



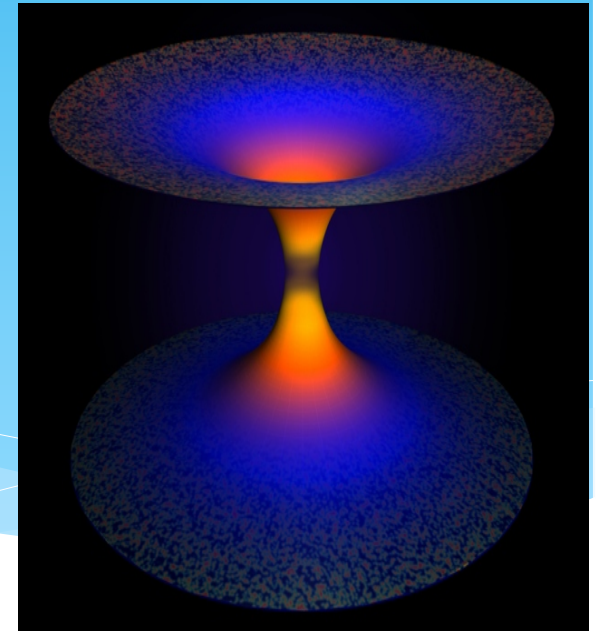
Gravitational Waves in Bouncing Cosmology

(1604.xxxxx)

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Rencontres de Moriond



Motivation I:

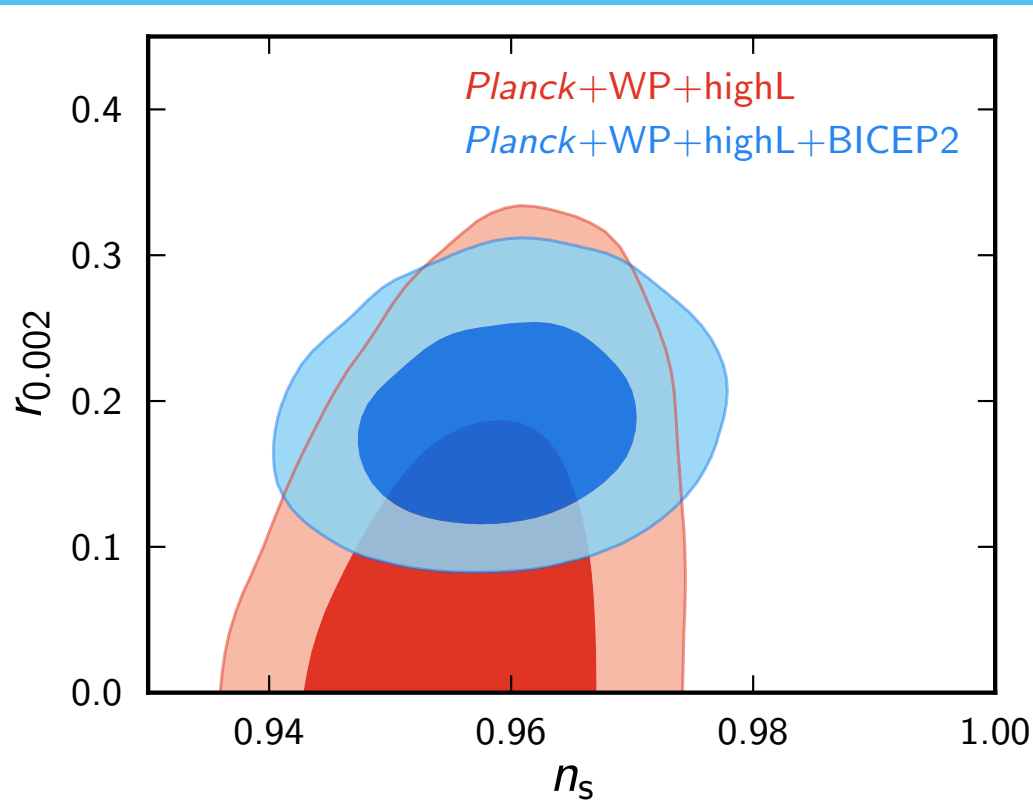
**Inflation is geodesically
past incomplete!**

New Physics is necessary!

Some NP discards inflation

=> Bouncing Cosmology

Motivation II: Moriond 2014



Aim:

**Can We Get Observable
Gravitational Waves on
CMB Scales in a Bouncing
Cosmology?**

Idea:

Coupling to Gauge Fields

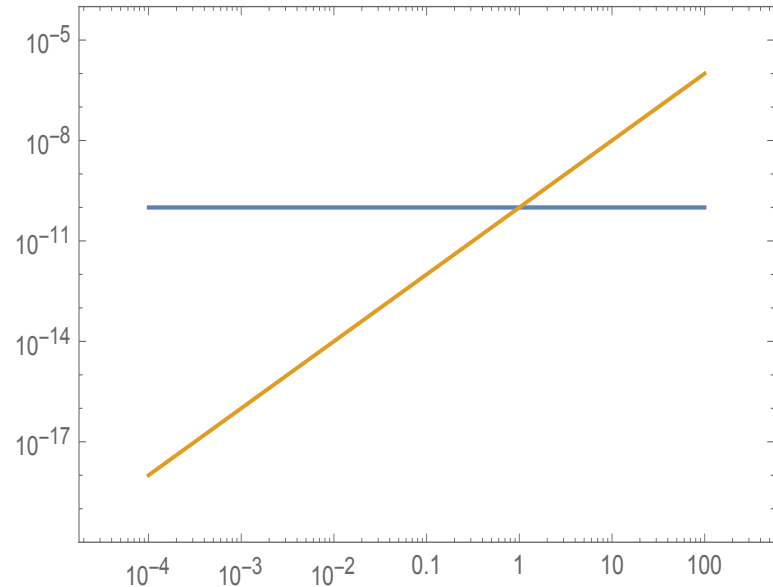
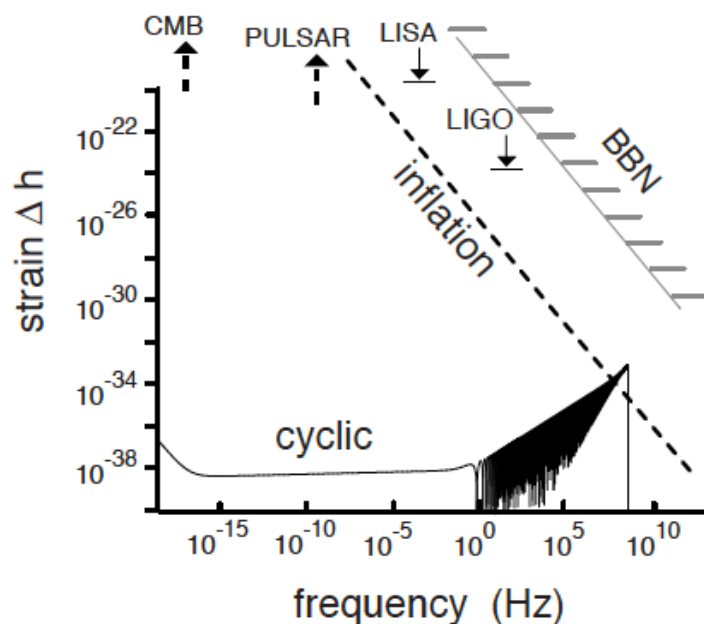
Problem: Blue Spectrum

$$a = a_0(-\tau)^b \Rightarrow \mathcal{P}_{vac.} \sim k^{2+2b}$$

Inf. : $b = -1$, *Bounce* : $0 < b \ll 1$

* Present Day Strain: $\sim P^{1/2}$

* Primordial



Updated Constraints: Meerburg et al. 2015

Early Universe Cosmology

Inflation

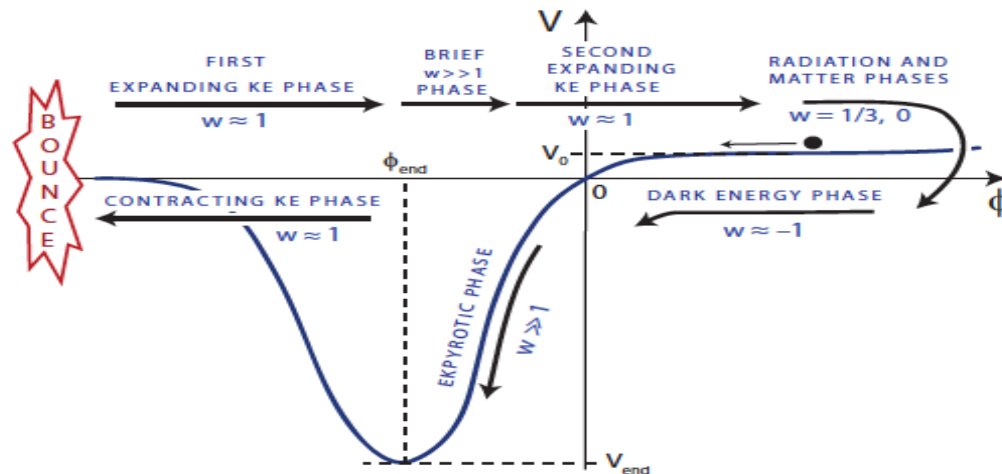
- * Universe **expands exponentially** $\sim dS$ space
- * Isotropy & Homogeneity
- * Vacuum fluctuations generate spectra
- * Nearly scale inv. scalar spectrum
- * **Nearly scale inv. GW spectrum**
- * **Geodesically Incomplete**

Bounce

- * Universe **slowly contracts towards Minkowski space**
- * Isotropy & Homogeneity
- * Vacuum fluctuations generate spectra
- * Nearly scale inv. scalar spectrum* (2-fields).
- * **Blue GW spectrum**
- * **Violates Null Energy Condition**

Brief History of Time

- * **Universe slowly contracts. $b \ll 1$.** Isotropizes and flattens! Vacuum fluctuations generate spectra
- * **Kinetic Energy Dominated Contraction. ($b=1/2$)**
- * **BOUNCE!** (H flips sign), No Big Bang singularity
- * **Kinetic Energy Dominated Expansion. ($b=1/2, \tau > 0$)**
- * **Standard Hot Big Bang.**



$$a = a_0 (-\tau)^b$$

Coupling to Gauge Fields

- * Controlled Backreaction.
- * Inflation (Barnaby, Peloso, Sorbo, Silverstein...) – GW regardless of the energy scale of inflation. (See V. Domcke's talk)
- * Exponential enhancement of gauge quanta - inflaton/ ekpyrosis generate additional spectra via inverse decays!
- * Uncorrelated with vacuum fluct.

$$\mathcal{S}_1 = \int d^4x \sqrt{-g} \left[\frac{M_p^2}{2} R - \frac{1}{2} (\partial\varphi_1)^2 - V(\varphi_1) - \frac{1}{4} F^{\mu\nu} F_{\mu\nu} - \frac{\alpha}{4f} \varphi_1 \tilde{F}^{\mu\nu} F_{\mu\nu} \right]$$
$$\mathcal{S}_2 = \int d^4x \sqrt{-g} \left[\frac{M_p^2}{2} R - \frac{1}{2} (\partial\varphi_1)^2 - V(\varphi_1) - (-\tau)^{-2n} \left\{ \frac{1}{4} F^{\mu\nu} F_{\mu\nu} - \frac{\gamma}{4} \tilde{F}^{\mu\nu} F_{\mu\nu} \right\} \right]$$

Solutions for GW with a Source

- * Valid for all FLRW cosmologies (Inflation ($b=-1$), matter($b=2$), ekpyrotic ($b \ll 1$) ...)
- * Various “magnetic field” tilt!
- * h- GW pert., J – source, A- gauge fluc.

$$\left[\partial_{\tau}^2 + \left(k^2 - \frac{a''}{a} \right) \right] \frac{h_{\lambda}}{a} \left(\tau, \vec{k} \right) = \overset{\text{SOURCE TERM}}{\downarrow} J_{\lambda} \left(\tau, \vec{k} \right)$$

$$J_{\lambda} \sim \tilde{A}^2$$

Model 2: constant ξ

$$\tilde{A}_{\sigma}(k, \tau) \simeq \sqrt{-\frac{\tau}{2\pi}} e^{\pi\xi} \Gamma(|2n+1|) |2\xi k \tau|^{-|n+1/2|}$$

Enhancement of fluctuations

- * The gauge quanta and hence the GW are exponentially enhanced
- * Non-gaussian.
- * Only the + helicity is enhanced.
- * No dependence on the tilt of the gauge fields! n drops out!

$$h \sim A^2 \sim e^{2\pi\xi}$$

$$P_T^{total} \equiv \frac{k^3}{2\pi^2} \langle \hat{h}_\lambda(\vec{k}) \hat{h}_{\lambda'}(\vec{k}') \rangle = \frac{4k^{2+2b}}{\pi^2 M_{pl}^2 k_0^{2b}} \left[1 + 4.1 \times 10^{-7} \frac{e^{4\pi\xi} k^{1+2b} H_{ek.-end}}{\xi^2 \underline{M_{pl}^2 k_0^{2b}}} \right]$$

$$\xi > 3 \Rightarrow P_T \sim k^{3+4b} H_{end}$$