi)^2 - (\nabla_\mu\nabla_\nu\phi)^2] ,$$

$$\mathcal{L}_5 = D(\phi, X)G^{\mu\nu}\nabla_\mu\nabla_\nu\phi + \frac{1}{3}D_{,X}(\phi, X) [(\square\phi)^3 - 3(\square\phi)(\nabla_\mu\nabla_\nu\phi)^2 + 2(\nabla_\mu\nabla_\nu\phi)^3] ,$$

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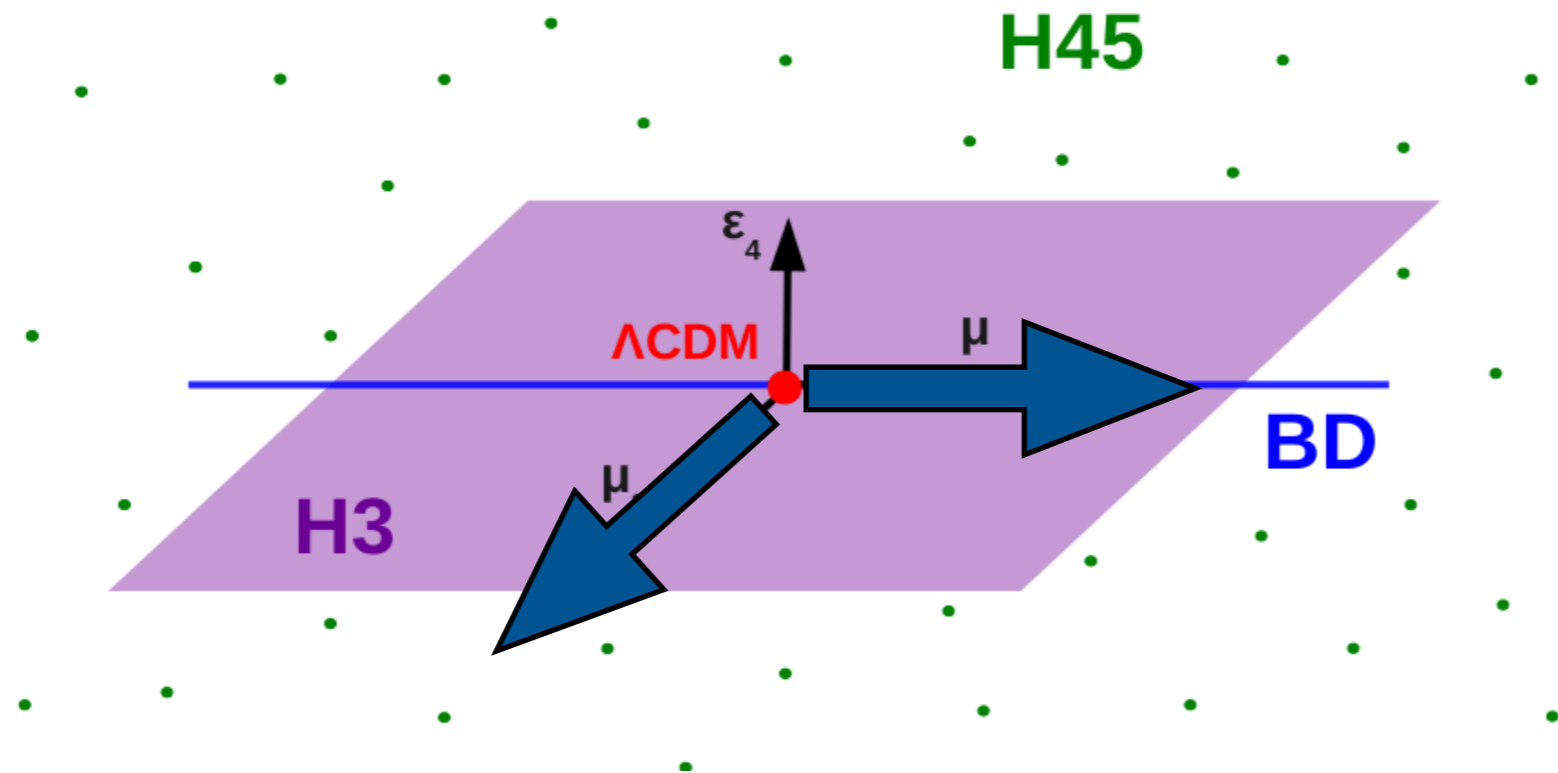
$\epsilon_4(t)$ $\tilde{\epsilon}_4(t)$

Beyond Horndeski

The most general (linear) theory without higher derivatives on the propagating degree of freedom

see Masahide talk on Friday

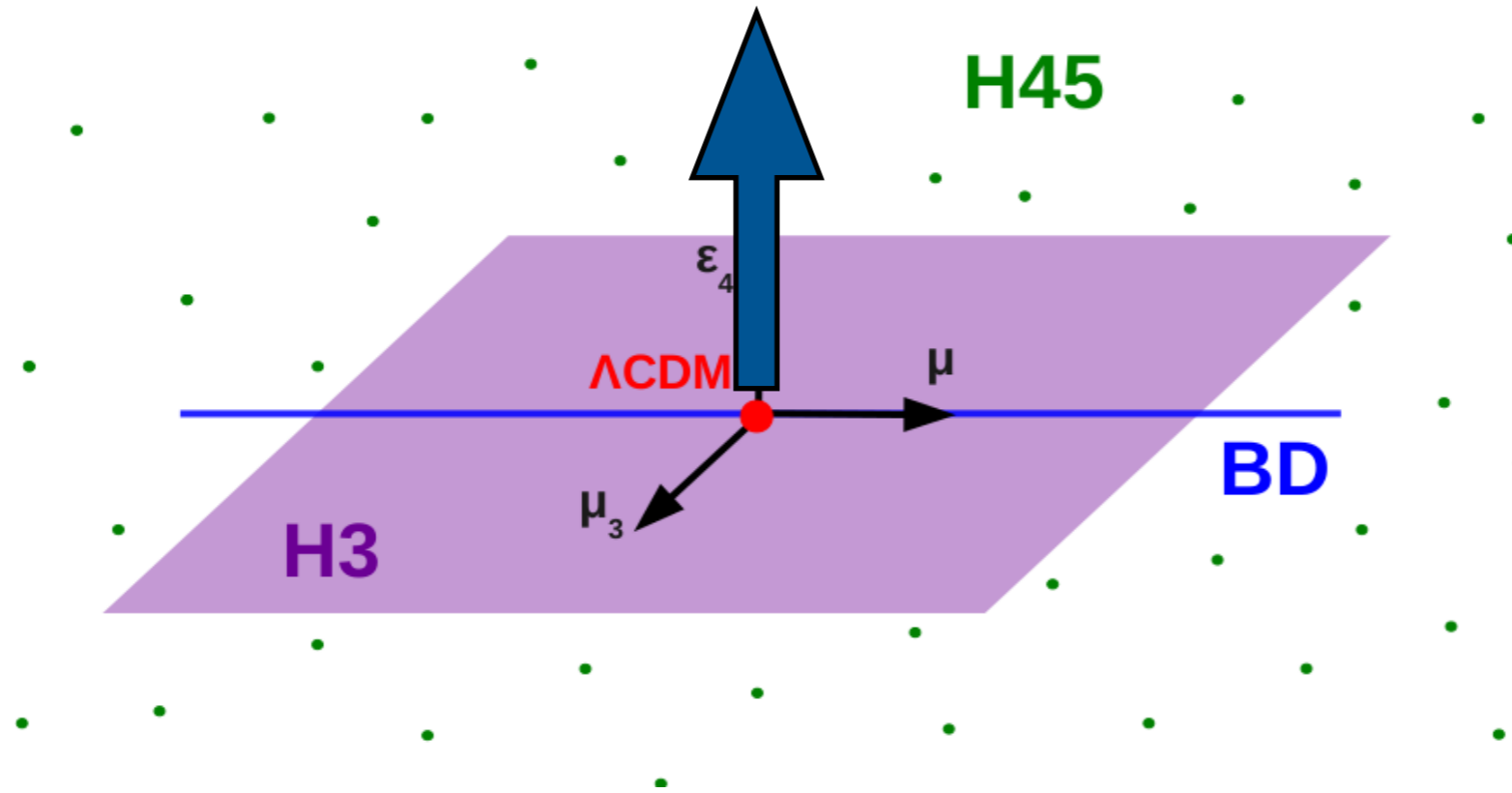
Newtonian gauge: scalar d.o.f.: Φ, Ψ, π



$$\mathcal{L} = (\mu - \mu_3) \vec{\nabla} \Phi \vec{\nabla} \pi + \dots$$

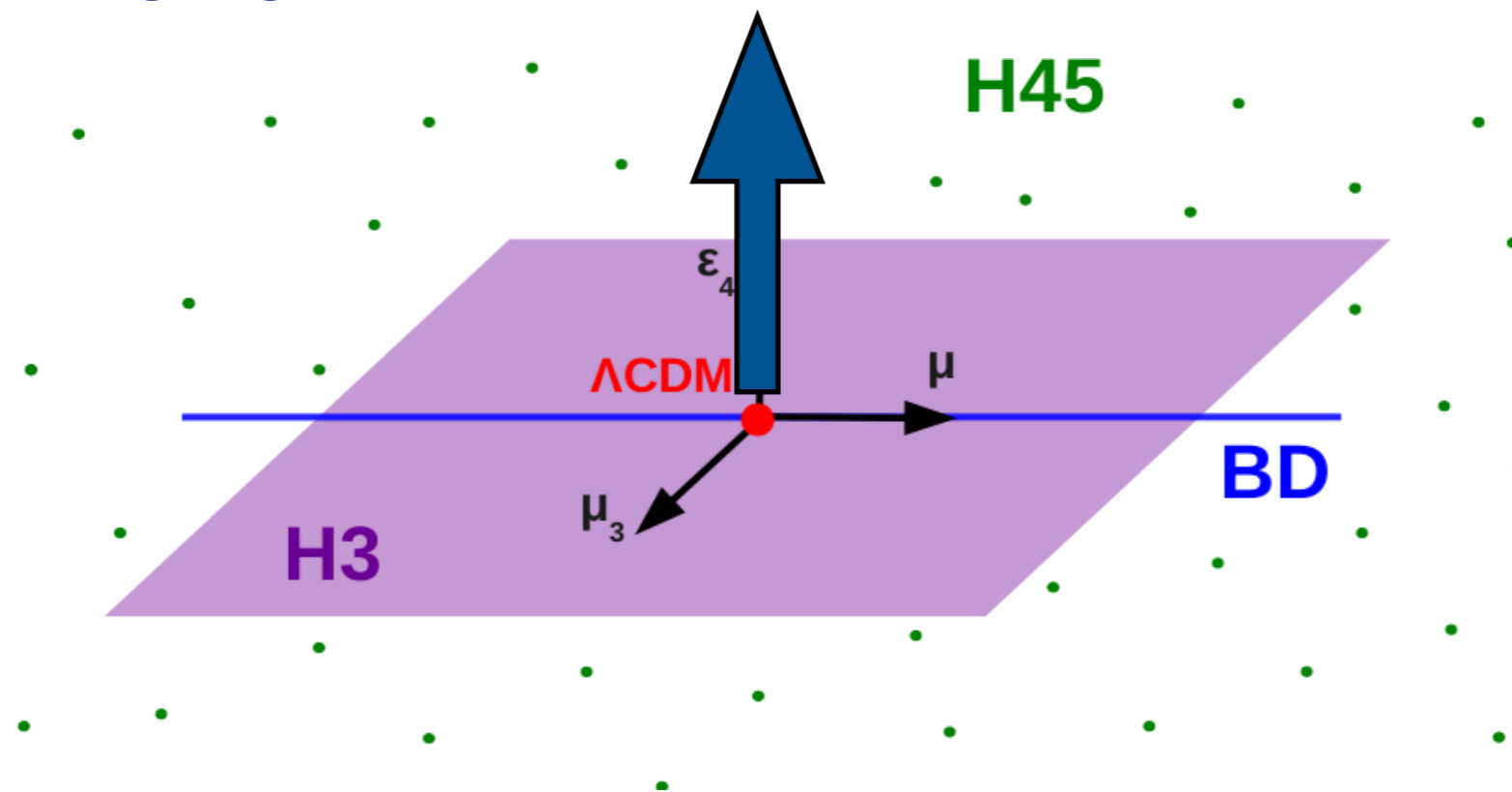
kinetic couplings metric-scalar

Newtonian gauge: scalar d.o.f.: Φ, Ψ, π



$$\mathcal{L} = (\dot{\epsilon}_4 + H\epsilon_4) \vec{\nabla} \Psi \vec{\nabla} \pi$$

Newtonian gauge: scalar d.o.f.: Φ, Ψ, π

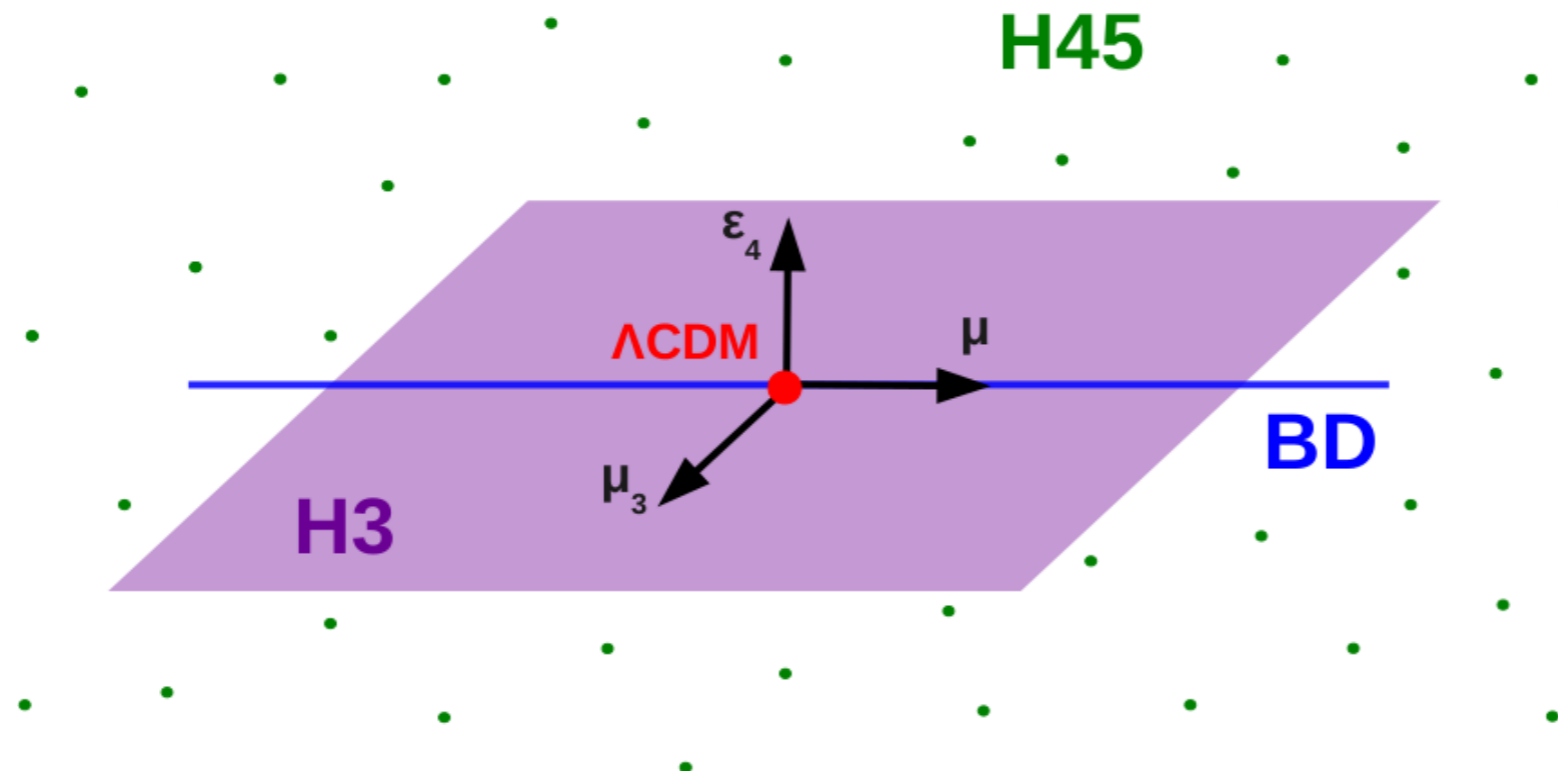


$$\mathcal{L} = (\dot{\epsilon}_4 + H\epsilon_4) \vec{\nabla} \Psi \vec{\nabla} \pi$$

$$c_T^2 = \frac{1}{1 + \epsilon_4}$$

but also: speed of gravitational waves!

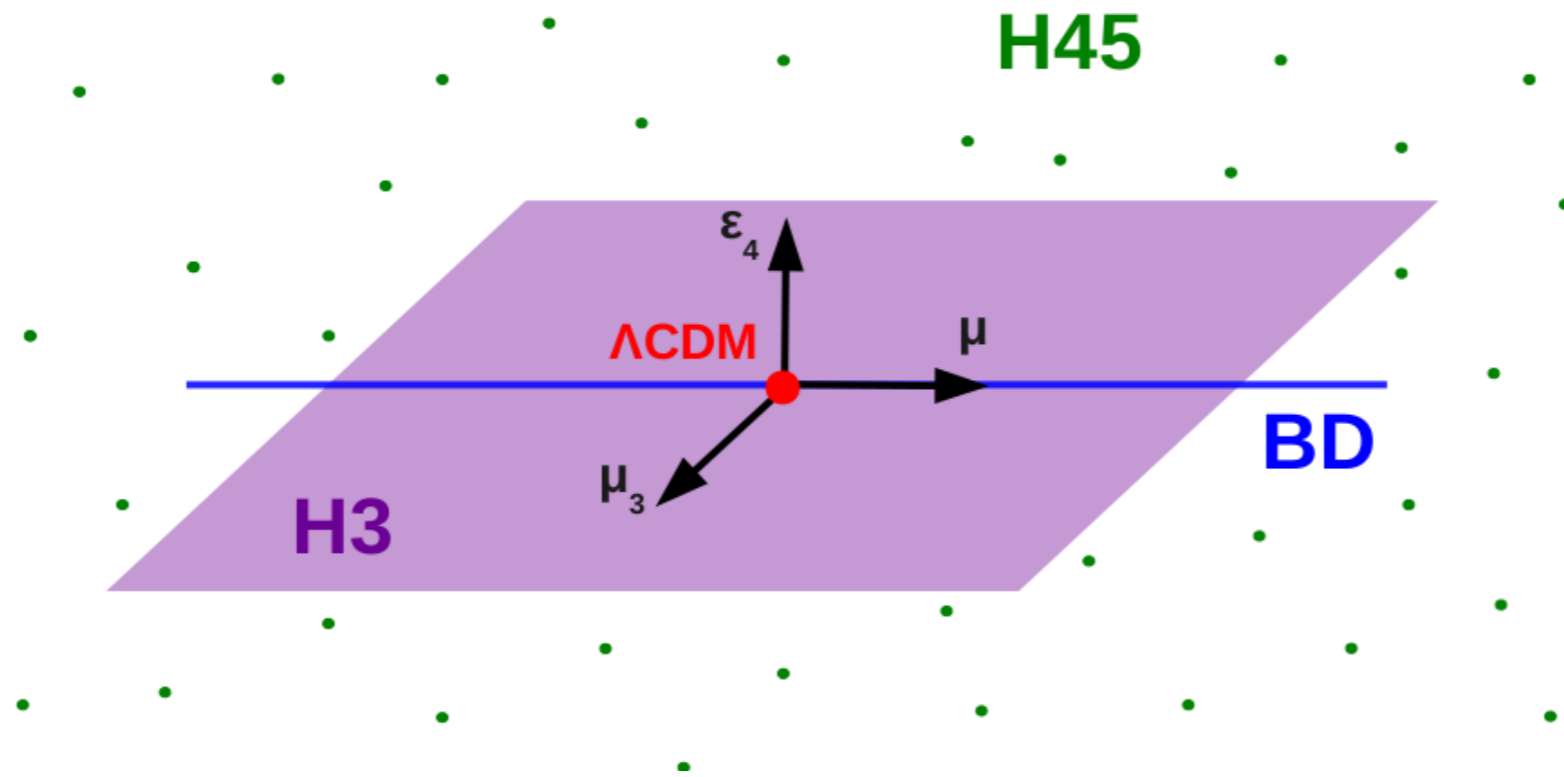
Newtonian gauge: scalar d.o.f.: Φ, Ψ, π



‘Observables’ in the perturbation sector:
effective Newton constant and gravitational slip parameter

$$-\frac{k^2}{a^2}\Phi = 4\pi G_{\text{eff}}[\mu, \mu_3, \epsilon_4](t) \rho_m \delta_m$$

$$\frac{\Psi}{\Phi} = \gamma[\mu, \mu_3, \epsilon_4](t)$$



The space of theories: not so smooth...

Stability conditions

$$S_\pi = \int a^3(t) M^2(t) \left[A(\mu, \mu_2^2, \mu_3, \epsilon_4) \dot{\pi}^2 + B(\mu, \mu_3, \epsilon_4) \frac{(\vec{\nabla}\pi)^2}{a^2} \right] + \text{lower order in derivatives.}$$

↑
No ghost: $A > 0$

↑
No gradient instabilities: $B < 0$

Stability conditions

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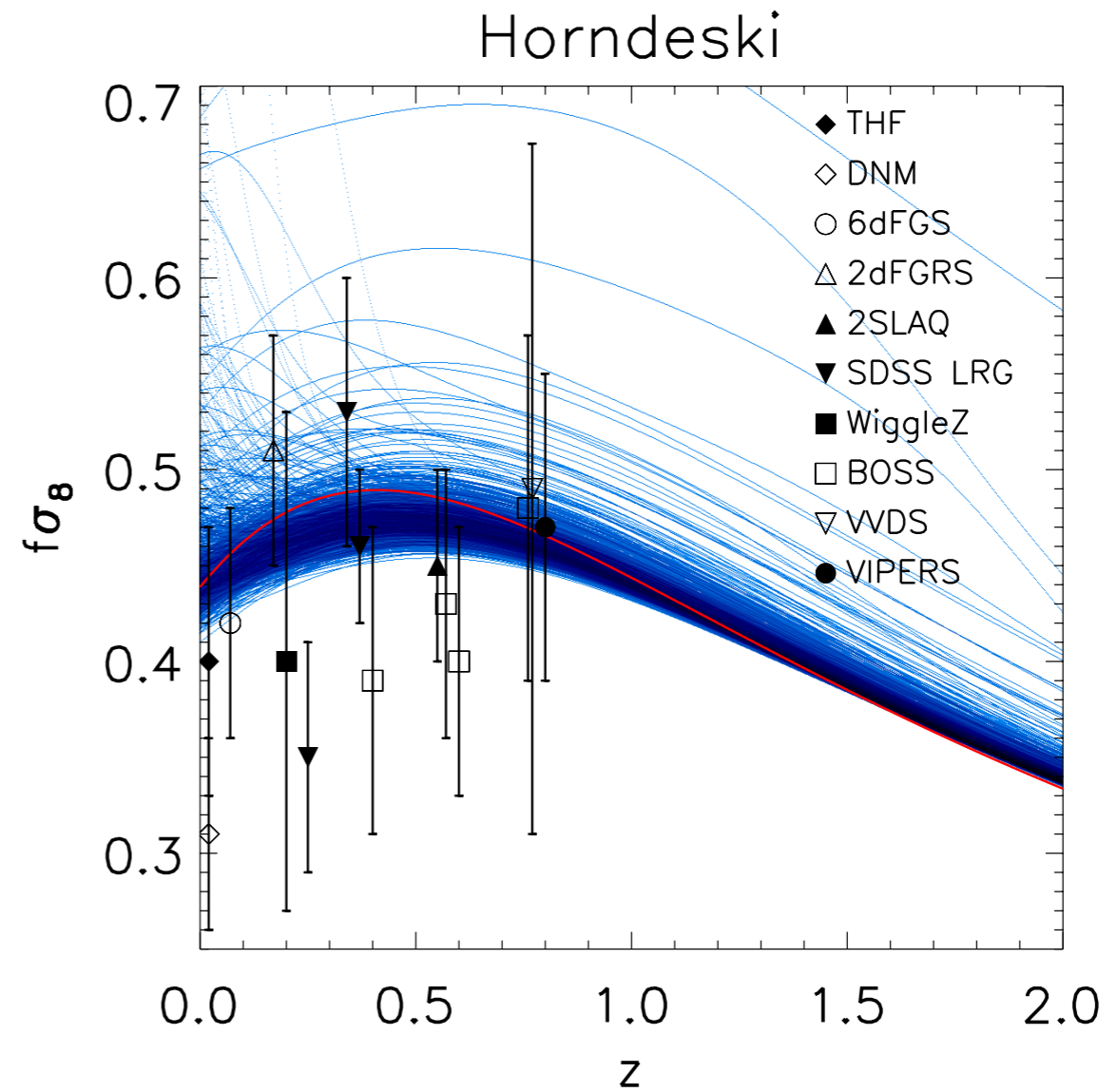
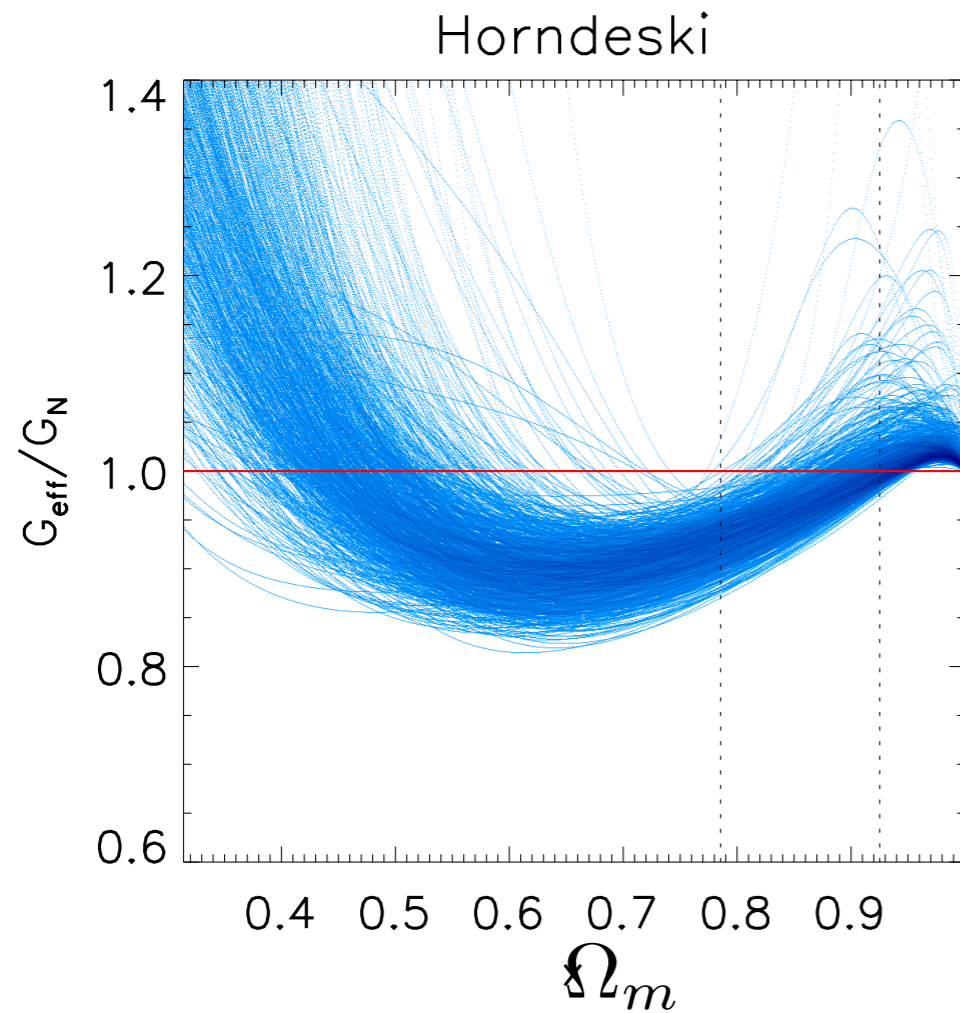
Basic requirement

Option 1: $c_s^2 < 1$

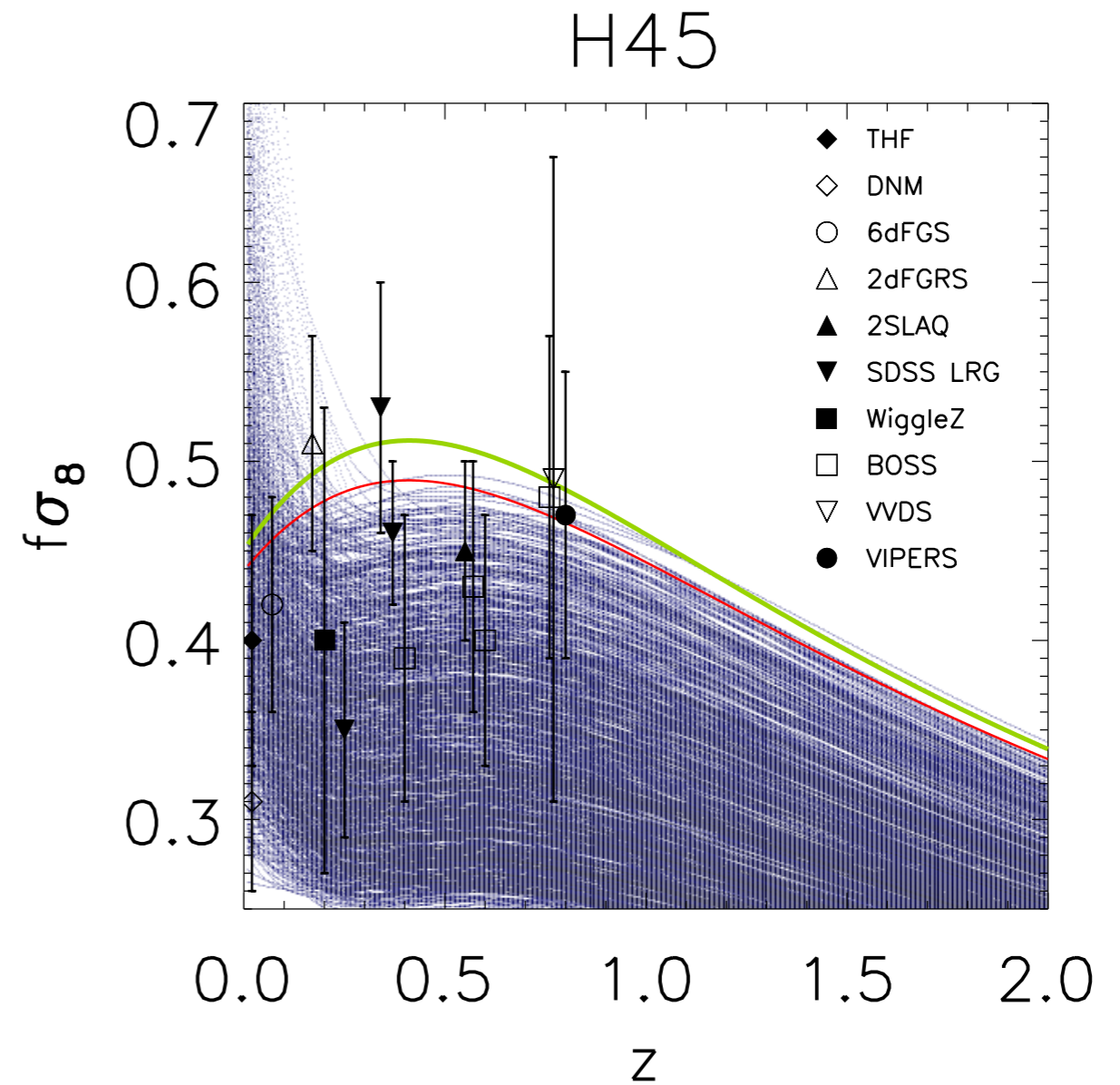
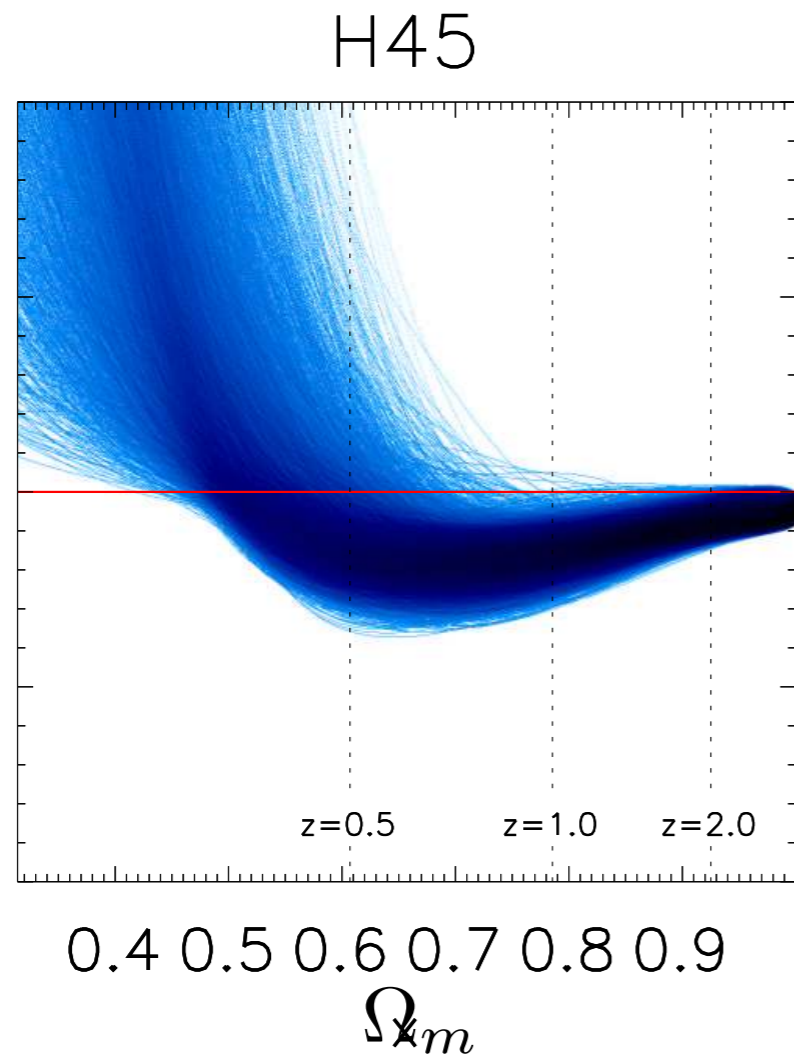
Option 2: $c_T^2 < 1$

Stability requirements make a strong selection

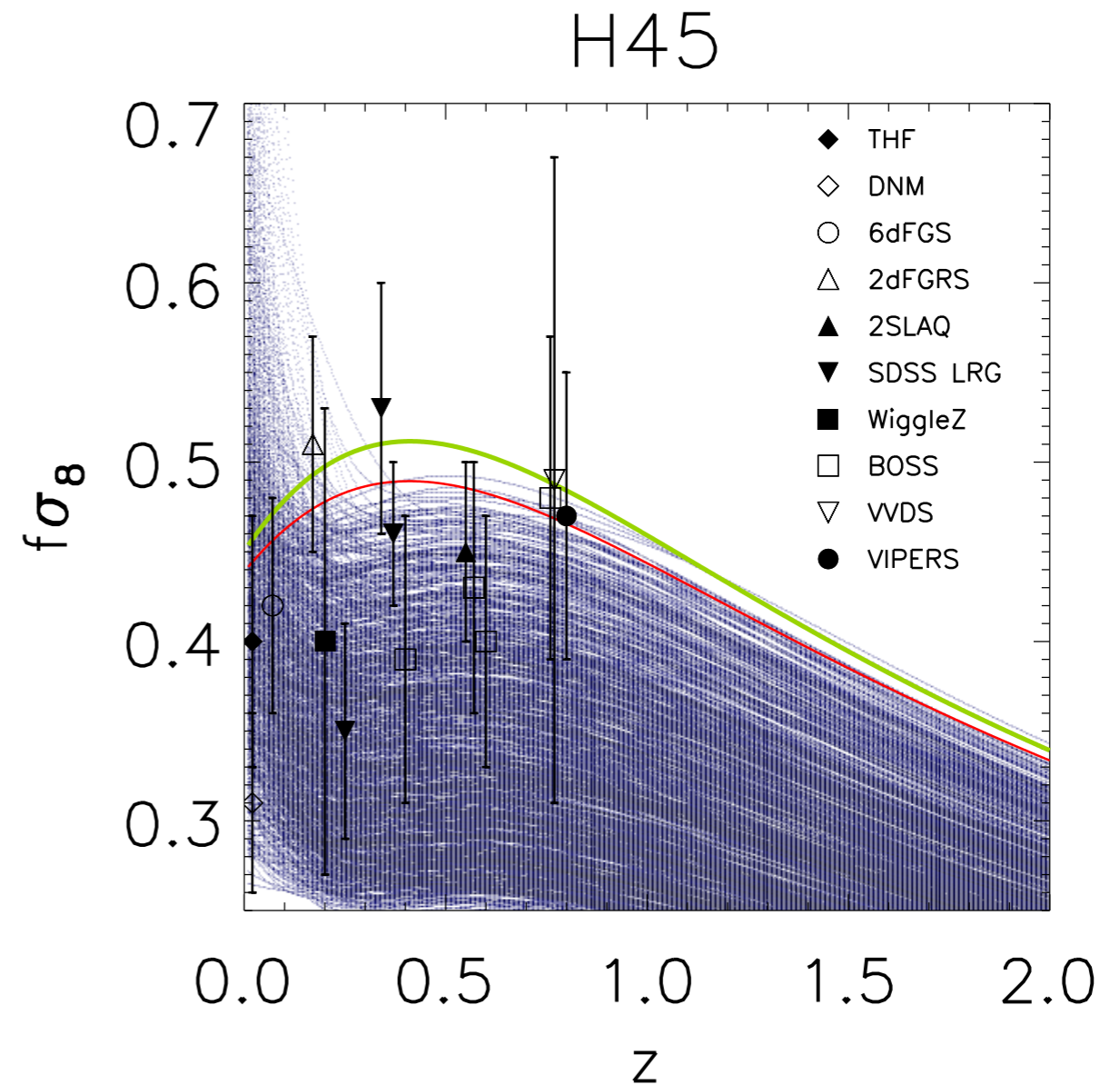
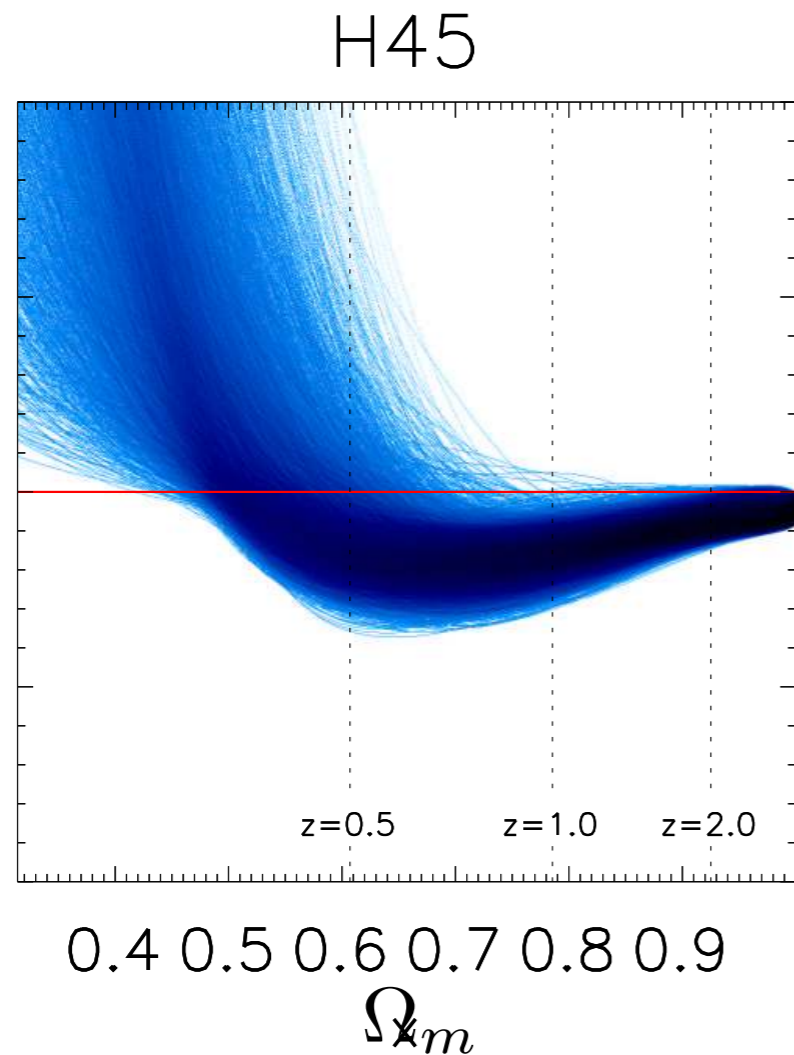
Growth rate



Growth rate (early DE)



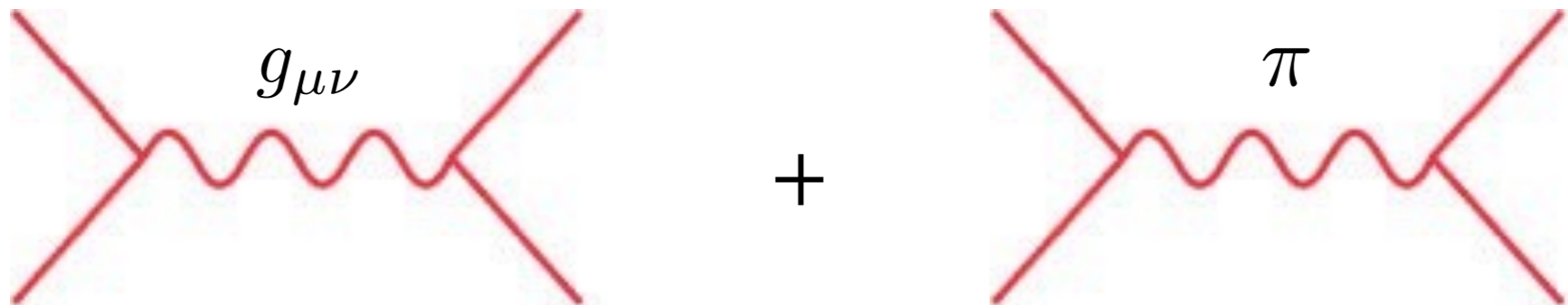
Growth rate (early DE)



Strong implications on CMB data fitting (Valentina's talk)

Protecting solar system gravity with screening

$$\mathcal{L} = -\frac{M_*^2}{2} h_{\mu\nu} \mathcal{E}^{\mu\nu}_{\alpha\beta}[\phi_0] h^{\alpha\beta} - \mathcal{A}^{\mu\nu}[\phi_0] \partial_\mu \pi \partial_\nu \pi - \pi T + \frac{1}{2} h^{\mu\nu} T_{\mu\nu}$$

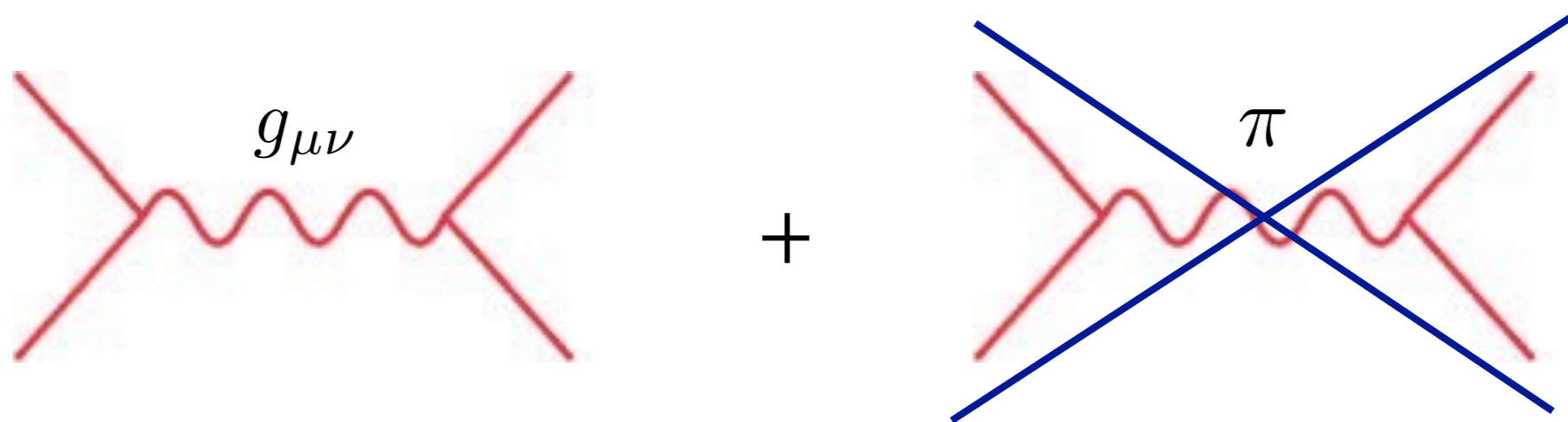


On cosmic scale the scalar contributes $O(1)$

We need screening!

Vainshtein screening

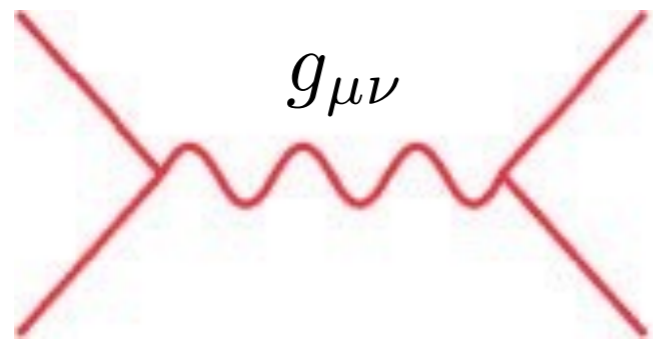
$$\mathcal{L} = -\frac{M_*^2}{2} h_{\mu\nu} \mathcal{E}^{\mu\nu}_{\alpha\beta}[\phi_0] h^{\alpha\beta} - \mathcal{A}^{\mu\nu}[\phi_0] \partial_\mu \pi \partial_\nu \pi - \pi T + \frac{1}{2} h^{\mu\nu} T_{\mu\nu}$$



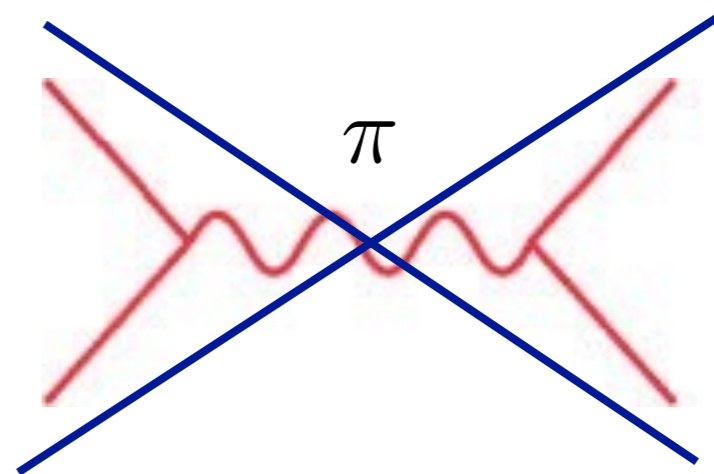
Vainshtein: non-linear effects suppress the scalar contribution

Vainshtein screening

$$\mathcal{L} = -\frac{M_*^2}{2} h_{\mu\nu} \mathcal{E}_{\alpha\beta}^{\mu\nu}[\phi_0] h^{\alpha\beta} - \mathcal{A}^{\mu\nu}[\phi_0] \partial_\mu \pi \partial_\nu \pi - \pi T + \frac{1}{2} h^{\mu\nu} T_{\mu\nu}$$



+



Vainshtein: non-linear effects suppress the scalar contribution

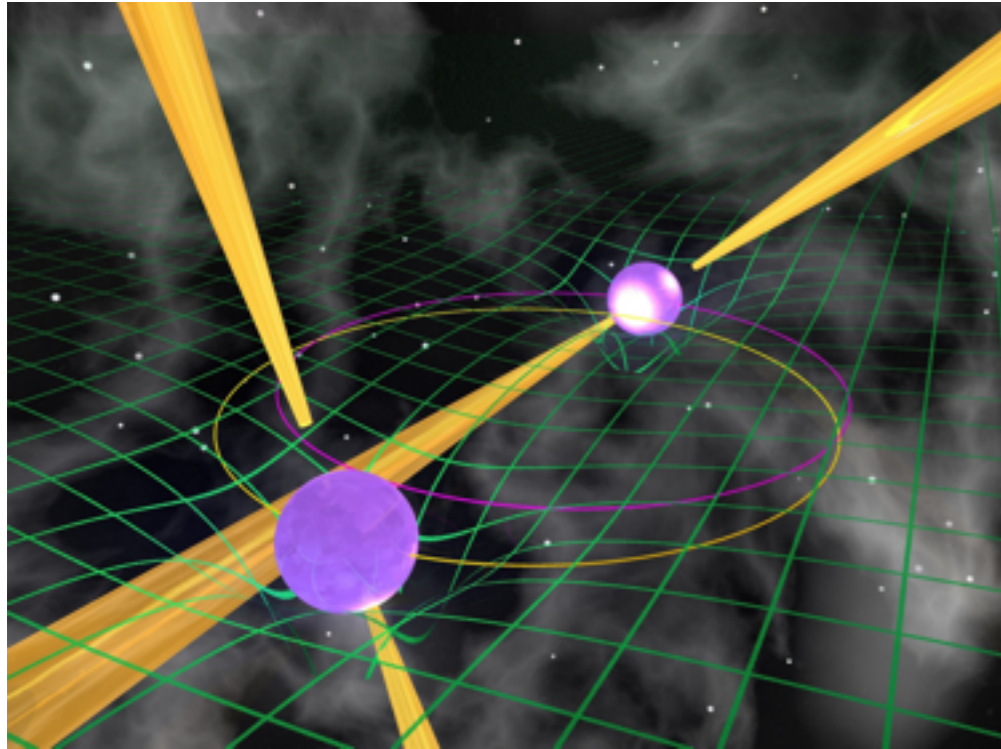
However: there can be modifications in the pure-graviton sector.
These are, generally, unscreenable!

Babichev, Deffayet, Esposito-Farese 2012

Beltran, F.P., Velten, 2015

Gravitational wave speed (as in heaven as on hearth)

J. Beltran, F.P., H. Velten, 2015

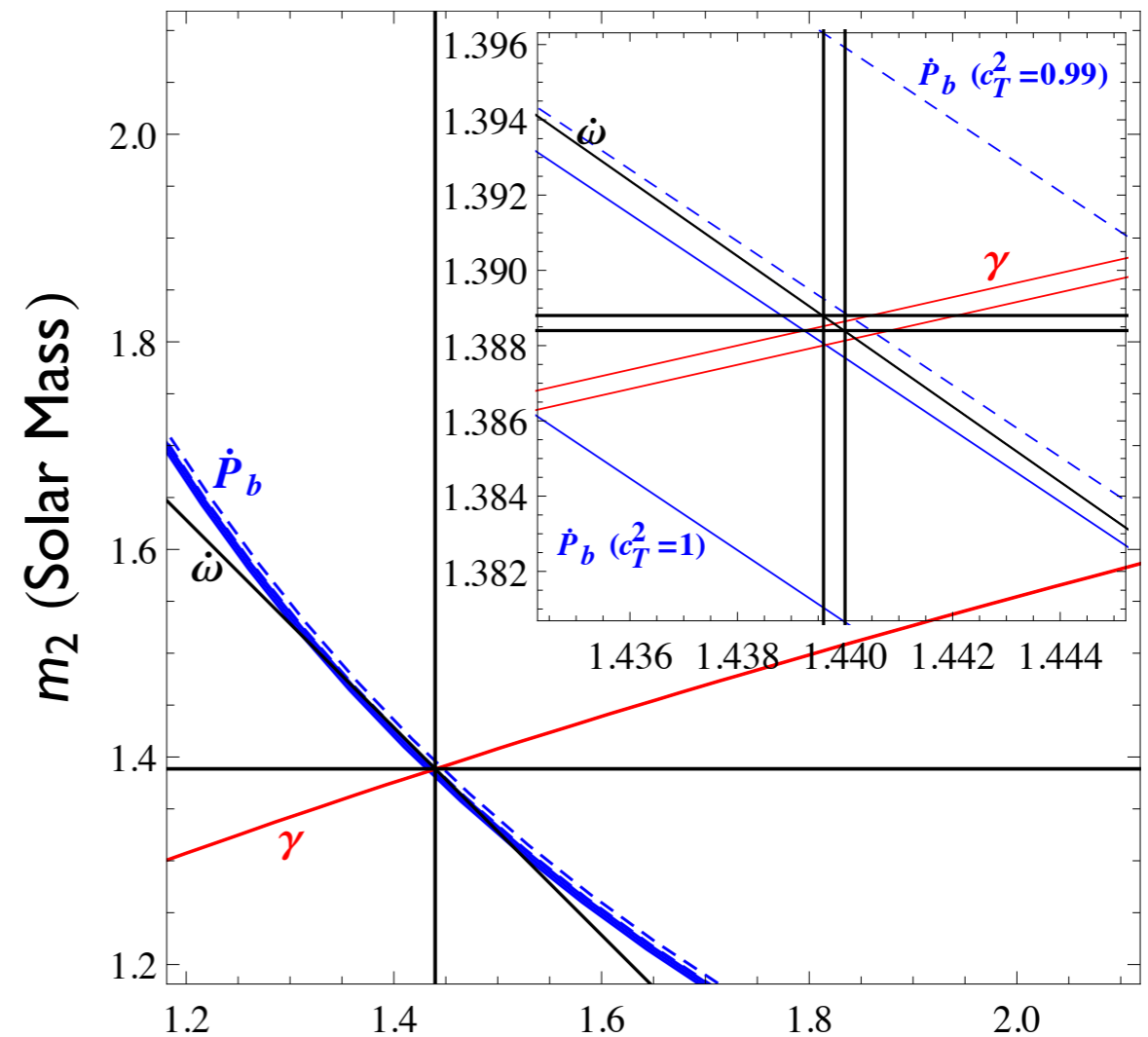


Hulse-Taylor
binary pulsars

$$c_T^2 = \frac{1}{1 + \epsilon_4}$$

$$\epsilon_4 \lesssim 10^{-2}$$

See also Blas, Sanctuary 2011



Gravitational wave speed (as in heaven as on earth)

J. Beltran, F.P., H. Velten, 2015

A question of timing...

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LES

Statistical and Quantum
Information, etc.

Astrophysics

Fields and Fields

Acoustics, and Optical Physics

Fluid Dynamics,
etc.

Classical Physics

Structure, etc.

Electronic Properties,

Particle, Biological, and
Physics

Gravitation and Astrophysics

Evading the Vainshtein Mechanism with Anomalous Gravitational Wave Speed: Constraints on Modified Gravity from Binary Pulsars

PDF

HTML

Jose Beltrán Jiménez, Federico Piazza, and Hermano Velten
Phys. Rev. Lett. **116**, 061101 (2016) – Published 9 February 2016

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Featured in Physics

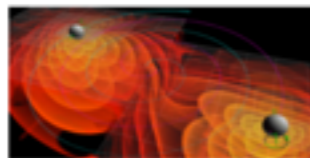
Editors' Suggestion

PDF

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Observation of Gravitational Waves from a Binary Black Hole Merger

B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration)
Phys. Rev. Lett. **116**, 061102 (2016) – Published 11 February 2016



Gravitational waves emitted by the merger of two black holes
have been detected, setting the course for a new era of
observational astrophysics.

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The condition MG's condition is in...



$$G_N \sim \frac{1}{8\pi M^2(t_0)[1 + \epsilon_4(t_0)]^2}$$

$$\frac{\dot{G}_N}{G_N} < 0.02H_0 \quad (\text{Lunar Laser Ranging})$$

self-acceleration

$$H^2 = \frac{1}{3M^2(t)} [\rho_m(t) + \rho_{DE}(t)]$$

An arrow points from the text "self-acceleration" to the coefficient '1' in the numerator of the Friedmann equation above.

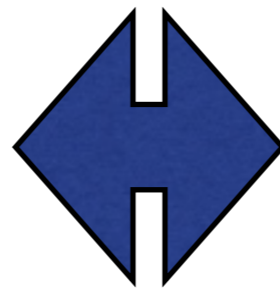
Final remarks

- EFT of DE powerful unifying framework
- Loads of new data from future Galaxy surveys
- Lot of data-fitting work ahead of us

Either

Tension persisting and eased by MG

or...



Bruxelles 22/03/2016



KEEP ON
ROCKING
IN THE
FREE
WORLD!