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*Higgs, LHC Data etc.*

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*M. Margarete Mühlleitner*

**Moriond QCD**  
**And Higgs-Energy Interactions**

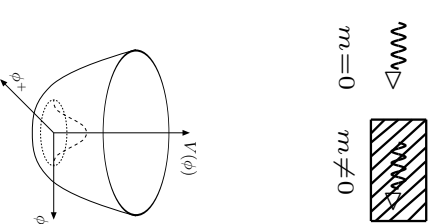
14 March 2013

## What Have We Seen at the LHC?

- \* The production of a new particle with mass around  $M = 125\text{GeV}$
- \* Is it *the* Standard Model scalar boson *responsible for EWSB*?  $\Rightarrow$

### Test of the EWSB mechanism

- Discovery –  $m$
- Interaction with the scalar boson with  $v = 246\text{ GeV} \neq 0$   $\rightsquigarrow g_{HXX} \sim m_X$
- Spin and parity quantum numbers –  $J^{PC}$
- EWSB: potential w/ non-vanishing VEV –  $\lambda_{HHH}, \lambda_{HHHH}$



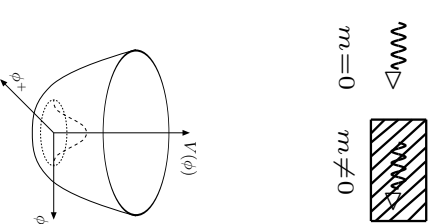
- \* Is it the scalar boson of the SM, of SUSY, a Composite scalar boson, ...?

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- Spin and parity quantum numbers  $\Leftarrow$  **This talk**
- EWSB: potential w/ non-vanishing VEV –  $\lambda_{HHH}, \lambda_{HHHH}$



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# Basis of Higgs-Spin/Parity Measurements at the LHC

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in collaboration with *S. Y. Choi, D. J. Miller and P. M. Zerwas*

- Literature

- \* LHC Higgs CXN WG, YR3

- \* S.Y. Choi, D.J. Miller, M.M. Muhlleitner and P.M. Zerwas  
“Identifying the Higgs spin and parity in decays to  $Z$  pairs”  
Phys. Lett. **B553** (2003) 61 [hep-ph/0210077]

- \* S.Y. Choi, M.M. Muhlleitner and P.M. Zerwas  
“Theoretical Basis of Higgs-Spin Analysis in  $H \rightarrow \gamma\gamma$  and  $Z\gamma$  Decays”  
Phys. Lett. **B718** (2013) 1031 [arXiv:1209.5268 [hep-ph]]

- **Further publications:** Hagiwara eal; De Rujula eal; Gao eal; S. Bolognesi eal; J. Ellis eal; Alves; Godbole eal; Plehn eal; Englert eal; Frank eal; Djouadi eal; ...

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# Program

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Necessary and sufficient conditions for  $J^P = 0^+$  [vis-a-vis SM]

- **Theoretical Tools:**

- \* helicity analyses
- \* operator expansions

- **Systematic analysis of production and decay processes**

- \*  $Z^*Z$  decays Choi eal; Gao eal; De Rujula eal; Bolognesi eal
- \*  $\gamma\gamma$  decays Ellis, Hwang; Alves; Choi eal
- \* CP-violating decays Soni, Xu; Chang eal; Godbole eal; Nelson
- \* Production in gluon fusion, in vector boson fusion Plehn eal; Hagiwara eal
- \* Production in Higgs-strahlung Miller eal; Ellis eal

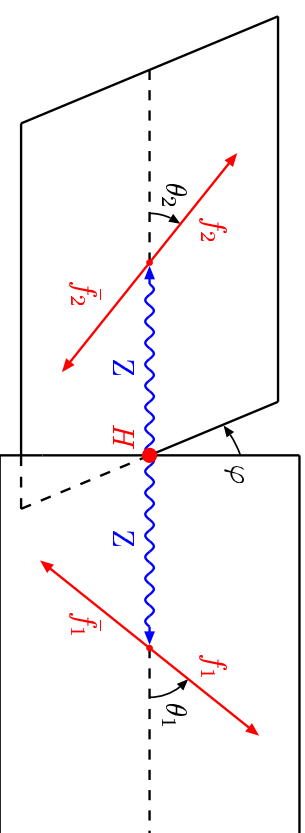
- **Observation in  $\gamma\gamma$ :** No spin 1 [Landau-Yang];  $C = +1$  [charge invariance]

# (I) Angular Distributions/ $\mathcal{T}$ thresholds in $H \rightarrow VV^* \rightarrow 4\mathcal{L}$

- ◇ Determination of spin and parity in

$$H \rightarrow ZZ^{(*)} \rightarrow (f_1 \bar{f}_1)(f_2 \bar{f}_2)$$

in  $H$  c.m. frame



- ◇ Helicity methods to generalize to arbitrary spin and parity

$$\langle Z(\lambda_1)Z(\lambda_2)|H\mathcal{J}(m)\rangle = \mathcal{T}_{\lambda_1\lambda_2} d_{m,\lambda_1-\lambda_2}^{\mathcal{J}}(\Theta) e^{-i(m-\lambda_1+\lambda_2)\varphi}$$

- ◇ General tensor for  $HZZ$  vertex for each  $\mathcal{J}^{\mathcal{P}}$

$$\mathcal{J} = T_{\mu\nu\beta_1\dots\beta_{\mathcal{J}}} \epsilon^*(Z_1)^\mu \epsilon^*(Z_2)^\nu \epsilon(H)^{\beta_1\dots\beta_{\mathcal{J}}}$$

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## Differential Distributions $\mathcal{P}$ ure-Spin/ $\mathcal{P}$ arity Unpolarized Boson $H^J$

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### ◇ Double polar angular distribution (CP-invariant theory)

$$\frac{1}{\Gamma'} \frac{d\Gamma'}{d \cos \theta_1 d \cos \theta_2} = \left[ \sin^2 \theta_1 \sin^2 \theta_2 |\mathcal{T}_{00}|^2 + \frac{1}{2} (1 + \cos^2 \theta_1) (1 + \cos^2 \theta_2) [|\mathcal{T}_{11}|^2 + |\mathcal{T}_{1,-1}|^2] \right] + (1 + \cos^2 \theta_1) \sin^2 \theta_2 |\mathcal{T}_{10}|^2 + \sin^2 \theta_1 (1 + \cos^2 \theta_2) |\mathcal{T}_{01}|^2 \Big] / \mathcal{N}$$

$\mathcal{N} = (16/9) \sum |\mathcal{T}_{\lambda\lambda'}|^2$  – normalization

### ◇ Azimuthal angular distribution (CP-invariant theory)

$$\frac{1}{\Gamma'} \frac{d\Gamma'}{d\phi} = \frac{1}{2\pi} [1 + |\zeta_1| \cos 2\phi]$$

$$|\zeta_1| = |\mathcal{T}_{11}|^2 / [2 \sum |\mathcal{T}_{\lambda\lambda'}|^2]$$

suppressing terms quadratic in  $\eta_i = 2v_i a_i / (v_i^2 + a_i^2) \sim 0.02$ ,  $v_i, a_i$  electroweak fermion  $f_i$  charges

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## Determination of Spin and Parity, Necessary Conditions

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- **Standard Model:**

$$\mathcal{T}_{00} = (M_H^2 - M_*^2 - M_Z^2)/(2M_*M_Z), \quad \mathcal{T}_{11} = +\mathcal{T}_{-1,-1} = -1, \quad \mathcal{T}_{10} = \mathcal{T}_{01} = \mathcal{T}_{1,-1} = 0$$

Necessary conditions:

- ◇ Double polar angular distribution

$$\frac{1}{\Gamma'} \frac{d\Gamma'}{d\cos\theta_1 d\cos\theta_2} = \frac{9}{16} \frac{1}{\gamma^4 + 2} \left[ \gamma^4 \sin^2\theta_1 \sin^2\theta_2 + \frac{1}{2} (1 + \cos^2\theta_1)(1 + \cos^2\theta_2) \right]$$

- ◇ Azimuthal angular distribution

$$\frac{1}{\Gamma'} \frac{d\Gamma'}{d\phi} = \frac{1}{2\pi} \left[ 1 + \frac{1}{2} \frac{1}{\gamma^4 + 2} \cos 2\phi \right]$$

$$\gamma^2 = (M_H^2 - M_*^2 - M_Z^2)/(2M_*M_Z)$$



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## Determination of Spin and Parity, Sufficient Conditions

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- $M_H < 2M_Z$ :  $d\Gamma/dM_*^2 \sim \beta$  for  $\mathcal{J}^P = 0^+$

◇  $d\Gamma/dM_*^2$  rules out  $\mathcal{J}^P = 0^-, 1^-, 2^-, 3^\pm, 4^\pm$  [threshold rise]

◇  $d\Gamma/dM_*^2$  and no  $[1 + \cos^2 \theta_1] \sin^2 \theta_2$

$[1 + \cos^2 \theta_2] \sin^2 \theta_1$  rules out  $\mathcal{J}^P = 1^+, 2^+$

$\Rightarrow$  only  $0^+$  left (sufficient conditions)

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## Pseudoscalar $A$ with $J^P = 0^-$

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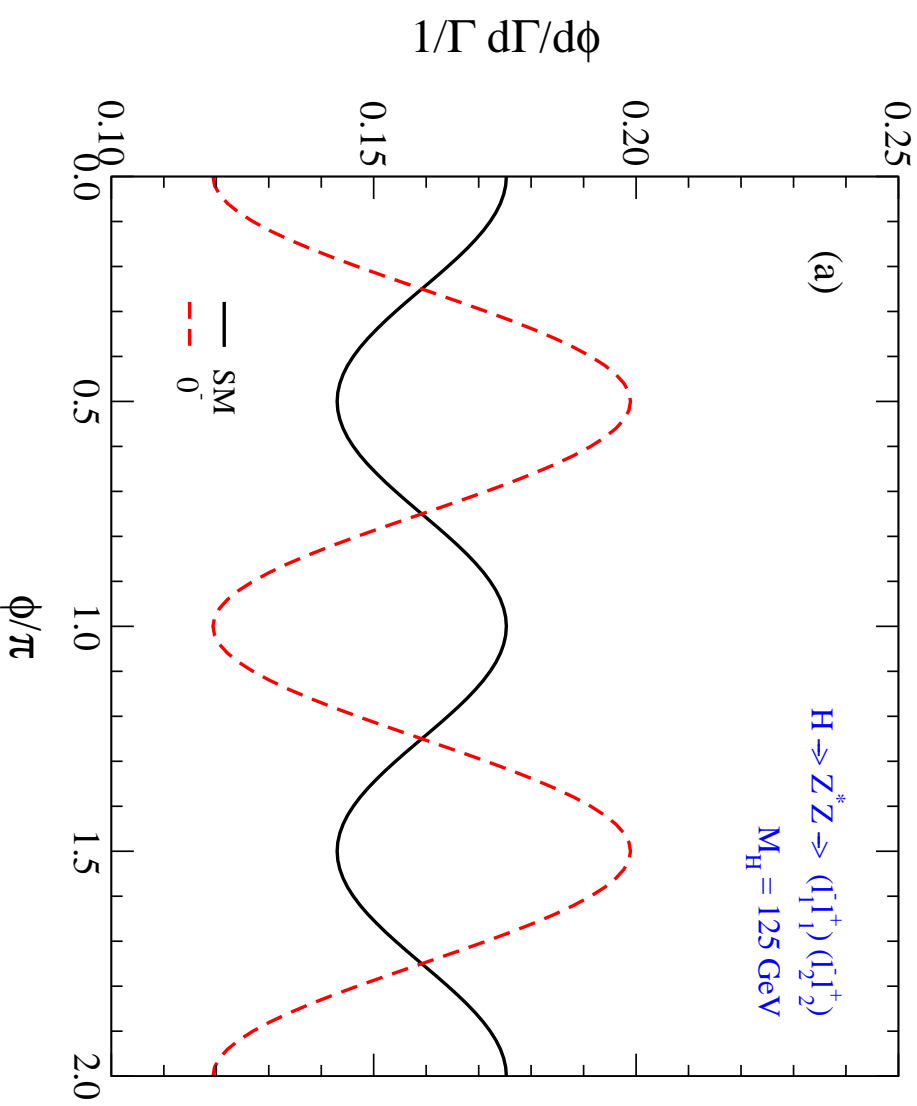
- **Differential Distributions:** Parity invariance  $\rightsquigarrow$

$$\begin{aligned}\frac{1}{\Gamma_A} \frac{d\Gamma_A}{d\cos\theta_1 \cos\theta_2} &= \frac{9}{64} (1 + \cos^2\theta_1)(1 + \cos^2\theta_2) \\ \frac{1}{\Gamma_A} \frac{d\Gamma_A}{d\phi} &= \frac{1}{2\pi} \left[ 1 - \frac{1}{4}\cos 2\phi \right]\end{aligned}$$

- **Threshold Behaviour:**  $d\Gamma_A/dM_*^2 \sim \beta^3$
- **If too small branching ratio  $A \rightarrow Z^*Z$ :** sufficient and necessary conditions of spin/parity
  - Spin 0: isotropic angular distribution in  $gg \rightarrow A \rightarrow \gamma\gamma$   $\longrightarrow$
  - Jets in  $gg \rightarrow A + gg$  anti-correlated for pseudoscalar (correlated for scalar) Hagiwara et al
  - Exploit fermionic decay channels

# # Azimuthal Angular Distributions: Parity

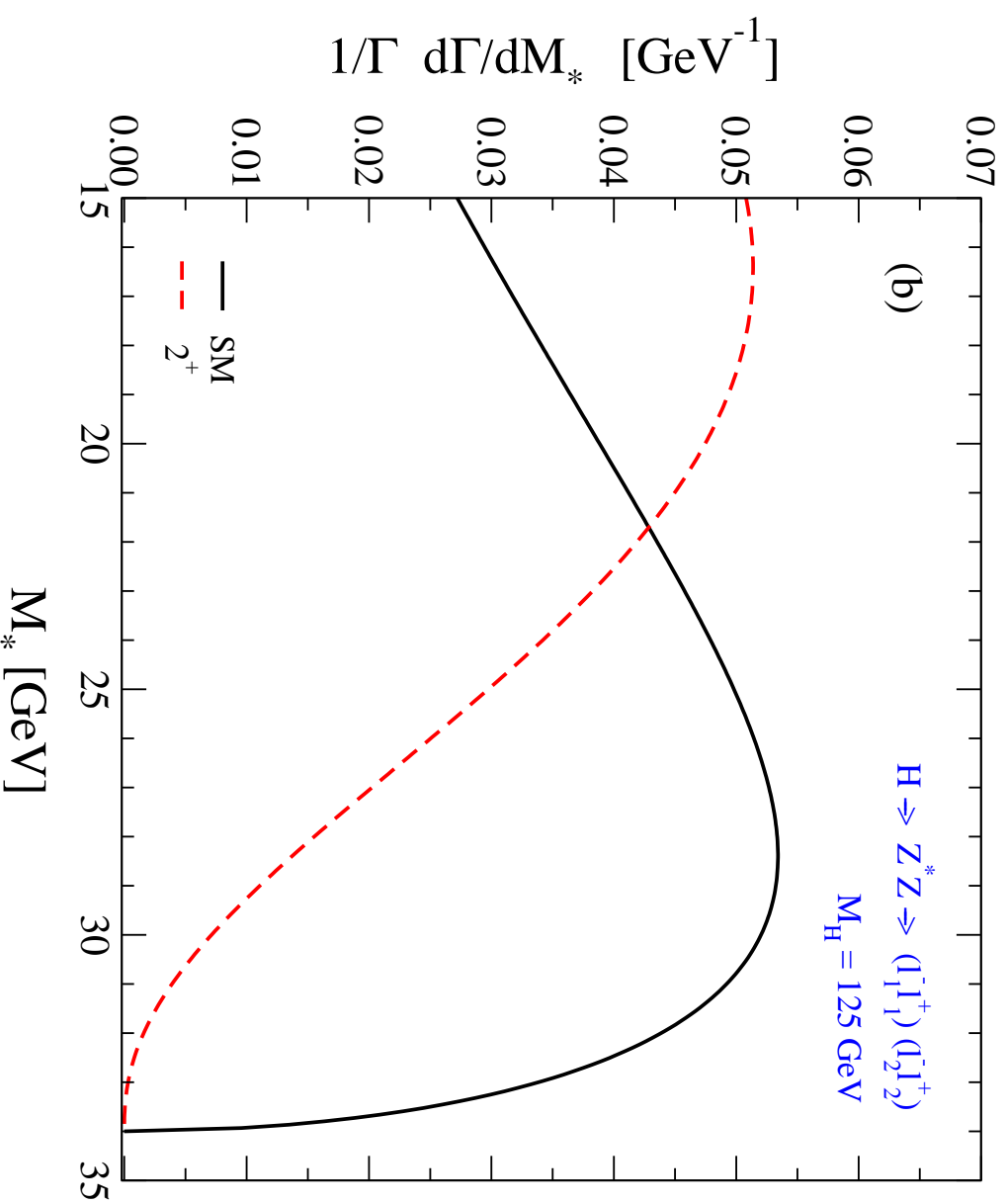
Choi, Miller, MMM, Zerwas



$$0^+ : d\Gamma/d\phi \sim 1 + f_{\text{kin}} \cos 2\phi, \quad 0^- : d\Gamma/d\phi \sim 1 - 1/4 \cos 2\phi$$

## # $\mathcal{T}$ Threshold Behaviour: Spin

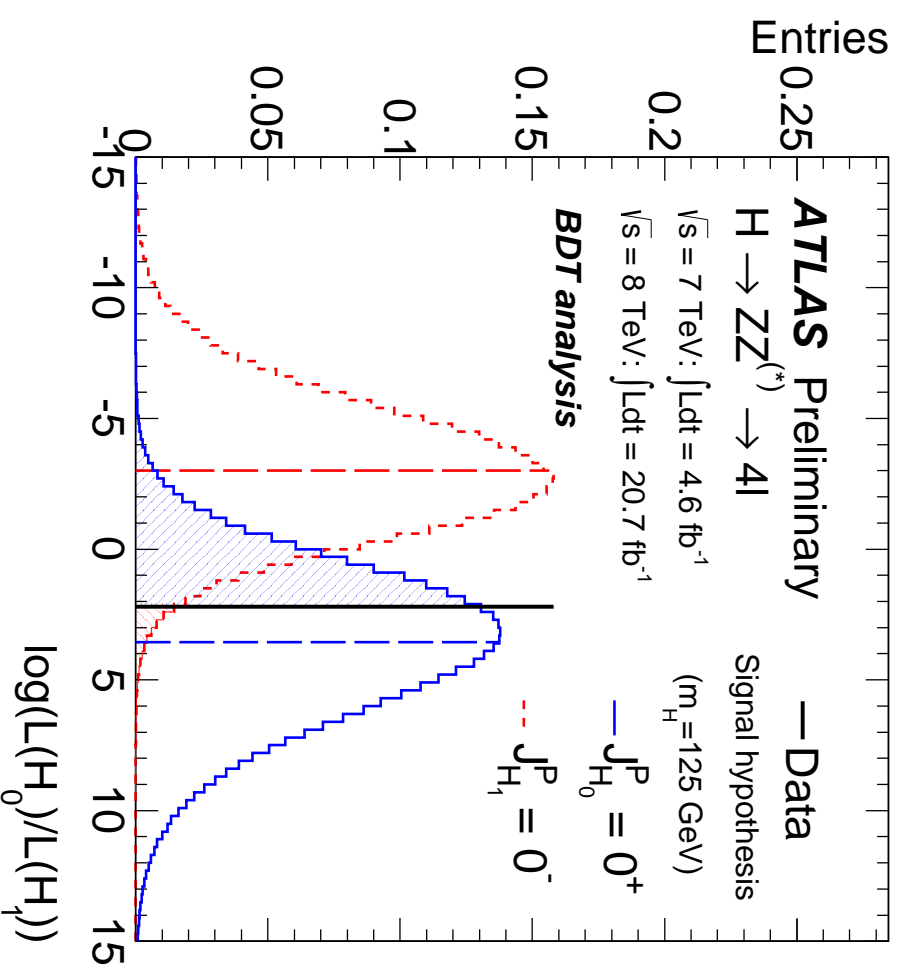
Choi, Miller, MMM, Zerwas



# ATLAS Results

- $0^+, 0^-, 1^+, 1^-, 2^+, 2^-$  hypotheses in  $H \rightarrow ZZ^* \rightarrow 4l$

ATLAS-CONF-2013-013



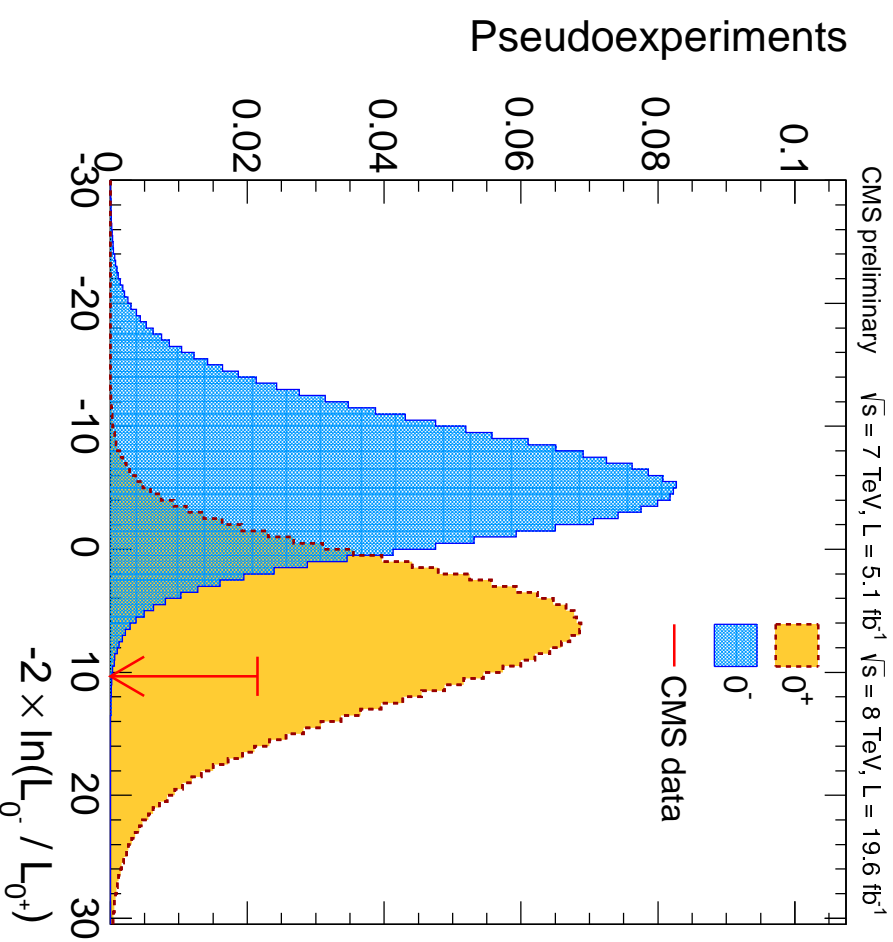
$0^-, 1^+$  states excluded at 97.8% CL in favour of  $0^+$

- Spin studies in  $H \rightarrow \gamma\gamma$  ATLAS-CONF-2012-168,  $H \rightarrow WW^* \rightarrow e\nu\mu\nu$  ATLAS-CONF-2013-031

## CMS Results

- $0^+$ ,  $0^-$ ,  $1^+$ ,  $1^-$ ,  $2^+$ ,  $2^-$  hypotheses in  $H \rightarrow ZZ^* \rightarrow 4l$

PRL 110 (2013)  
CMS-PAS-HIG-13-002



$0^-, 1, 2$  excluded at 95% CL or higher

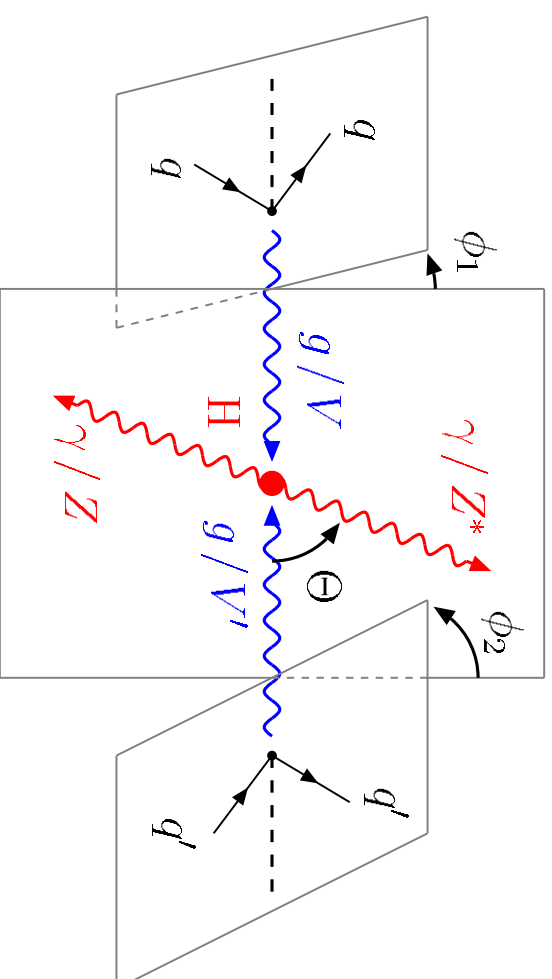
- Spin studies in  $H \rightarrow WW^* \rightarrow l\nu l\nu$  CMS-PAS-HIG-13-003

## (II) $\mathcal{H}$ iggs-Spin Analysis through $gg \rightarrow H^J \rightarrow \gamma\gamma$ Decays

- Systematic helicity analyses for angular distributions

$$\frac{1}{\sigma} \frac{d\sigma(\gamma\gamma)}{d\cos\Theta} = (2J + 1) [\kappa_0^J \gamma_0^J D_{00}^J + \kappa_0^J \gamma_2^J D_{02}^J + \kappa_2^J \gamma_0^J D_{20}^J + \kappa_2^J \gamma_2^J D_{22}^J]$$

- \*  $D_{m\lambda}^J$  squared Wigner functions,  $m = S_z$  spin component,  $\lambda \equiv \lambda_\gamma - \lambda'_\gamma$
- \*  $\kappa$  production helicity probability
- \*  $\gamma$  decay helicity probability



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## (II) Higgs-Spin Analysis through $gg \rightarrow H^J \rightarrow \gamma\gamma$ Decays

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### • Systematic helicity analyses for angular distributions

$$\frac{1}{\sigma} \frac{d\sigma(\gamma\gamma)}{d\cos\Theta} = (2J + 1) [\mathcal{K}_0^J \mathcal{Y}_0^J \mathcal{D}_{00}^J + \mathcal{K}_2^J \mathcal{Y}_2^J \mathcal{D}_{02}^J + \mathcal{K}_2^J \mathcal{Y}_0^J \mathcal{D}_{20}^J + \mathcal{K}_2^J \mathcal{Y}_2^J \mathcal{D}_{22}^J]$$

- \*  $\mathcal{D}_{m\lambda}^J$  squared Wigner functions,  $m = S_z$  spin component,  $\lambda \equiv \lambda_\gamma - \lambda'_\gamma$
- \*  $\mathcal{X}$  production helicity probability
- \*  $\mathcal{Y}$  decay helicity probability

### • Types

'scalar-type assignment' (Higgs):  $\mathcal{X}_0^J = \mathcal{Y}_0^J = 1$  and  $\mathcal{X}_2^J = \mathcal{Y}_2^J = 0$  [ $J \geq 0$ ]

'tensor-type assignment' (graviton-like):  $\mathcal{X}_0^J = \mathcal{Y}_0^J = 0$  and  $\mathcal{X}_2^J = \mathcal{Y}_2^J = 1$  [ $J \geq 2$ ]



## General Spin/Parity Assignments

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- Selection rules for Higgs spin/parity from observing the polar angular distributions of a spin- $J$  Higgs state in  $gg \rightarrow H \rightarrow \gamma\gamma$

$\mathcal{P} \setminus J$	0	1	2, 4, ...	3, 5, ...
even	1	forbidden	$\mathcal{D}_{00}^J$ $\mathcal{D}_{02}^J$ $\mathcal{D}_{20}^J$ $\mathcal{D}_{22}^J$	$\mathcal{D}_{22}^J$
odd	1	forbidden	$\mathcal{D}_{00}^J$	forbidden

- Squared Wigner functions  $\mathcal{D}_{m\lambda}^J$  up to  $\sim |\cos^{2J} \Theta|$

$$\mathcal{D}_{00}^0 = 1$$

$$\mathcal{D}_{00}^2 = (3 \cos^2 \Theta - 1)^2 / 4 \quad \mathcal{D}_{22}^2 = (\cos^4 \Theta + 6 \cos^2 \Theta + 1) / 16$$

## General Spin/Parity Assignments

- Selection rules for Higgs spin/parity from observing the polar angular distributions of a

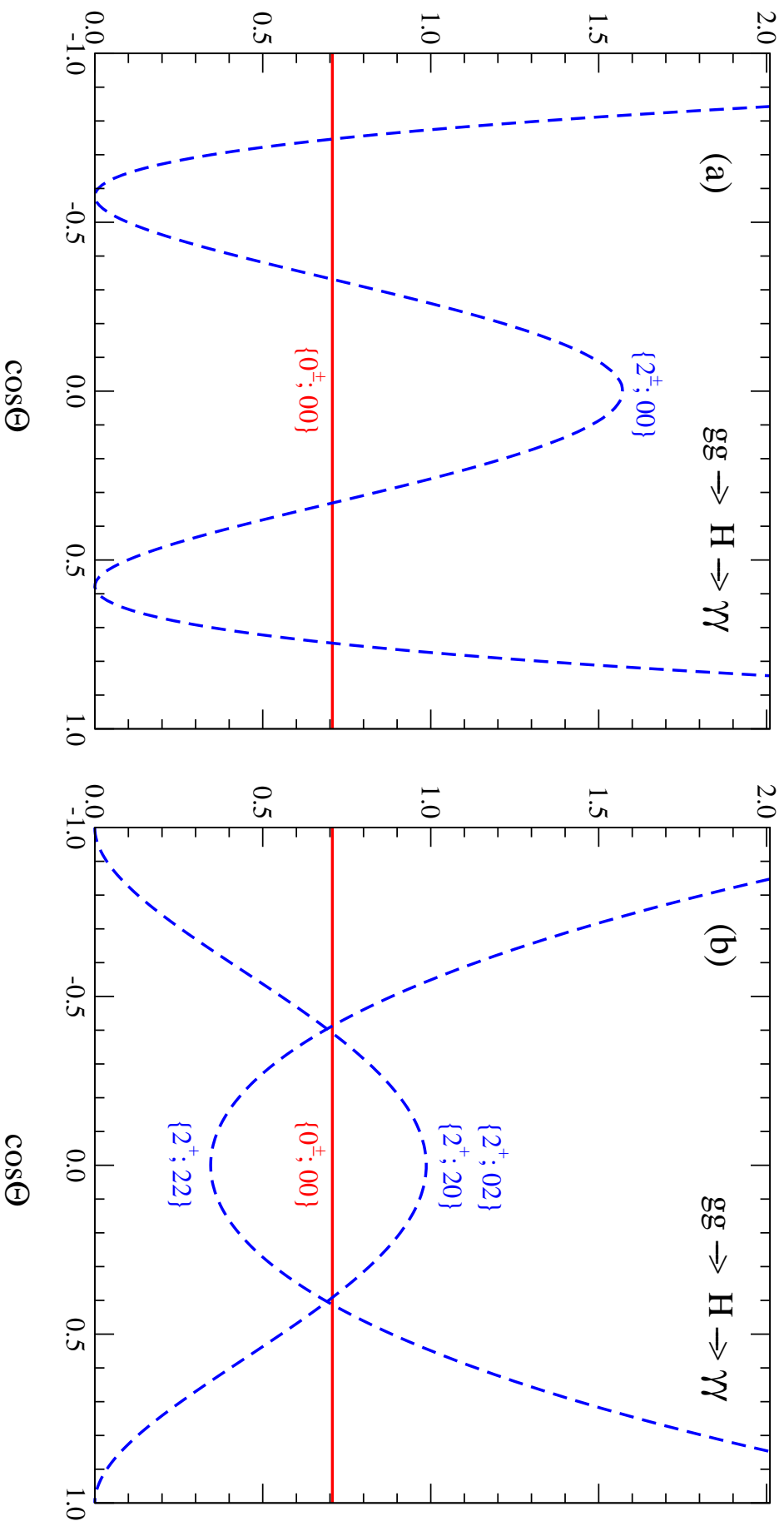
spin- $J$  Higgs state in  $gg \rightarrow H \rightarrow \gamma\gamma$

$\mathcal{P} \setminus J$	0	1	2, 4, ...	3, 5, ...
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odd	1	forbidden	$\mathcal{D}_{20}^J$ $\mathcal{D}_{22}^J$	forbidden

- $0^\pm$  :  $D_{00}^0$  observed, none else  $\rightsquigarrow \pm$  undisc      $1^\pm$  : forbidden by Landau/Yang  
 $2^+$  :  $D_{00}^2$  and  $D_{22}^2 \neq 0$ , both      $3^+$  :  $D_{22}^3 \neq 0$ , none else  
 $2^-$  :  $D_{00}^2 \neq 0$ , none else      $3^-$  : forbidden  
 ...     ...

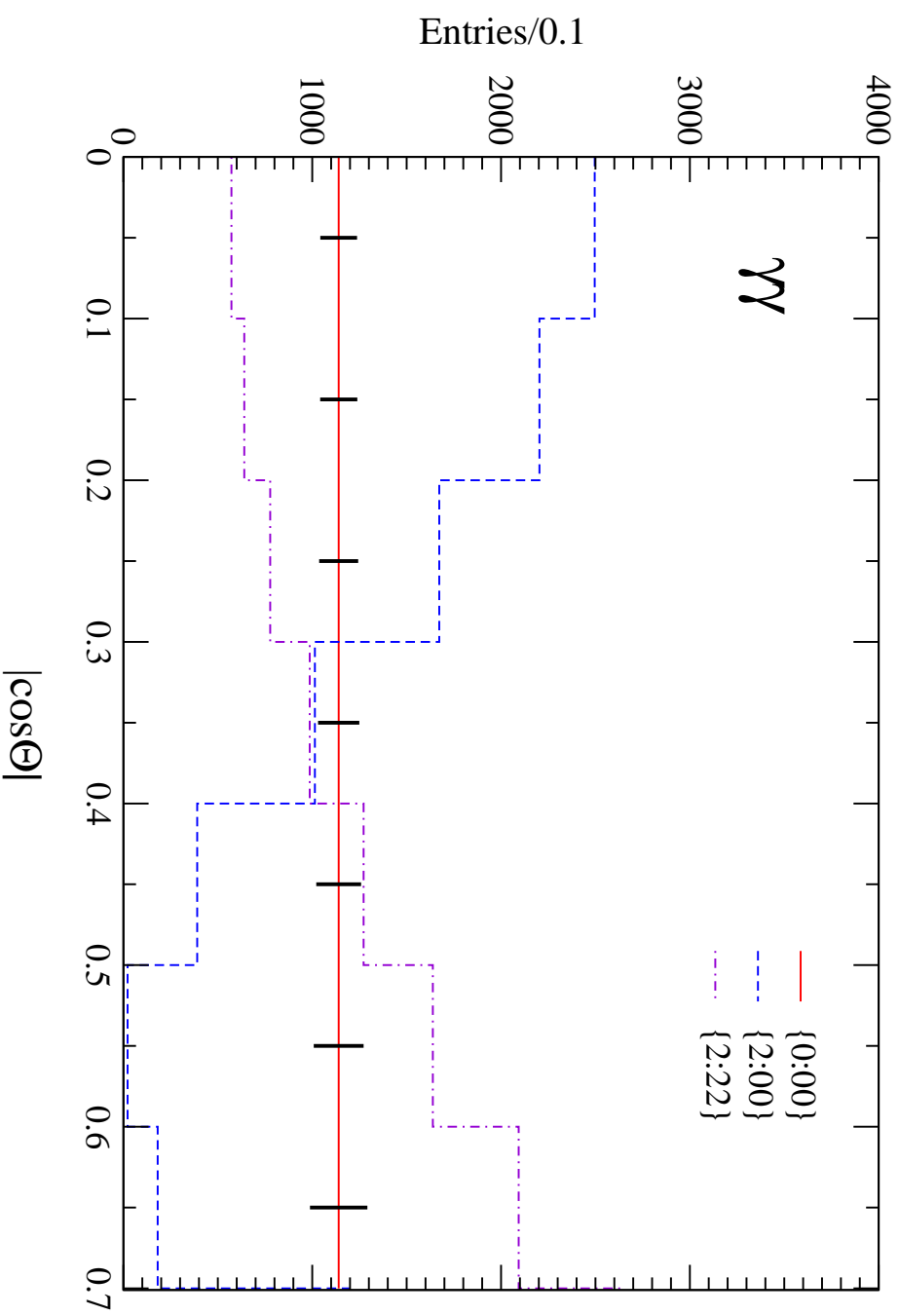
# Scalar-type, $\mathcal{T}$ tensor-type

Choi, Miller, MMM, Zerwas



# Distinction Scalar-type, $\mathcal{T}$ tensor-type

Choi, MMM, Zerwas



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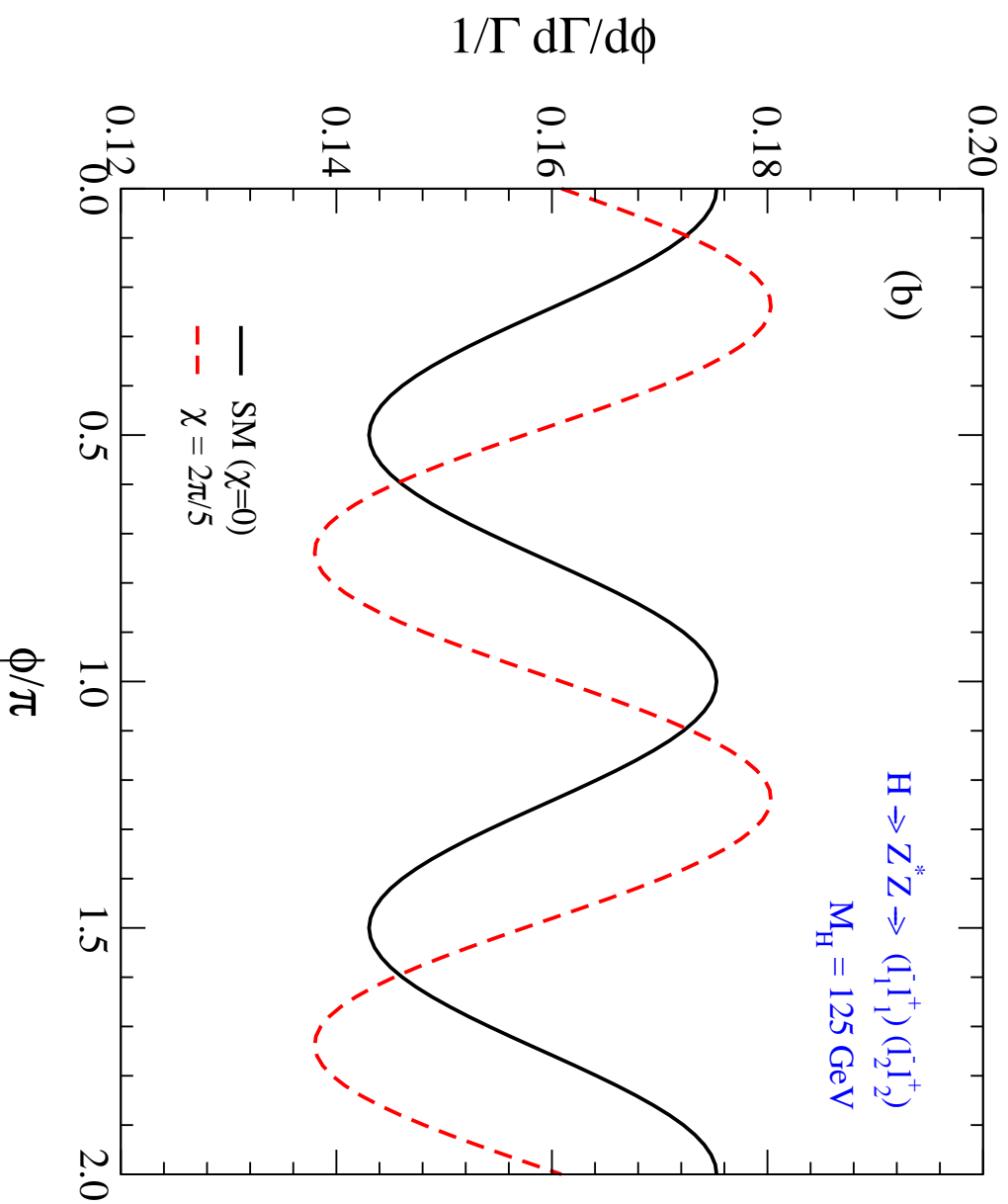
## (III) Further Analyses

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- **Analogous analysis:** Angular distribution of  $Z^*Z$  axis in  $Z^*Z$  final states
- **Parity check in:**
  - \* Azimuthal corr. between radiation planes in  $qq \rightarrow VV' + qq \rightarrow H, A + qq$  Plehn eal; Hagiwara eal
  - \* Correlations of planes in  $gg \rightarrow H, A + 2 \text{ jets}$  Hagiwara eal
- **Spin/Parity in Higgs-strahlung:**  $q\bar{q} \rightarrow Z/W + H^J$  Choi eal; Ellis eal; Englert eal; Frank eal; Djouadi eal
- **Fermionic decays:** Angular correlations among fermion decay products in  $H^J \rightarrow f\bar{f} \rightarrow a\bar{a} \dots$   
Kramer eal; Berge eal
- **CP-violating  $H'$ :**
  - \* In  $H' \rightarrow Z^*Z$ , hopefully Godbole, Miller, MMM
  - \* Alternatively in Higgs + 2 jets

# $\mathcal{CP}$ Violation in $H' \rightarrow Z^*Z \rightarrow 4l$

Choi, Miller, MMM, Zerwas



$$H' = \cos \chi H + \sin \chi e^{i\xi} A$$

Ellis eal; Choi eal

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## Conclusions

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- \* Angular helicity analyses and threshold effects in particle decays into  $VV'$ ,  $\gamma\gamma$ ,  $f\bar{f}$
- \* Initial-final state angular correlations in Higgs decays into  $\gamma\gamma$ ,  $VV'$  in gluon fusion
- \* Azimuthal angle correlation in gluon fusion + 2 jets, vector boson fusion

Straightforward strategies identified for proving  $J^P = 0^+$  experimentally  
under necessary and sufficient conditions.

- \* CP-violation: - in  $H' \rightarrow Z^*Z$ 
  - in azimuthal distributions of decay planes in vector boson fusion, gluon fusion, fermion decays

**Thank you for your attention!**



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## (III) $\mathcal{F}$ urther Analyses - Continued

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- CP-violating spin-0 Higgs boson:

- In  $Z^*Z$  decays

$$V_{H'ZZ}^{\mu\nu} = ig_Z M_Z \left[ a g^{\mu\nu} + b \frac{p^\mu p^\nu}{M_H^2} + c \epsilon^{\mu\nu\rho\sigma} \frac{p_\rho k_\sigma}{M_H^2} \right]$$

CP-violation:  $c \wedge a$  and/or  $b$  non-zero

- CP-sensitive asymmetries
- Azimuthal angular modulation of the two jets in  $gg \rightarrow H' + gg \rightarrow \gamma\gamma + gg$
- Azimuthal angle-correlation between the two  $\tau$  decay planes in  $H' \rightarrow \tau^-\tau^+ \rightarrow a^-b^+ \dots$

Godbole et al

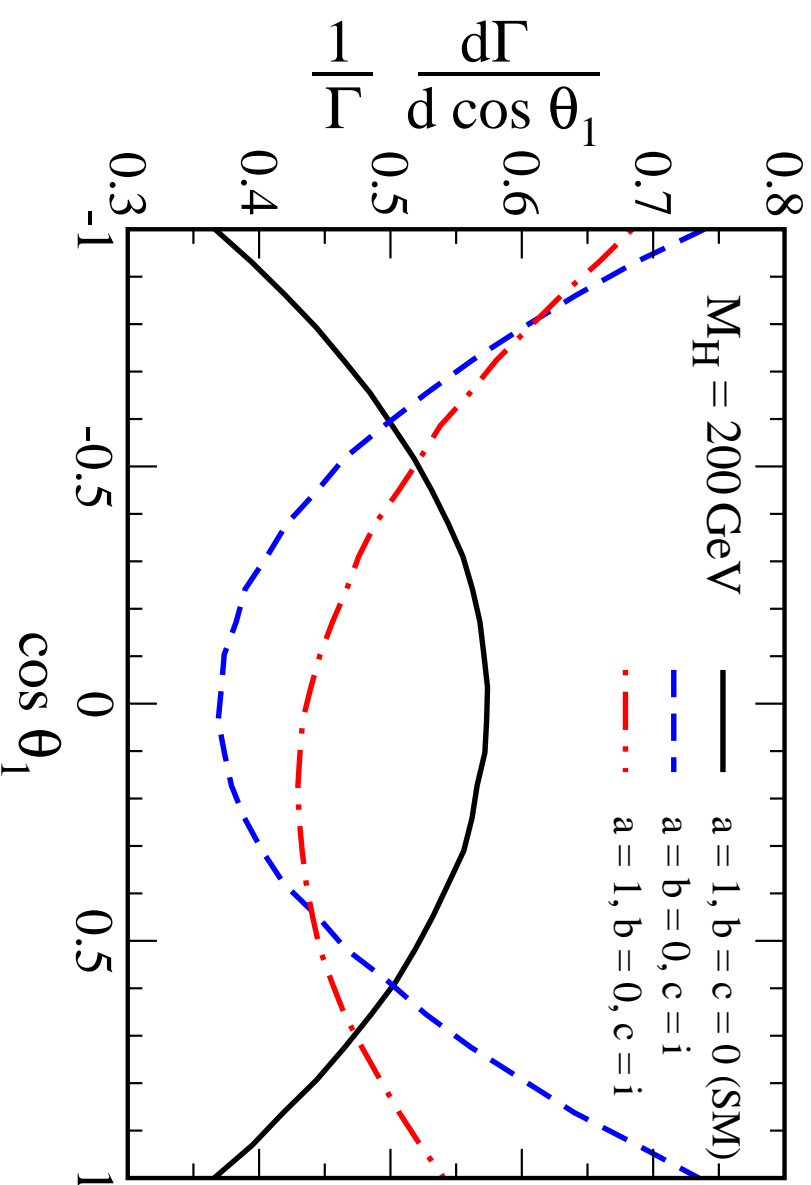
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## Higgs boson quantum numbers

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angular distribution in  $\cos \theta$

Godbole, Miller, MMM



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## Higgs boson quantum numbers

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angular distribution in  $\phi$

Godbole, Miller, MMM

