

Invariants and Flavour

in the general Two Higgs

Doublet Model

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Two Higgs doublet models (2HDM)

## Several Motivations

- New sources of CP violation  
SM cannot account for BAV
  - Possibility of having spontaneous CP violation  
EW sym breaking and CP same footing  
T.D. Lee 1973 ; Kobayashi and Maskawa 1973
  - Peccei Quinn type solution to CP strong
  - Supersymmetry
- LHC important role

Notation

Yukawa interactions

$$\mathcal{L}_Y = -\bar{Q}_L^0 \Gamma_1 \Phi_1^T d_R^0 - \bar{Q}_L^0 \Gamma_2 \Phi_2^T d_R^0 - \bar{Q}_L^0 \Delta_1 \tilde{\Phi}_1^T u_R^0 - \bar{Q}_L^0 \Delta_2 \Phi_2^T u_R^0 + h.c.$$
$$\Phi_L = -i\tau_2 \Phi_L^*$$

Quark mass matrices

$$M_d = \frac{1}{\sqrt{2}} (\sqrt{1} \Gamma_1 + \sqrt{2} e^{i\alpha} \Gamma_2); \quad M_u = \frac{1}{\sqrt{2}} (\sqrt{1} \Delta_1 + \sqrt{2} e^{-i\alpha} \Delta_2)$$

Diagonalised by

$$U_{dL}^T M_d U_{dR} = D_d \equiv \text{diag} (m_d, m_s, m_b)$$

$$U_{uL}^T M_u U_{uR} = D_u \equiv \text{diag} (m_u, m_c, m_t)$$

Expansion around the vev's

$$\Phi_j = v e^{i\alpha_j} \begin{pmatrix} \phi_j^+ \\ \frac{1}{\sqrt{2}} (\sigma_j + \rho_j + i\eta_j) \end{pmatrix} \quad j=1,2$$

We perform the following transformation

$$\begin{pmatrix} H^0 \\ R \end{pmatrix} = 0 \begin{pmatrix} \rho_1 \\ \rho_2 \end{pmatrix} ; \quad \begin{pmatrix} G^0 \\ I \end{pmatrix} = 0 \begin{pmatrix} \eta_1 \\ \eta_2 \end{pmatrix} ; \quad \begin{pmatrix} G^+ \\ H^+ \end{pmatrix} = 0 \begin{pmatrix} \phi_1^+ \\ \phi_2^+ \end{pmatrix}$$

$$0 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sigma_1 & \sigma_2 \\ \sigma_2 & -\sigma_1 \end{pmatrix} ; \quad \sqrt{2} = \sqrt{\sigma_1^2 + \sigma_2^2} = (\sqrt{2} G_F)^{-1/2} \approx 246 \text{ GeV}$$

$O$  angles out

$H^0$  with couplings to quarks proportional to mass matrices

$G^0$  the neutral pseudo-goldstone boson

$G^+$  charged pseudo-goldstone boson

Physical neutral Higgs fields are combination of  $H^0$ ,  $R$  and  $I$

## Neutral and charged Higgs interactions for the quark sector

$$\begin{aligned}
 \mathcal{L}_Y(\text{quark}, \text{Higgs}) = & -\bar{d}_L^0 \frac{1}{\sqrt{2}} (M_d H^0 + N_d^0 R + i N_d^0 I) d_R^0 + \\
 & + \bar{u}_L^0 \frac{1}{\sqrt{2}} [M_u H^0 + N_u^0 R + i N_u^0 I] u_R^0 + \\
 & + \frac{\sqrt{2} H^+}{\sqrt{2}} (\bar{u}_L^0 N_d^0 d_R^0 - \bar{u}_R^0 N_u^0 d_L^0) + \text{h.c.}
 \end{aligned}$$

$$N_d^0 = \frac{1}{\sqrt{2}} (\sqrt{2} \Gamma_1 - \nu_1 e^{i\alpha} \Gamma_2), \quad N_u^0 = \frac{1}{\sqrt{2}} (\sqrt{2} - \nu_1 e^{-i\alpha} \Delta_2)$$

Flavor structure of quark sector of ZHDM characterized by

$$M_d, M_u, N_d^0, N_u^0$$

leptonic sector, Dirac neutrinos

$$M_e, M_\nu, N_e^0, N_\nu^0$$

Yukawa couplings in terms of quark mass eigenstates  
for  $H^+$ ,  $H^0$ ,  $R$ ,  $I$

$$\begin{aligned}
 \mathcal{L}_Y = & \dots \sqrt{2} \frac{H^+}{\sqrt{2}} \bar{u} (-v N_d \gamma_R + N_u^+ v \gamma_L) d + \text{h.c.} - \\
 & - \frac{H^0}{\sqrt{2}} (\bar{u} D_u u + \bar{d} D_d d) - \\
 & - \frac{R}{\sqrt{2}} [\bar{u} (N_u \gamma_R + N_u^+ \gamma_L) u + \bar{d} (N_d \gamma_R + N_d^+ \gamma_L) d] + \\
 & + i \frac{I}{\sqrt{2}} [\bar{u} (N_u \gamma_R - N_u^+ \gamma_L) u - \bar{d} (N_d \gamma_R - N_d^+ \gamma_L) d]
 \end{aligned}$$

$$\gamma_L = (1 - \gamma_5)/2; \quad \gamma_R = (1 + \gamma_5)/2 \quad V \equiv V_{CKM}$$

Flavour changing neutral currents controlled by:

$$N_d = \frac{1}{\sqrt{2}} U_{dL}^\dagger (\sqrt{2} \Gamma_1 - \nu_1 e^{i\alpha} \Gamma_2) U_{dR}$$

$$N_u = \frac{1}{\sqrt{2}} U_{uL}^\dagger (\sqrt{2} \Delta_1 - \nu_1 e^{-i\alpha} \Delta_2) U_{uR}$$

For generic two Higgs doublet models

$N_u, N_d$  non-diagonal arbitrary

For definiteness rewrite  $N_d$ :

$$N_d = \frac{\sqrt{2}}{\nu_1} D_d - \frac{\sqrt{2}}{\sqrt{2}} \left( \frac{\nu_2}{\nu_1} + \frac{\nu_1}{\sqrt{2}} \right) U_{dL}^\dagger e^{i\alpha} \Gamma_2 U_{dR}$$

→  
controls flavour

→  
leads to FCNC

Models with two or more Higgs doublets

potentially large HFNC

## Strict experimental limits on FCNC processes!

In the SM, FCNC are only generated at loop level

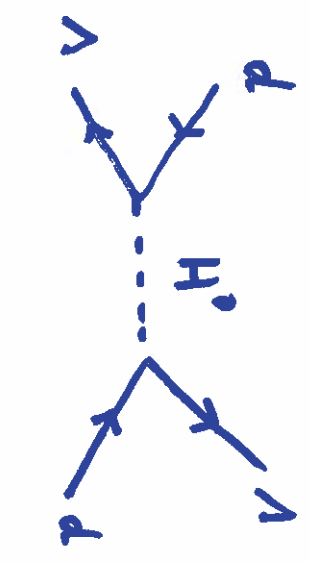
⇒ very suppressed

Processes that play a crucial role in testing the SM and putting limits on Physics BSM:

- $K^0 - \bar{K}^0$  mixing
- $D^0 - \bar{D}^0$  mixing
- $B_d^0 - \bar{B}_d^0$  mixing
- $B_s^0 - \bar{B}_s^0$  mixing

rare Kaon decays  
rare B-meson decays

CP violation



$K_L - K_S$  mass difference  
 $m_H \gtrsim 1 \text{ TeV}$

CP violation  $\epsilon_K$   
 $m_H \gtrsim 30 \text{ TeV}$



Proposed solutions, case of Multi-Higgs models

NFC

Wenberg, Glashow (1977)

or

Paschos (1977)

existence of suppression factors in HFVNC

Antaramian, Hall, Rawn (1992)

Hall, Wenberg (1993)

Yoshimura, Rindani (1991)

First models of this type with no ad-hoc assumptions suppression by small elements of

VEKM : BGL models

Branes, Gumm, Lavoura (1996)

More recently, we have generalized BGL models to larger class of models of "Minimal Flavour Violation" type

The flavour structure of Yukawa couplings is not constrained by gauge invariance

All flavour changing transitions in SM are mediated by charged weak currents with flavour mixing controlled by  $V_{CKM}$

MFV essentially requires flavour and CP violation linked to known structures of Yukawa couplings

[all new flavour changing transitions are controlled by the CKM matrix]

## About Minimal Flavour Violation

Buras, Gambhir, Gorbahn, Jager, Salvendy (2001)  
D'Ambrosio, Giudice, Jagger, Strumia (2002)

### Leptonic sector

Coregiani, Gumbren, Jagger, Wae (2005)

$G_F = U(3)^5$  largest symmetry of the gauge sector  
flavour violation completely determined by Yukawa couplings

### Our framework

- multi-Higgs models
- no Natural Flavour Conservation
- obey above condition (one of the defining ingredients of MFV framework)

"Higgs-mediated FCNC's: Natural Flavour Conservation vs.

### Minimal Flavour Violation"

Buras, Ciuchci, Gori, Jagger, arXiv:1005.5310 (JHEP)  
Barbieri, Lodone, Strass, Jona-Purga; Cervoni, Gerard; ...

In order to obtain a structure for  $\Gamma_i$ ,  $\Delta_i$  such that FCNC at tree level strength completely controlled Yukawa Brauno, Gurus, Lorena imposed symmetry

$$Q_{Lj}^{\circ} \rightarrow \exp(iZ) Q_{Lj}^{\circ} ; U_{Rj}^{\circ} \rightarrow \exp(2iZ) U_{Rj}^{\circ} ; \Phi_2 \rightarrow \exp(iZ) \Phi_2, \tau \neq 0, \pi$$

$$\Gamma_1 = \begin{pmatrix} \times & \times & \times \\ \times & \times & \times \\ 0 & 0 & 0 \end{pmatrix} ; \Gamma_2 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ \times & \times & \times \end{pmatrix} ; \Delta_1 = \begin{pmatrix} \times & \times & 0 \\ \times & \times & 0 \\ 0 & 0 & 0 \end{pmatrix} ; \Delta_2 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & \times \end{pmatrix}$$

$l=3$

Both Higgs have non-zero Yukawa couplings in the up and down sector

Special WB shown by the symmetry

FCNC in down sector

$$\text{if instead of } U_{Rj}^{\circ} \rightarrow \exp(2iZ) U_{Rj}^{\circ} \text{ impose } d_{Rj}^{\circ} \rightarrow \exp(2iZ) d_{Rj}^{\circ}$$

then FCNC in up sector

# WB invariant definition

$$M_d^0 = \frac{\sqrt{2}}{\sqrt{1}} M_d - \left( \frac{\sqrt{2}}{\sqrt{1}} + \frac{\sqrt{1}}{\sqrt{2}} \right) \mathcal{P}_f^{\delta} M_d$$

$$M_u^0 = \frac{\sqrt{2}}{\sqrt{1}} M_u - \left( \frac{\sqrt{2}}{\sqrt{1}} + \frac{\sqrt{1}}{\sqrt{2}} \right) \mathcal{P}_f^{\delta} M_u$$

together with

$$\mathcal{P}_f^{\delta} \Gamma_2 = \Gamma_2, \quad \mathcal{P}_f^{\delta} \Gamma_1 = 0$$

$$\mathcal{P}_f^{\delta} \Delta_2 = \Delta_2, \quad \mathcal{P}_f^{\delta} \Delta_1 = 0$$

$\delta$  stands for u (up) or d (down)

$\mathcal{P}_f^{\delta}$  are projection operators

Bohalla, Nisot, Vuon 2004

$$\mathcal{P}_f^u = U_{uL} P_f U_{uL}^{\dagger}$$

$$\mathcal{P}_f^d = U_{dL} P_f U_{dL}^{\dagger}$$

$$(P_f)_{jk} = \delta_{jl} \delta_{lk}$$

e.g.  $P_3 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$

# Flavour structure

$$M_d, M_u, N_d^0, N_u^0$$

Freedom of choice of WB  $\Rightarrow$  Work with WB invariants  
Zero textures are WB dependent

Above four matrices encode breaking of flavour sym  
present in gauge sector

Large redundancy of parameters

WB transformations do not change the physics

Examples of WB invariants:  $\text{tr}(H_u H_d)$ ,  $\text{tr}(H_u H_d^2)$   
 $\text{tr}(H_u^2 H_d)$ ,  $\text{tr}(H_u^2 H_d^2) \rightarrow Y_{CKM}$  ambiguity  
in sign  $\sum_m Q$ ,  $Q_{diff} = Y_{\alpha i} Y_{\beta j} V_{\alpha j}^* V_{\beta i}^*$  ( $\alpha \neq \beta$ ), ( $i \neq j$ )

Branco, Lavoura, 1988

WB also very useful to study CP violation

$$I_1^{CP} \equiv \text{tr} [H_u, H_d]^3 = 6i (m_t^2 - m_c^2) (m_b^2 - m_u^2) (m_s^2 - m_d^2) \times \\ \times (m_g^2 - m_\lambda^2) (m_g^2 - m_d^2) (m_\lambda^2 - m_d^2) \text{Tr } Q_{\text{weak}}$$

Bornhauser, Branco, Gounaris 1986

$\det [H_u, H_d]$  Jarvikog, 1985 3 generations

One can check predictions of flavor model comparing invariant quantities with their corresponding experimental values

In 2HDM one can build new WB invariants which do not occur SM

Special WB's  $N_d$  diagonal,  $N_d^0 = N_d$   
or  $N_u$  diagonal,  $N_u^0 = N_u$

Examples

$$V_{CKM} \equiv U_{uL}^\dagger U_{dL}$$

$$I_1 \equiv \text{tr} (M_d N_d^{0\dagger}) = m_d (N_d^{0\dagger})_{11} + m_s (N_d^{0\dagger})_{22} + m_b (N_d^{0\dagger})_{33}$$

not sensitive to HFNC  
 $\sum_m I_1$  probes phases of  $(N_d)_{ij}$  (electric dipole moment of quarks)

$$I_2 \equiv \text{tr} [M_d N_d^0, M_d M_d^\dagger]^2 \text{ sensitive to off-diag elements } N_d$$

$$I_1^{\text{CP}} \propto \sum_m \text{Im} \text{Quark}, \quad V_{\text{CKM}} = U_{UL}^\dagger U_{dL}$$

$U_{uL} \neq U_{dL}$  misalignment of the matrices  $H_d, H_u$

analogously

$$I_3^{\text{CP}} \equiv \text{tr} [H_d, H_u^0]^3 = 6i \Delta_d \Delta_u \text{Im} \theta_3, \quad V_3 \equiv U_{dL}^\dagger U_{uL}^0$$

$$H_{Nd}^0 = N_d^0 N_d^{0\dagger}$$

$$I_2^{\text{CP}} \equiv \text{tr} [H_u, H_{Nd}^0]^3 = 6i \Delta_u \Delta_{Nd} \text{Im} \theta_2, \quad V_2 = U_{uL}^\dagger U_{NdL}^0$$

$$I_6^{\text{CP}} \equiv \text{tr} [H_{Nd}^0, H_{Nu}^0]^3$$

and many more

$V_{\text{CKM}}, V_2, V_3$  signal misalignment in flavor space of Hermitian matrices constructed in the framework of ZHDM



So far, we have only written invariants which are sensitive to left-handed mixings

One can construct analogous invariants which are sensitive to right-handed mixings, like:

$$I_7^{CP} \equiv \text{Tr} [H_d^i, H_{Nd}^i]_3^3 = 6i \Delta_d \Delta_{Nd} \text{Im } Q_7$$

$$H_d^i = M_d^\dagger M_d, \quad H_{Nd}^i = N_d^{\dagger 0} N_d^0$$

$Q_7$  rephasing invariant quartet of  $U_{dR} U_{dR}^\dagger$

and again many more

# The Minimal Flavour Violation case

Lowest invariant sensitive to CP violation

$$I_9^{CP} = \text{Im} \text{tr} [ M_d N_d^{\dagger} M_d M_d^{\dagger} M_u M_u^{\dagger} M_d M_d^{\dagger} ]$$

must contain flavour matrices from the up and down sector

lowest order in powers of mass from SM case (  $\text{Tr} [ H_u, H_d ]^3 \propto I_2$  )

BGL type models have richer flavour structure parametrised by four matrices

$$I_9^{CP} (\chi = u, i=3) = - \left( \frac{\sqrt{2}}{\sigma_1} + \frac{\sqrt{1}}{\sqrt{2}} \right) (m_R^2 - m_A^2) (m_R^2 - m_D^2) (m_A^2 - m_d^2) \times \\ \text{FCNC in down sector, } P_3 \quad \times (m_c^2 - m_u^2) \text{Im} (V_{22}^* V_{32} V_{33}^* V_{23})$$

$I_9^{CP}$  controlled by  $V_{CKM}$  (BGL)

$I_9^{CP} \neq 0$  even if  $m_t = m_c$  or  $m_t = m_u$  since discrete symmetry singlets out top quark

$I_9^{CP}$  can be related to flavour asymmetry generated at EW phase transition

# Scalar Potential

$$Z_4 \text{ forbids } \phi_1^\dagger \phi_2, \phi_1^\dagger \phi_2 \phi_2^\dagger \phi_2, \phi_1^\dagger \phi_2 \phi_1^\dagger \phi_2$$

ungauged accidental continuous symmetry  
not a symmetry of full Lagrangian

after spontaneous gauge symmetry breaking  $\rightarrow$   
 $\rightarrow$  pseudo Goldstone boson

solution: soft symmetry breaking  $m_{12} \phi_1^\dagger \phi_2 + \text{h.c.}$

Work in progress

Phenomenological implications of BGL models  
36 different models  $6 \text{ quarks} \times 6 \text{ leptons}$

i) making use of exp results in agreement with the SM  
plus wild average on  $B \rightarrow \tau \nu$

ii) all the above plus  $B \rightarrow D \tau \nu$  from BFBAR

Taking into account the T parameter constraint

## Conclusions

Multi-Higgs models are very interesting candidates for NP

There are new mechanisms beyond NFC to obtain strong suppression of FCNC as required by experiment

LHC results may bring surprises for the Higgs sector

WB invariant conditions are a powerful tool to analyse the Higgs structure of these models