

# Measurements of gamma angle using $B \rightarrow DK$ at LHCb

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on behalf of the LHCb Collaboration

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Rencontres de Moriond QCD and High Energy Interactions  
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# Outline

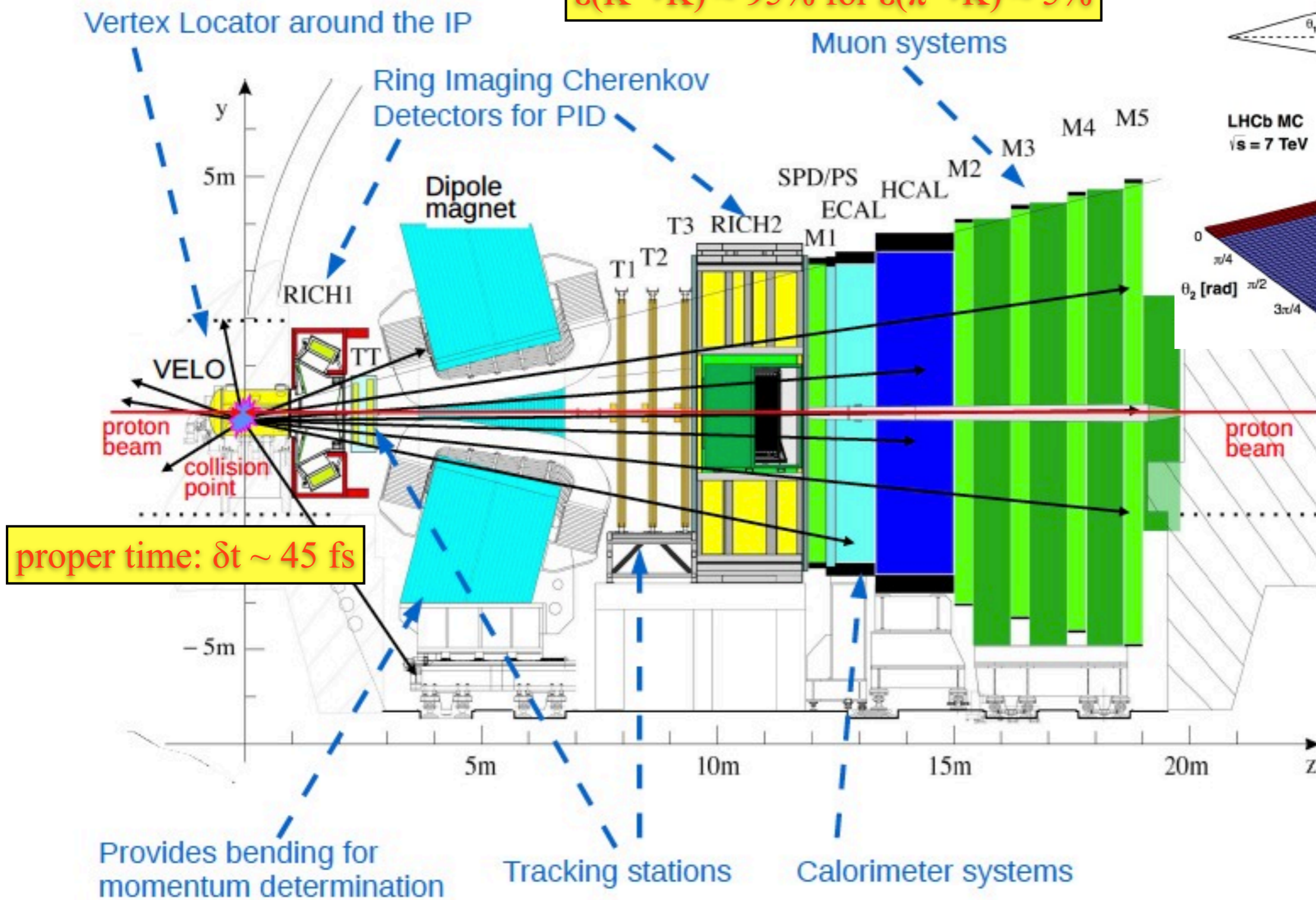
- **Brief view of the LHCb experiment**
- **Brief introduction of gamma Measurements at tree level**
- **Measurements with  $D \rightarrow 2\text{Body}$**
- **Measurements with  $D \rightarrow 3\text{Body}$**
- **Gamma Combination**
- **Conclusion**

# LHCb Apparatus

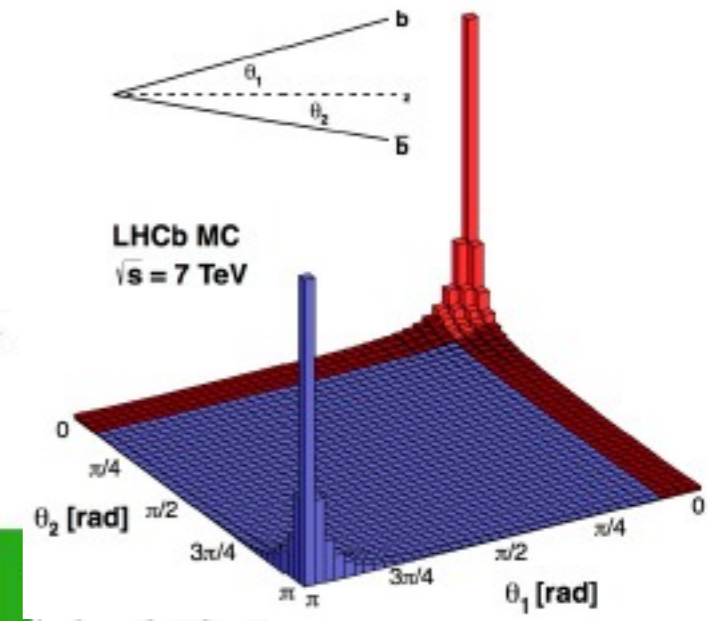
Designed for heavy quark physics  
Forward detector

$\sim 20\mu\text{m}$  IP resolution for high- $p_T$  tracks

$\epsilon(K \rightarrow K) \sim 95\%$  for  $\epsilon(\pi \rightarrow K) \sim 5\%$



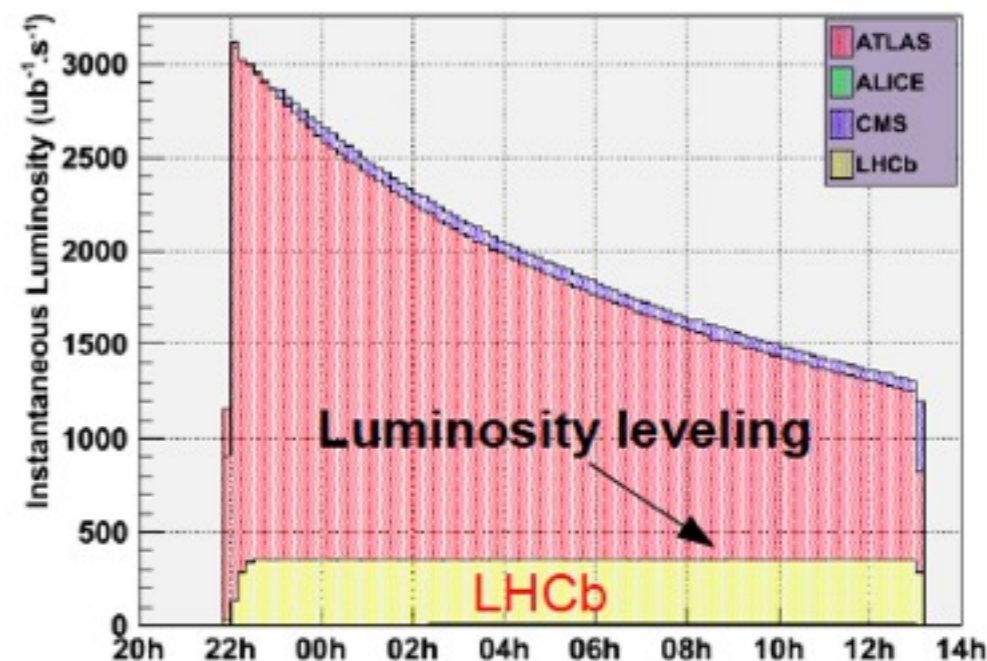
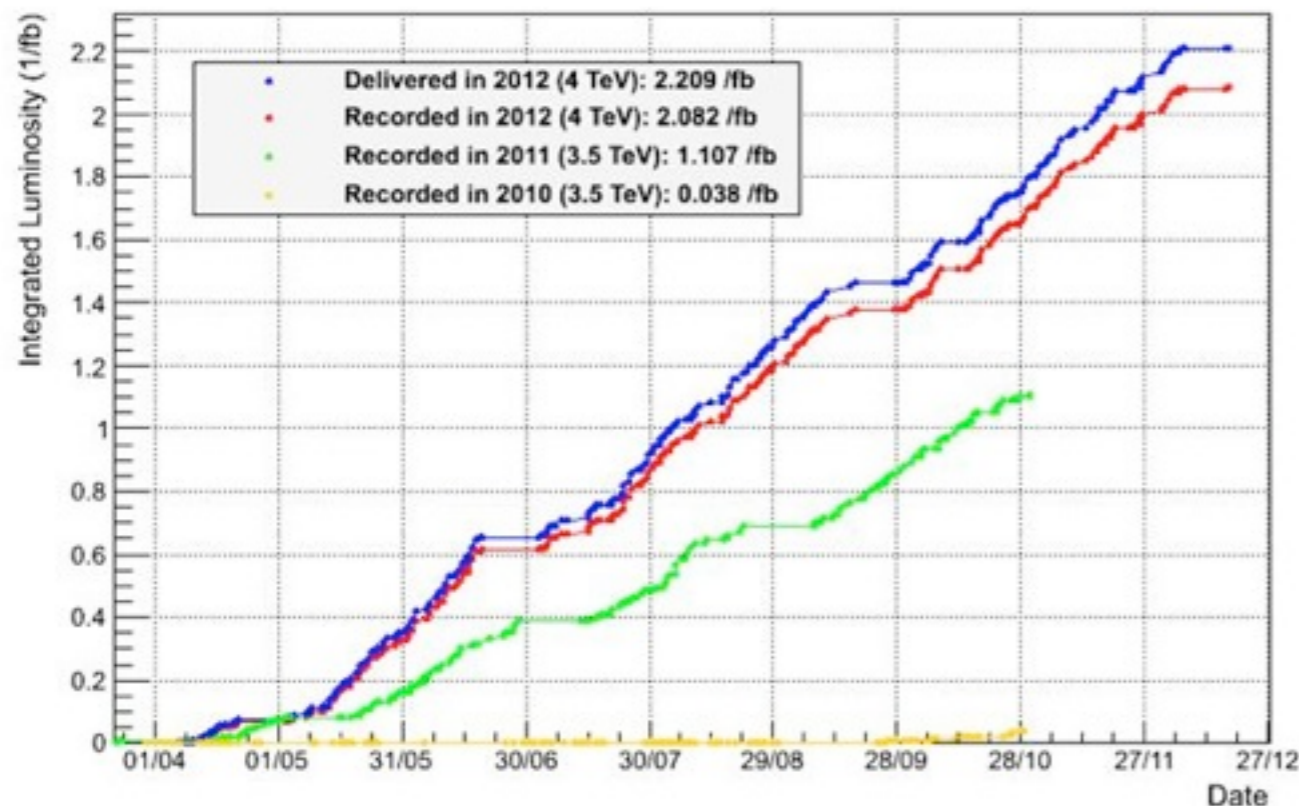
proper time:  $\delta t \sim 45$  fs



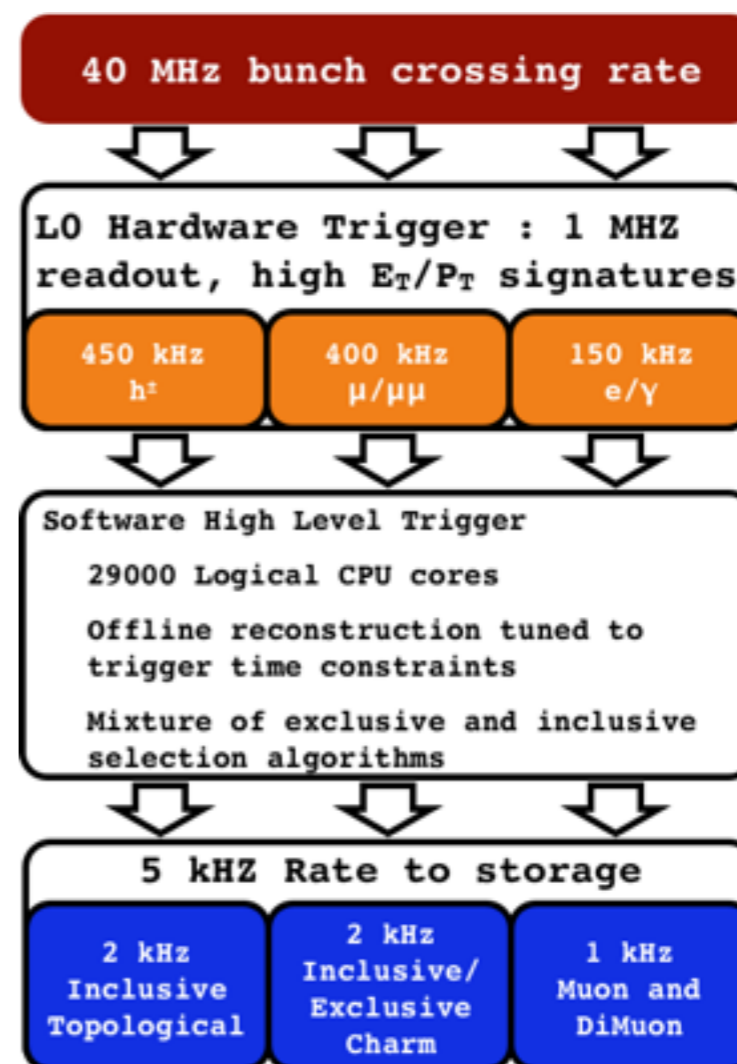
Charged Tracks  $\Delta p/p \sim 0.4\%$  at 5 GeV/c to 0.6% at 100 GeV/c,  $\sigma(m) \sim 10-25$  MeV

# LHCb Operation & Trigger

LHCb Integrated Luminosity pp collisions 2010-2012

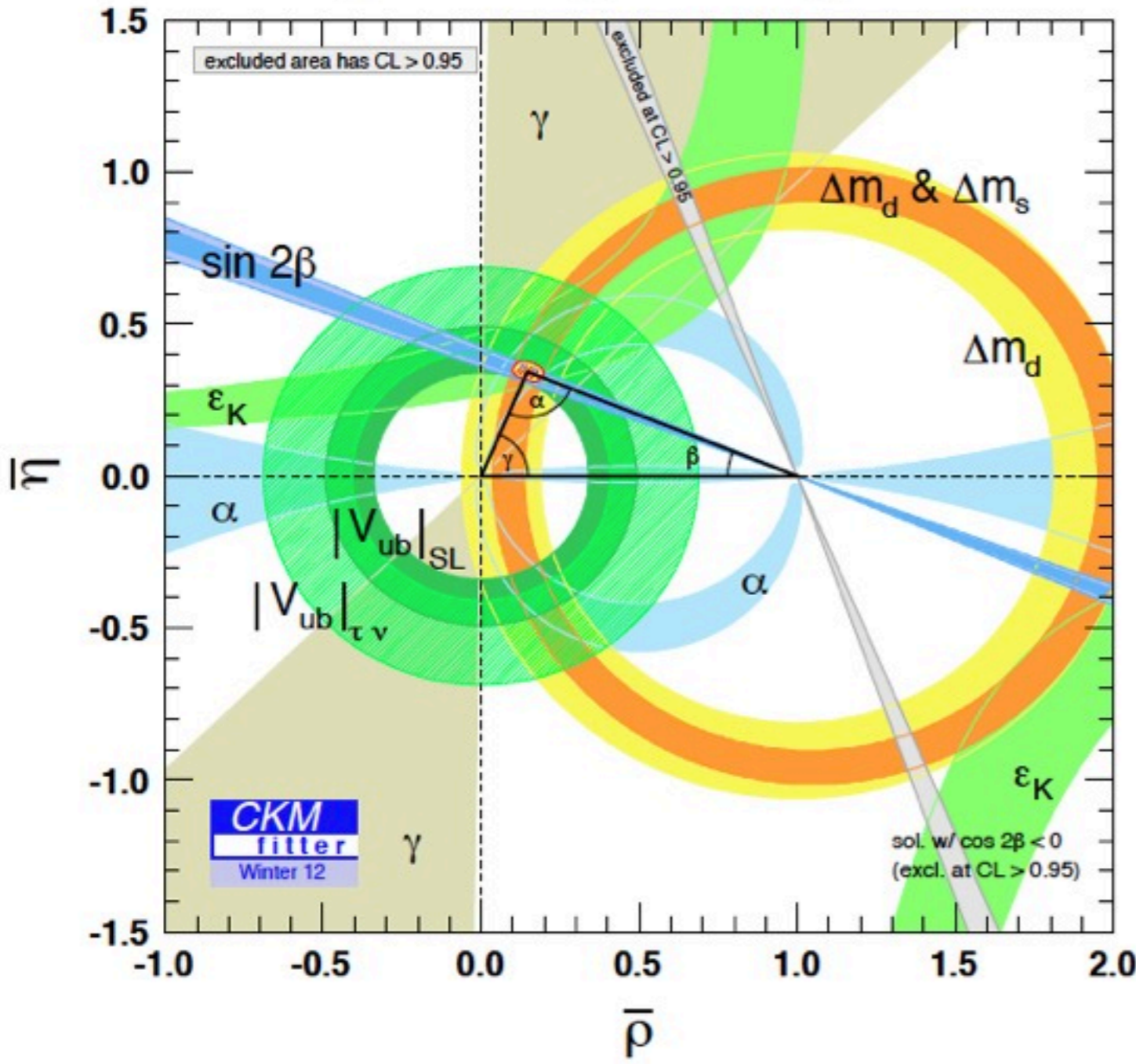


- **1.0 fb<sup>-1</sup> data @ 7 TeV in 2011**  
(Results in this talk)
- **~2 fb<sup>-1</sup> data @ 8 TeV in 2012**
- **Luminosity leveling**
- **Three level triggers:**
  - B decays with hadrons**
  - $\epsilon$  (L0 x HLT) ~ 20-50 %**



# CKM Angle gamma

$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$



$$\gamma = \arg \left[ -V_{ud} V_{ub}^* / (V_{cd} V_{cb}^*) \right]$$

➤ The least well known variable

**Babar:**  $\gamma = (69^{+17}_{-16})^\circ$  Babar Collaboration arXiv:1301.1029

**Belle:**  $\gamma = (68^{+15}_{-14})^\circ$  Belle Collaboration arXiv:1301.2033

**CKMFitter:**  $\gamma = (66 \pm 12)^\circ$

**UTFit:**  $\gamma = (76 \pm 10)^\circ$

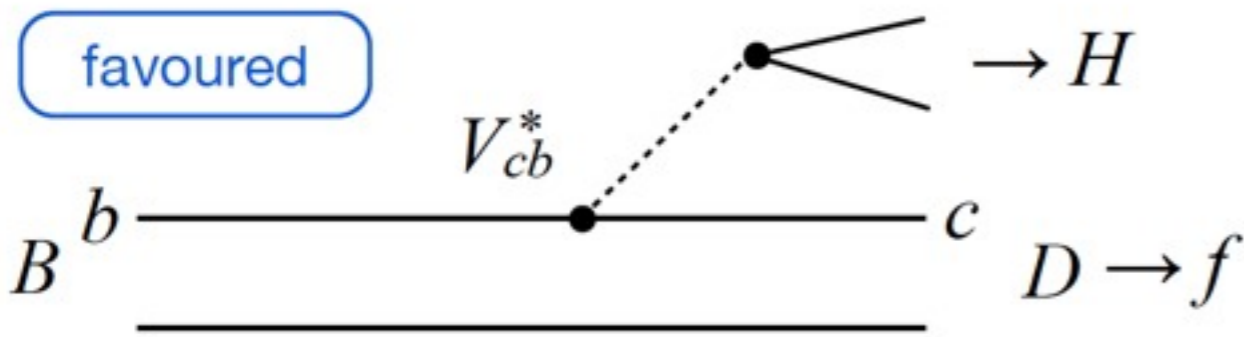
$\gamma$  from other constraints:  $\sim 4.3^\circ$   
CKM Fitter

**Theory:**  $\delta\gamma/\gamma \sim 0.000001$   
Jure Zupan, arXiv:1101.0134

➤ Can be accessed through tree-level transitions (i.e.  $B \rightarrow DK$ ) ➔ Test of standard model (This Talk)

➤ Can be accessed through loop-level transitions (i.e.  $B_{(s)} \rightarrow \pi\pi(KK)$ ) ➔ Probe of new physics

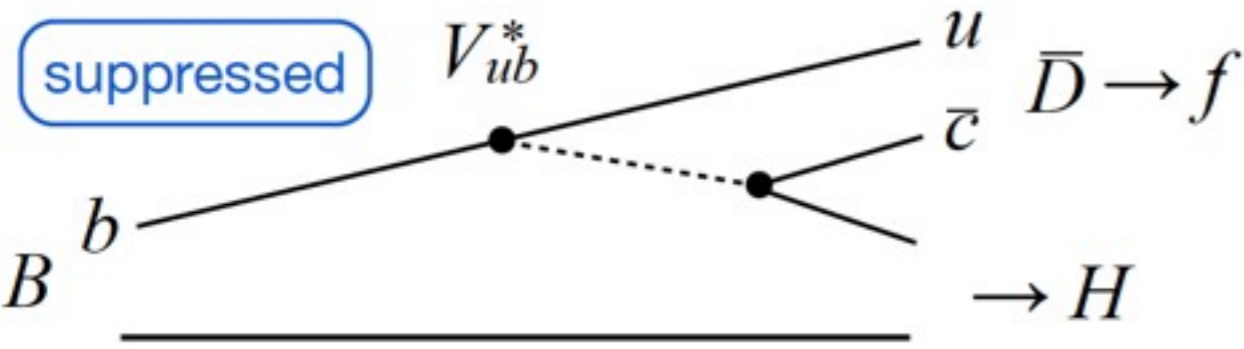
# $\gamma$ in B decays to Open Charm



$H = \mathbf{K}$  ( $\pi, \mathbf{KK}, \mathbf{K}\pi\pi$  etc)

$f = \mathbf{CP}$  eigenstates, e.g.  $\mathbf{KK}, \pi\pi$  (GLW)

M. Gronau and D. Wyler, Phys. Lett. B 253 (1991) 483  
 M. Gronau and D. London, Phys. Lett. B 265 (1991) 172



$f =$  quasi-flavour-specific states

e.g.  $\mathbf{K}\pi$  (ADS)

D. Atwood, I. Dunietz and A. Soni, Phys. Rev. Lett. 78 (1997) 3257

$f =$  self-conjugate multi(3)-body states

e.g.  $\mathbf{K}_s\pi\pi$  (GGSZ)

A. Giri, Y. Grossman, A. Soffer and J. Zupan, Phys. Rev. D68 (2003) 054018

$$\Gamma(B \rightarrow D[\rightarrow f]H) = A_c^2 (r_D^2 + r_B^2 + 2r_B r_D \text{Re}(e^{i(\delta_B + \delta_D \pm \gamma)}))$$

$\delta_B, \delta_D$ : hadronic phase difference for B and D decays

**Neglecting mixing in D:**

$r_D$ : ratio of D decay amplitudes,  $r_D=1$  for GLW

T. Grossman, A. Soffer, J. Zupan, arXiv: hep-ph/0505270

**Neglecting CPV in D:**

B. Bhattacharya, D. London, M. Gronau, J. L. Rosner, arXiv: 1301.5631

Sensitivity of  $\gamma$  depends largely on  $r_B = A_u/A_c$ :

$B \rightarrow DK: r_B^K \sim 0.1$  (more sensitive)

$B \rightarrow D\pi: r_B^\pi \sim 0.01$

# $\gamma$ Studies with $B^+ \rightarrow D^0 K^+$ (GLW)

Phys. Lett. B 712 (2012) 203,  
arXiv: 1203.3662

$$R_{CP+} = 2 \frac{\Gamma(B^- \rightarrow D_{CP+} K^-) + \Gamma(B^+ \rightarrow D_{CP+} K^+)}{\Gamma(B^- \rightarrow D^0 K^-) + \Gamma(B^+ \rightarrow \bar{D}^0 K^+)} = 1 + r_B^2 + 2r_B \cos \delta_B \cos \gamma$$

$$A_{CP+} = \frac{\Gamma(B^- \rightarrow D_{CP+} K^-) - \Gamma(B^+ \rightarrow D_{CP+} K^+)}{\Gamma(B^- \rightarrow D^0 K^-) + \Gamma(B^+ \rightarrow \bar{D}^0 K^+)} = \frac{2r_B \sin \delta_B \sin \gamma}{R_{CP+}}$$

$D^0 \rightarrow KK$   
 $D^0 \rightarrow \pi\pi$

➤ 3 parameters, 2 observables

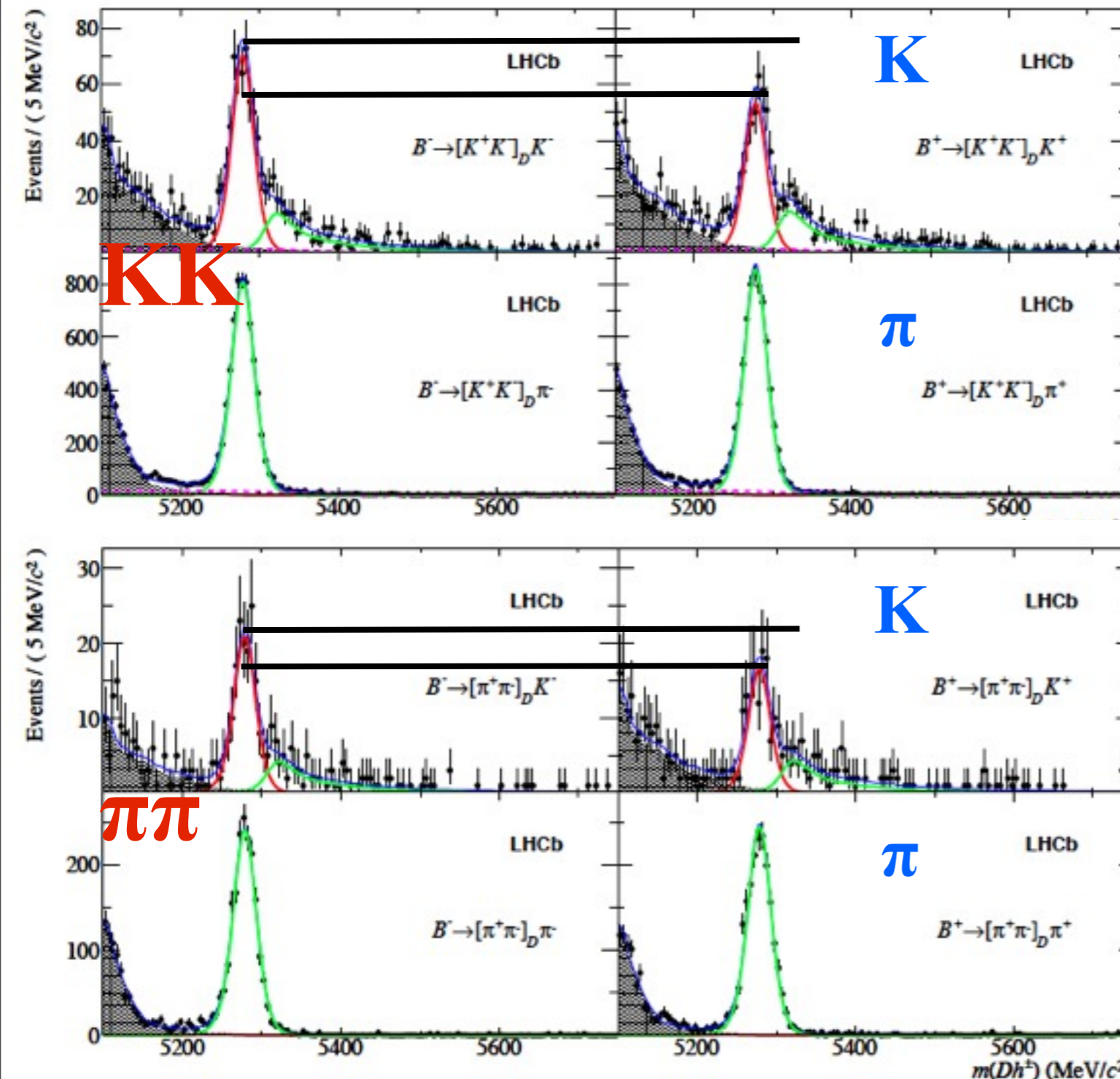
➤ Two GLW channels used and averaged over  $R_{CP}$  and  $A_{CP}$ :  $D^0 \rightarrow KK$ ,  $D^0 \rightarrow \pi\pi$

➤ No CP violation assumed in  $H=\pi$  channels and favored D decay mode

$$R_{CP+} = 1.007 \pm 0.038 \pm 0.012,$$

$$A_{CP+} = 0.145 \pm 0.032 \pm 0.010,$$

4.5 $\sigma$ !!



# $\gamma$ Studies with $B^+ \rightarrow D^0 K^+$ (ADS)

Phys. Lett. B 712 (2012) 203,  
arXiv: 1203.3662

$$R_{ADS} = \frac{\Gamma(B^- \rightarrow D[\rightarrow \pi^- K^+] K^-) + \Gamma(B^+ \rightarrow D[\rightarrow \pi^+ K^-] K^+)}{\Gamma(B^- \rightarrow D[K^- \pi^+] K^-) + \Gamma(B^+ \rightarrow D[\rightarrow K^+ \pi^-] K^+)} = r_B^2 + r_D^2 + 2r_B r_D \cos \gamma \cos(\delta_B + \delta_D)$$

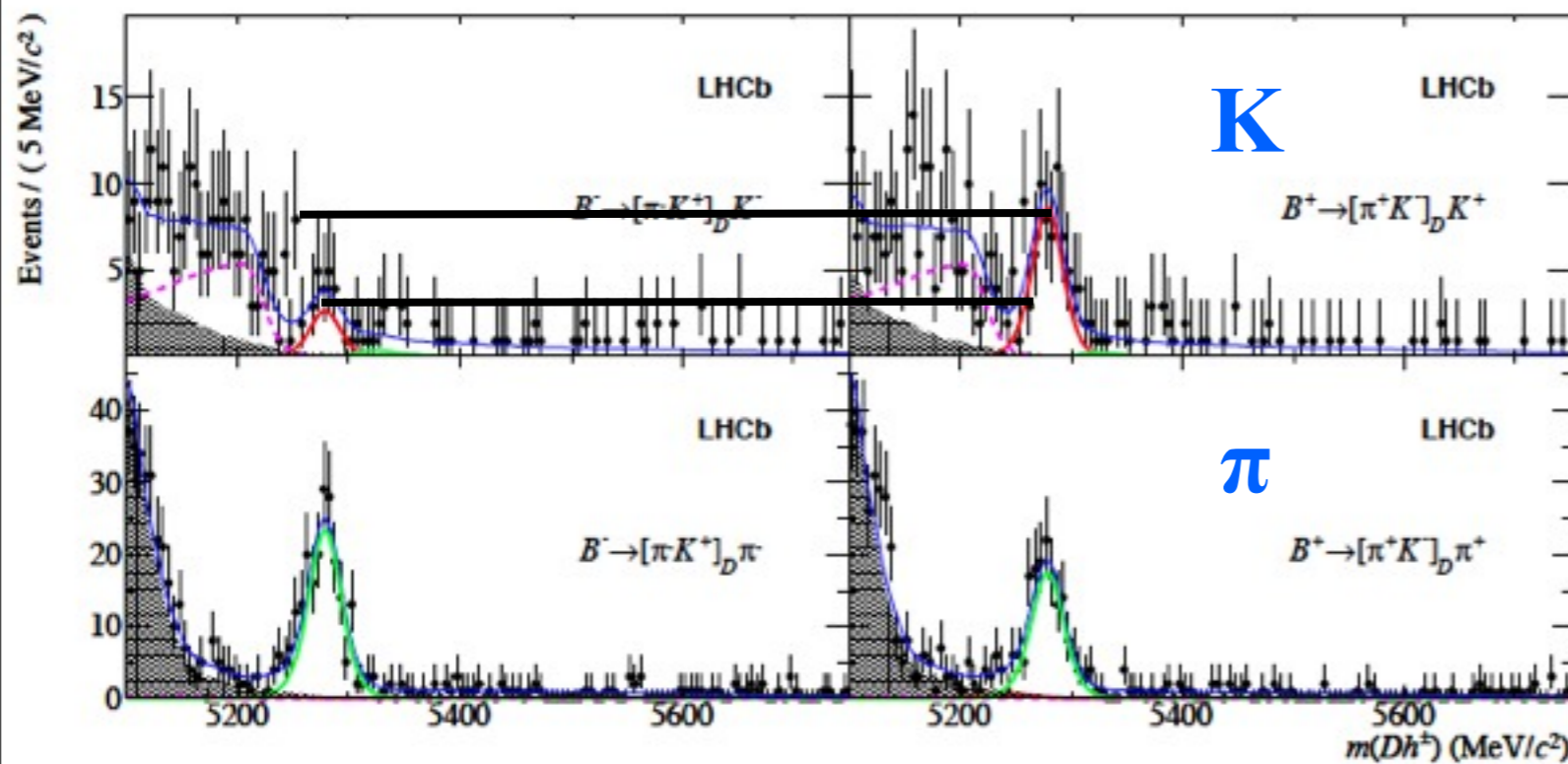
$$A_{ADS} = \frac{\Gamma(B^- \rightarrow D[\rightarrow \pi^- K^+] K^-) - \Gamma(B^+ \rightarrow D[\rightarrow \pi^+ K^-] K^+)}{\Gamma(B^- \rightarrow D[K^- \pi^+] K^-) + \Gamma(B^+ \rightarrow D[\rightarrow K^+ \pi^-] K^+)} = \frac{2r_B r_D \sin \gamma \sin(\delta_B + \delta_D)}{R_{ADS}}$$

➤ 5 parameters, 4 observables + 2 inputs from D decays

CLEO Collaboration, Phys. Rev.D 82(2010) 112006

First observation of  $B^+ \rightarrow D^0 K^+$  ADS mode:  $5.1\sigma$

$D^0 \rightarrow K^- \pi^+$   
 $D^0 \rightarrow K^+ \pi^-$



**B → Dπ channel:**

$$R_{ADS(\pi)} = 0.00410 \pm 0.00025 \pm 0.00005$$

$$A_{ADS(\pi)} = 0.143 \pm 0.062 \pm 0.011$$

**B → DK channel:**

$$R_{ADS(K)} = 0.0152 \pm 0.0020 \pm 0.0004$$

$$A_{ADS(K)} = -0.52 \pm 0.15 \pm 0.02$$

$4.0\sigma$

➤ Combining GLW and ADS modes, we have  $5.8\sigma!$  significance of direct CP violation (first observation)



# $\gamma$ Studies with $B^+ \rightarrow D^0 K^+$ (GGSZ)

Phys. Lett. B 718 (2012) 43,  
arXiv: 1209.5869

➤ Model independent method (using CLEO-c information) with binning on  $D^0 \rightarrow K_s \pi \pi$  and  $D^0 \rightarrow K_s K K$  Dalitz region:

Re-phase of parameters:

$$x_{\pm} = \text{Re}[r_B e^{i(\delta_B \pm \gamma)}] \quad y_{\pm} = \text{Im}[r_B e^{i(\delta_B \pm \gamma)}]$$

Number of events in bins of the Dalitz plot:

$$N_{\pm i}^+ = h_{B^+} \left[ K_{\mp i} + (x_+^2 + y_+^2) K_{\pm i} + 2\sqrt{K_i K_{-i}} (x_+ c_{\pm i} \mp y_+ s_{\pm i}) \right]$$

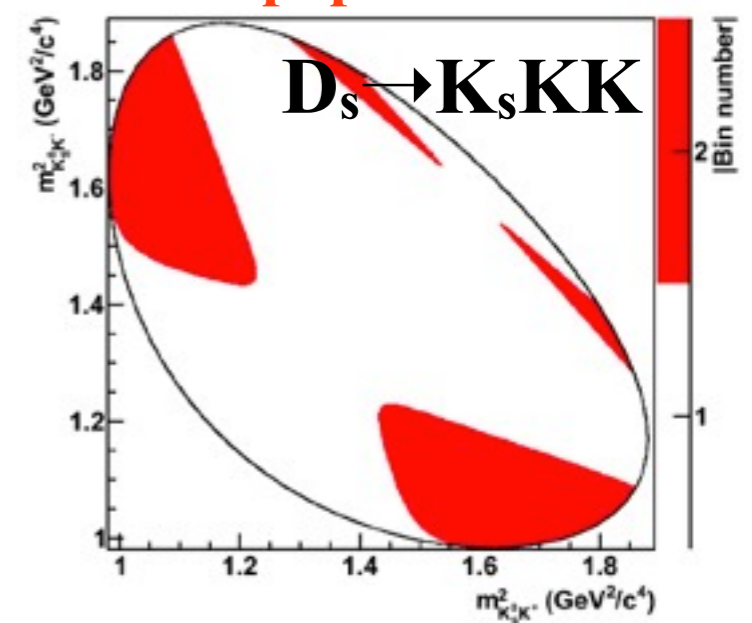
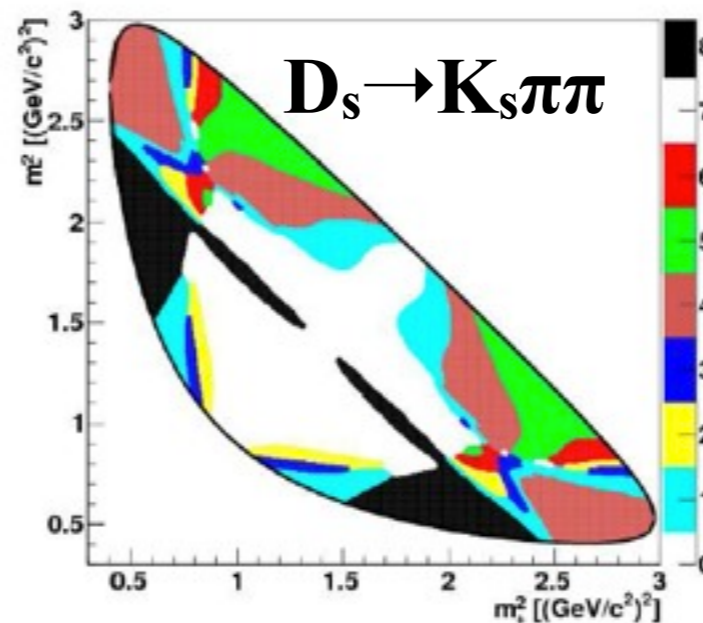
$$N_{\pm i}^- = h_{B^-} \left[ K_{\pm i} + (x_-^2 + y_-^2) K_{\mp i} + 2\sqrt{K_i K_{-i}} (x_- c_{\pm i} \pm y_- s_{\pm i}) \right]$$

CLEO-c information

CLEO Collaboration, Phys. Rev.D 82(2010) 112006

Colors for bin number as in CLEO-c paper

$K_i$  represent Dalitz distribution in flavor-tagged D decays

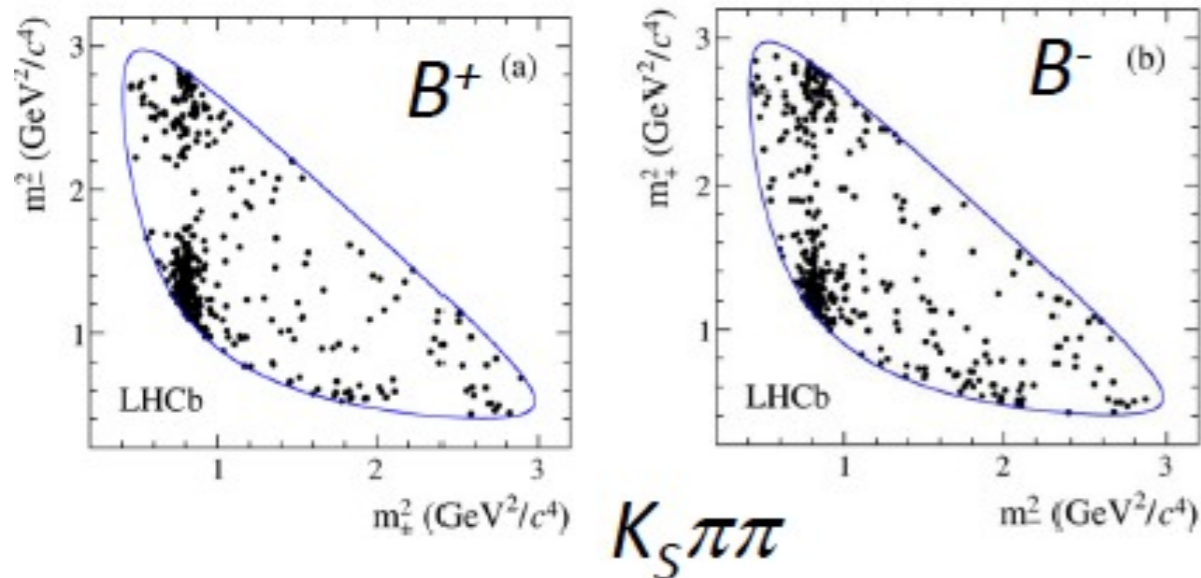


Binning optimized according to Dalitz analysis;  
Deviation only reduces sensitivity but does not introduces bias

# $\gamma$ Studies with $B^+ \rightarrow D^0 K^+$ (GGSZ): Results

Phys. Lett. B 718 (2012) 43,  
arXiv: 1209.5869

➤ Around 660  $K_S \pi \pi$  and 100  $K_S K K$  signal events



$$x_- = (0.0 \pm 4.3 \pm 1.5 \pm 0.6) \times 10^{-2},$$

$$y_- = (2.7 \pm 5.2 \pm 0.8 \pm 2.3) \times 10^{-2},$$

$$x_+ = (-10.3 \pm 4.5 \pm 1.8 \pm 1.4) \times 10^{-2},$$

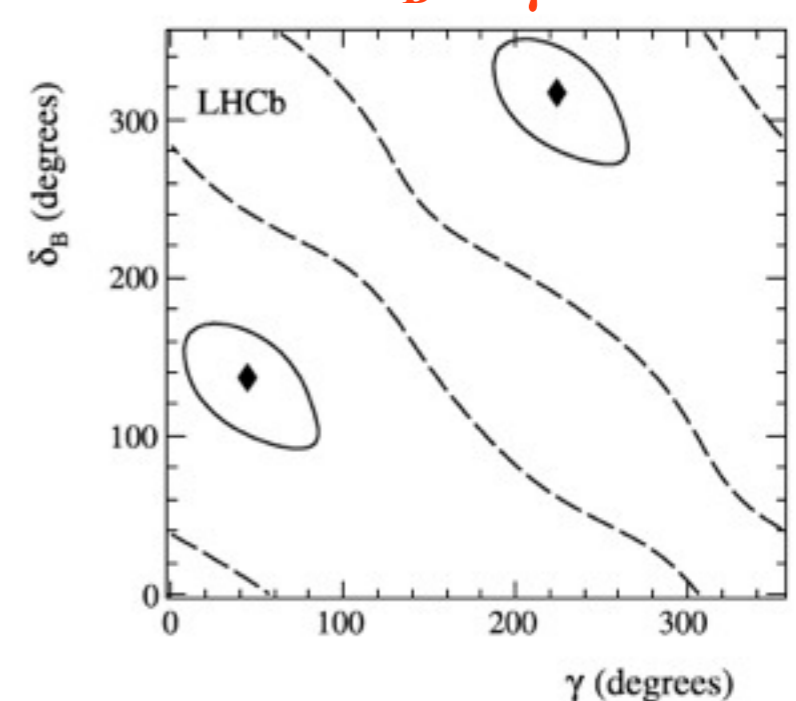
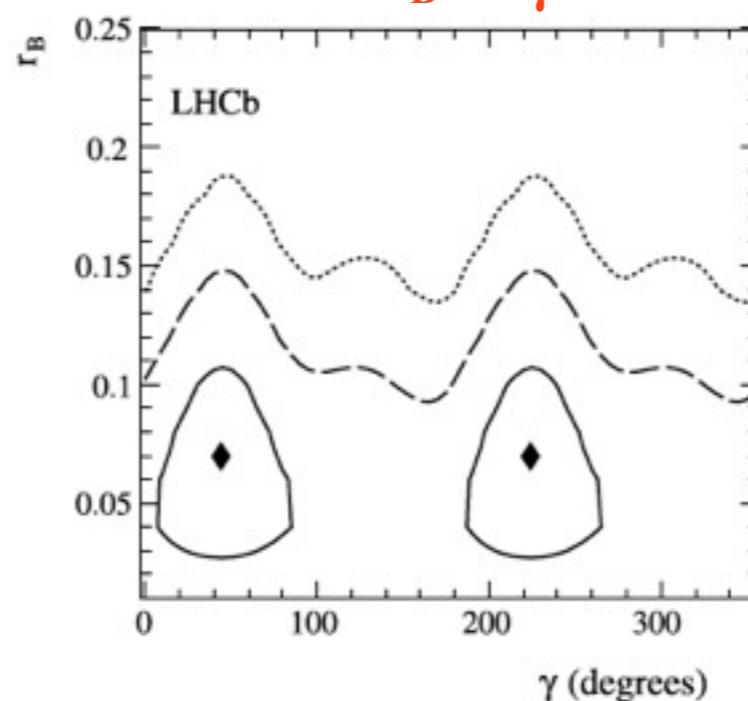
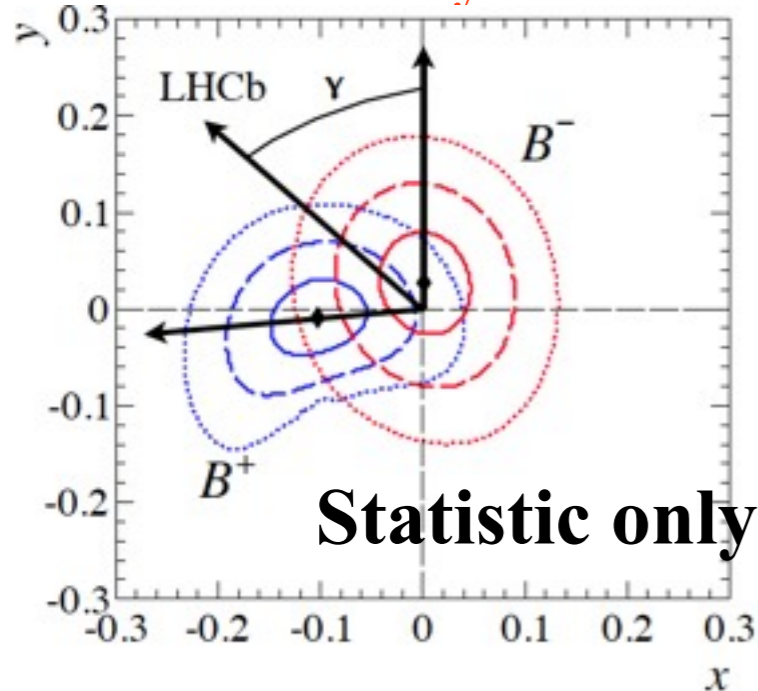
$$y_+ = (-0.9 \pm 3.7 \pm 0.8 \pm 3.0) \times 10^{-2},$$

Stat. Sys. CLEO-c input

Measured x-y contour

Fitted  $r_B$  vs  $\gamma$

Fitted  $\delta_B$  vs  $\gamma$



Statistic only

$$r_B = 0.07 \pm 0.04$$

$$\gamma = (44^{+43}_{-38})^\circ$$

$$\delta_B = (137^{+35}_{-46})^\circ$$

➤  $r_B$  lower than world average (but consistent)  $\rightarrow$  smaller sensitivity to  $\gamma$

➤  $D^0$  decay to  $K\pi\pi\pi$  (similar analysis as 2-Body)

$D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$

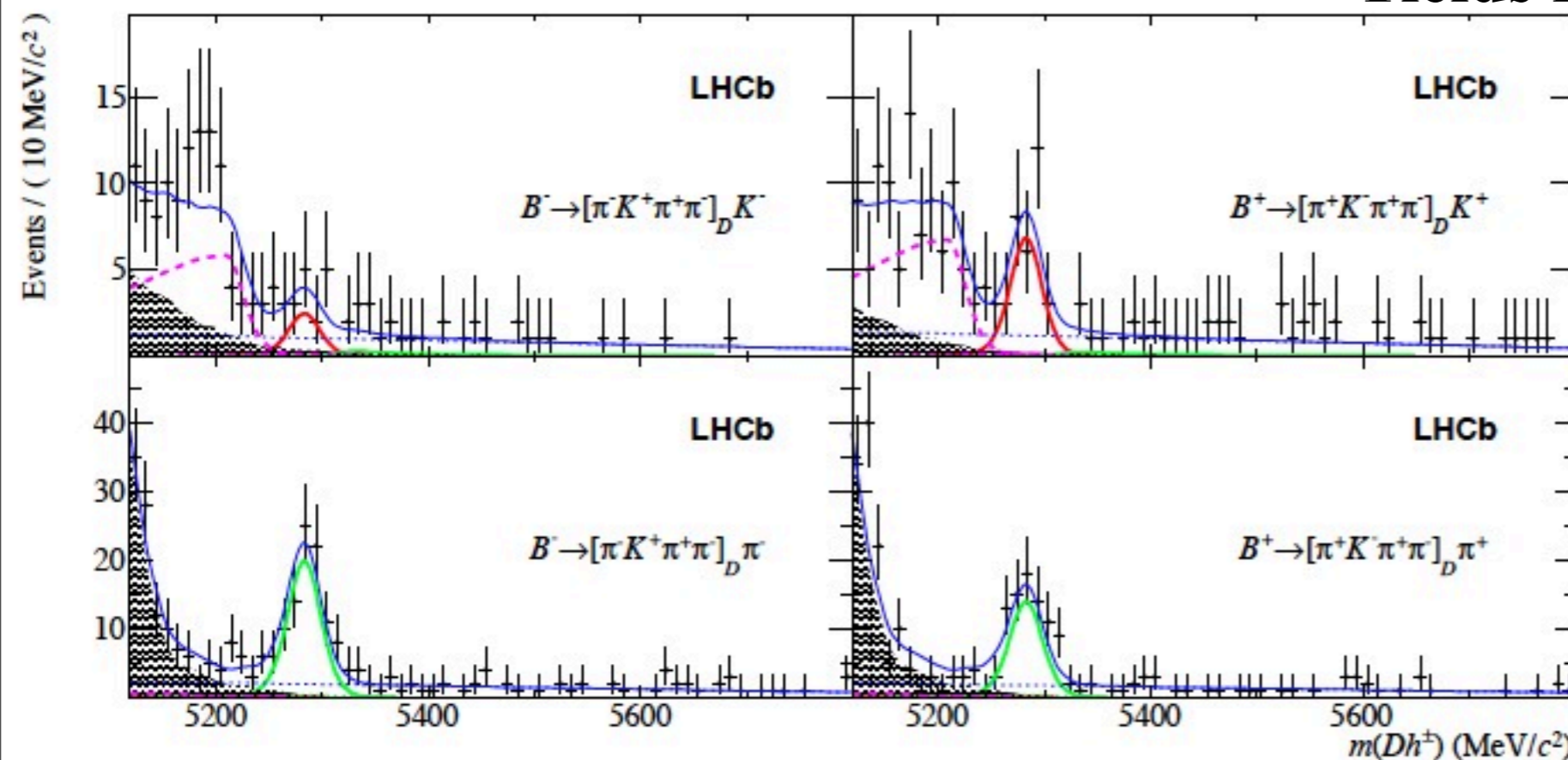
$D^0 \rightarrow K^+ \pi^- \pi^- \pi^+$

Yields for suppressed mode:

$\sim 40 B \rightarrow DK$

First observation:  $5.7\sigma$

$\sim 160 B \rightarrow D\pi > 10\sigma$



Inputs from CLEO-c:  
CLEO Collaboration, Phys. Rev. D80 (2009) 031105, arXiv:0903.4853

$$R_{\text{ADS}(K)}^{K3\pi} = 0.0124 \pm 0.0027$$

$$A_{\text{ADS}(K)}^{K3\pi} = -0.42 \pm 0.22$$

$$R_{\text{ADS}(\pi)}^{K3\pi} = 0.00369 \pm 0.00036$$

$$A_{\text{ADS}(\pi)}^{K3\pi} = +0.13 \pm 0.10$$

➤ Constraint on  $r_B$ :

$$r_B^K = 0.097 \pm 0.011$$

# $\gamma$ Combination with LHCb data: Inputs

Parameters common:  
gamma combination  
improve better than  
simple average

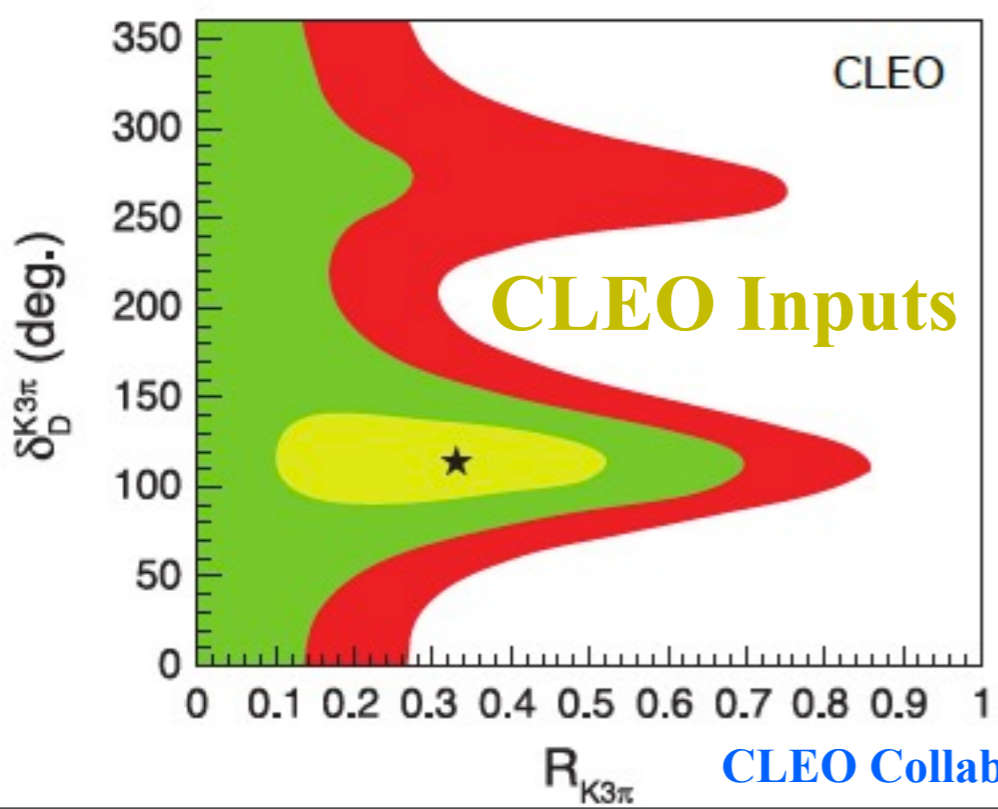
Analysis	$N_{\text{obs}}$	Parameters
$B^+ \rightarrow Dh^+, D \rightarrow hh$ , GLW/ADS	14	$\gamma, \tau_B, \delta_B, \tau_B^\pi, \delta_B^\pi, R_{K/\pi}, \tau_{K\pi}, \delta_{K\pi}, \Delta a_{CP}^{\text{dir}}$
$B^+ \rightarrow DK^+, D \rightarrow K_s^0 h^+ h^-$ , GGSZ	4	$\gamma, \tau_B, \delta_B$
$B^+ \rightarrow Dh^+, D \rightarrow K\pi\pi\pi$ , ADS	7	$\gamma, \tau_B, \delta_B, \tau_B^\pi, \delta_B^\pi, R_{K/\pi}, \tau_{K3\pi}, \delta_{K3\pi}, \kappa_{K3\pi}$
Cleo $D^0 \rightarrow K\pi, D^0 \rightarrow K\pi\pi\pi$	9	$x_D, y_D, \delta_{K\pi}, \delta_{K3\pi}, \kappa_{K3\pi}, \tau_{K\pi}, \tau_{K3\pi}, \mathcal{B}(K\pi), \mathcal{B}(K\pi\pi\pi)$
CP violation in the charm system	2	$A_{CP}^{D \rightarrow KK}, A_{CP}^{D \rightarrow \pi\pi}$
$B^0 \rightarrow DK^{0*}, D \rightarrow hh, K^* \rightarrow K\pi$ , GLW	2	$\gamma, \tau_B^{K^{0*}}, \delta_B^{K^{0*}}, \kappa_B^{K^{0*}}$
$B^+ \rightarrow DK^+\pi^+\pi^-, D \rightarrow K\pi$ , ADS	2	$\gamma, \tau_B^{DK\pi\pi}, \delta_B^{DK\pi\pi}, \kappa_B^{DK\pi\pi}, \tau_{K\pi}, \delta_{K\pi}$
$B^0 \rightarrow D^+\pi^-$ time dependent	5	$\gamma, \lambda_{D+\pi^-}, \delta_{D+\pi^-}, \Delta m_d, \sin 2\beta$
$B_s^0 \rightarrow D_s^+ K^-$ time dependent	5	$\gamma, \lambda_{D_s K}, \delta_{D_s K}, \Delta m_s, \Gamma_s, \Delta\Gamma_s, \phi_s$

Included in Combination

Not Included in Combination

Observed variables

$\gamma, \tau_B$  etc + nuisance parameters



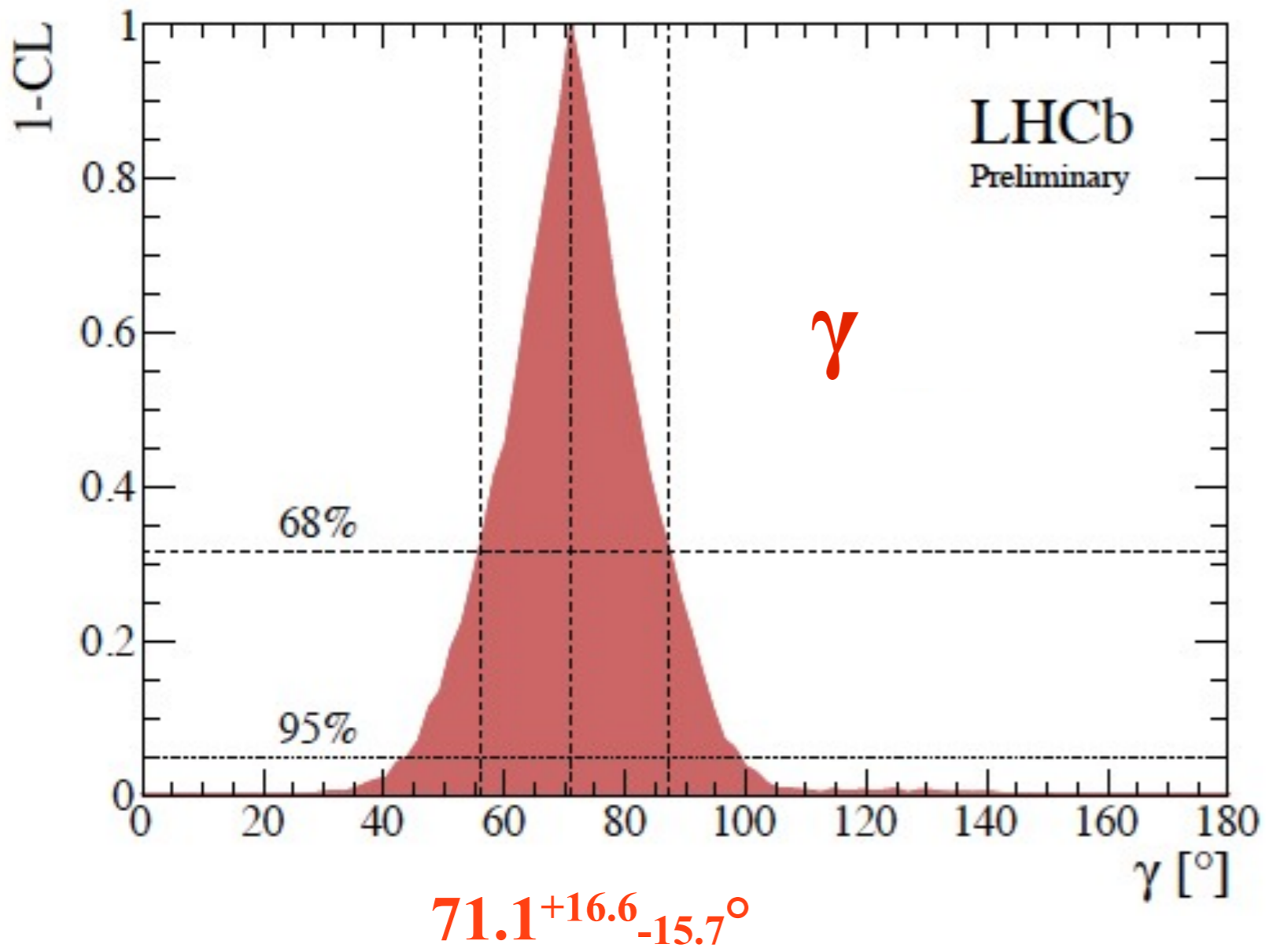
- D mixing ignored at this precision
- CP violation in charm system included

$$\Delta a_{CP}^{\text{dir}} = (-0.656 \pm 0.154) \times 10^{-2}$$

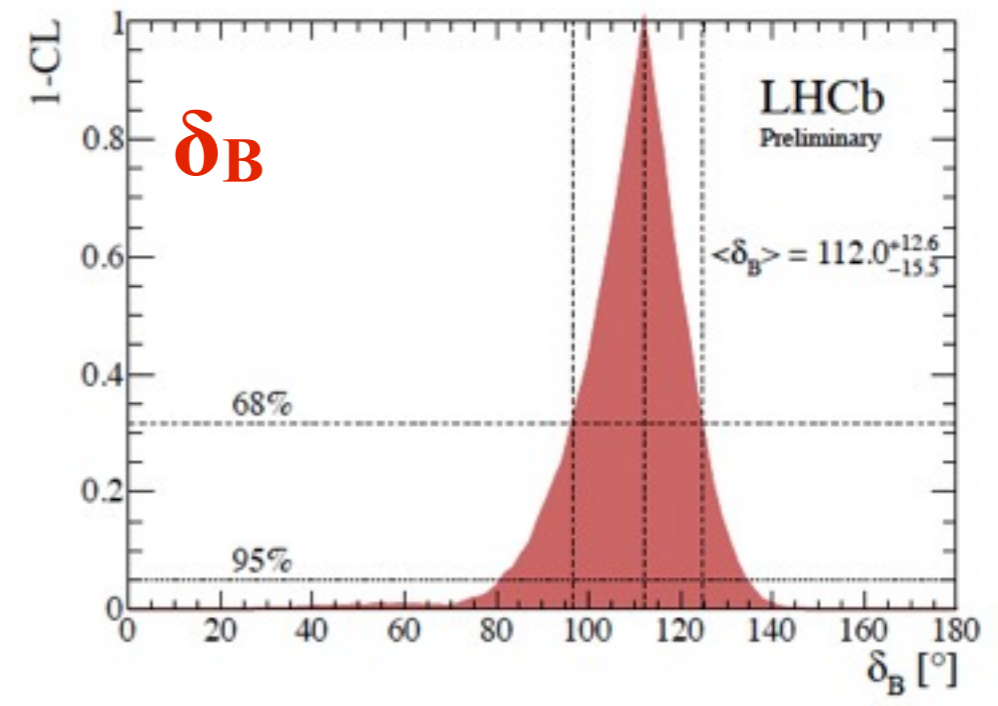
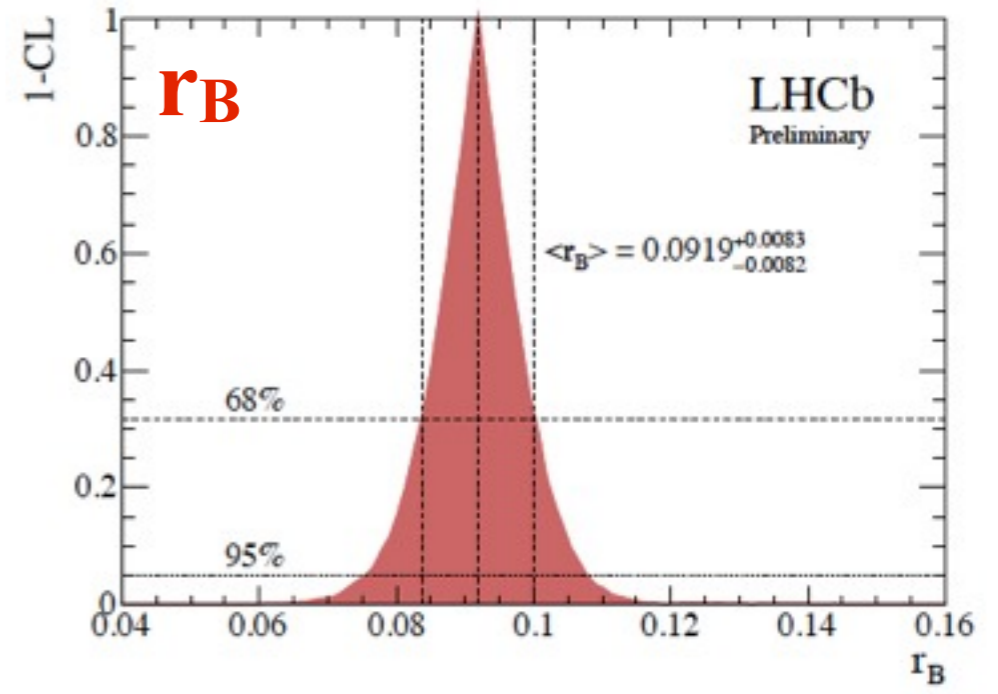
HFAG, arXiv: 1207.1158

- The combination uses frequentist technique

CLEO Collaboration, Phys. Rev. D80 (2009) 031105, arXiv:0903.4853



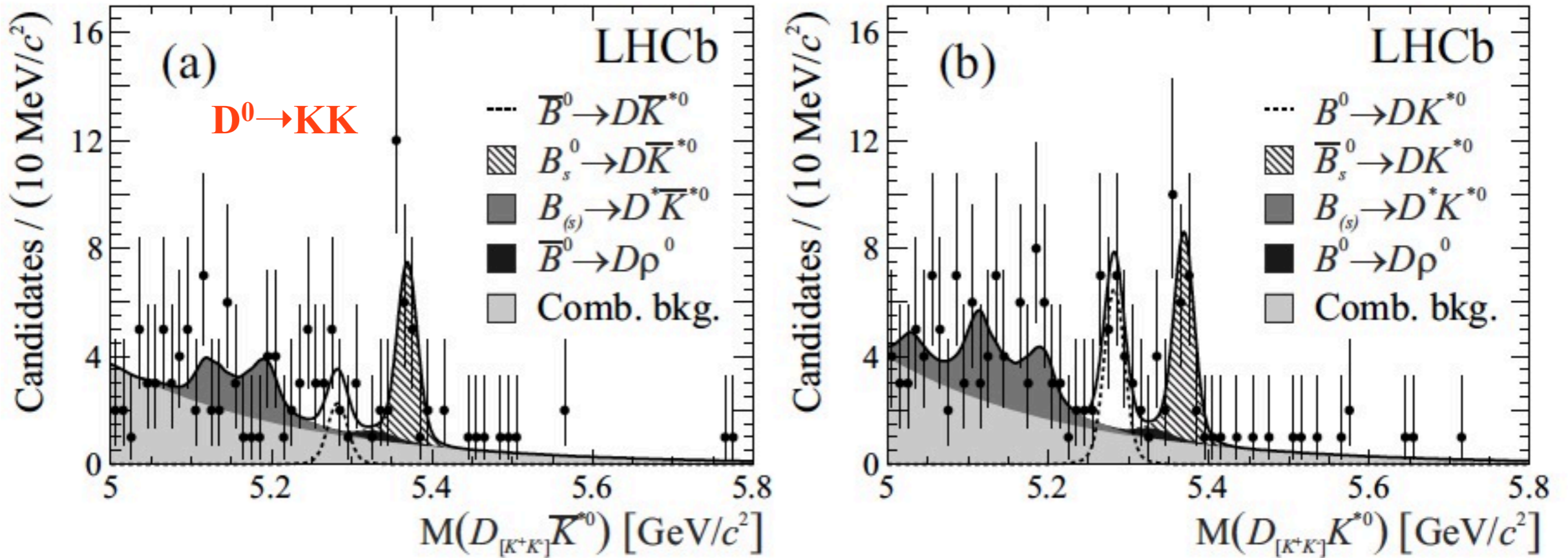
$\gamma \in [55.4, 87.7]^\circ$  @ 68% CL ,  
 $\gamma \in [41.4, 101.3]^\circ$  @ 95% CL ,



- Self-tagging decay:  $B^0 \rightarrow D^0 K^*$  (GLW mode); Direct extension of  $B \rightarrow D^0 K$ ; Dalitz analysis possible

$D^0 \rightarrow K^- K^+$

~30 events



- Decays like  $B^+ \rightarrow D h^+ \pi^+ \pi^-$  also explored:

- For GLW mode: ~120 per  $\text{fb}^{-1}$  signals for  $KK$  and ~60 per  $\text{fb}^{-1}$  for  $\pi\pi$

- For GGSZ mode: ~200 per  $\text{fb}^{-1}$  signals for  $K_s KK$  and  $K_s \pi\pi$

- Other decays like  $B^0 \rightarrow D^0 K \pi$ ,  $B_s^0 \rightarrow D^0 KK$ ,  $B^0 \rightarrow D^0 \pi\pi$ ,  $B_s^0 \rightarrow D_s K$  etc.

# Conclusion

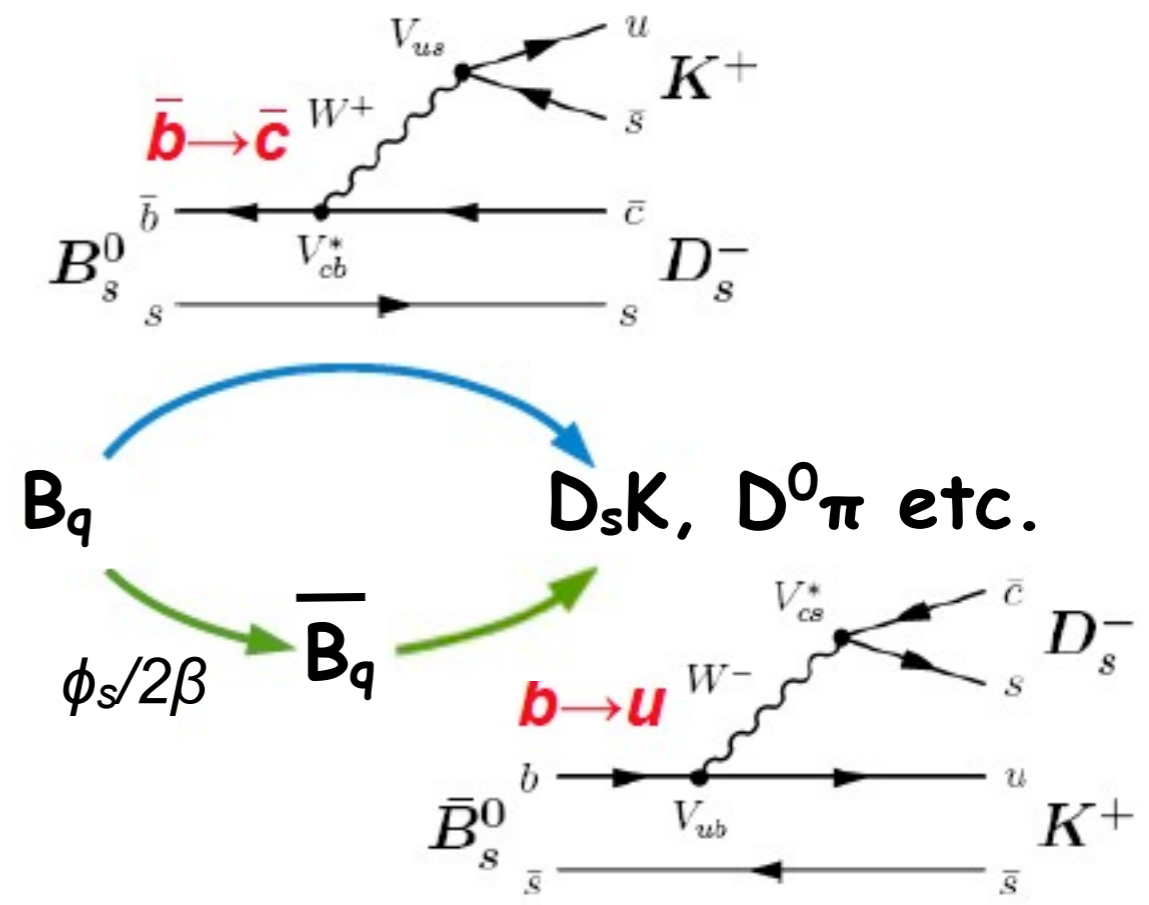
- **LHCb has performed very well during the past three years of data taking**
- **With  $1.0 \text{ fb}^{-1}$  data taken in 2011, it already improves our knowledge on  $\gamma$**
- **None of the channels dominates the sensitivity**
- **Combination of  $B \rightarrow DK$  measurements gives  $\gamma = 71.1^\circ$  with uncertainty  $\sim 16^\circ$**
- **Other channels like  $B_s \rightarrow D_s K$ ,  $B \rightarrow D^0 K^*$  etc. also explored**
- **Stay tuned for more results with  $3 \text{ fb}^{-1}$  data**

**Thank You for your attention**

# $\gamma$ Studies with other $B_s \rightarrow D_s K$ (1)

➤ Interference between  $b \rightarrow u$  and  $b \rightarrow c$  can appear through mixing

➤  $\gamma + \phi_s$  ( $2\beta$ ) can be accessed with  $B_s \rightarrow D_s K$  ( $r_B \sim 0.3$ ),  $B^0 \rightarrow D^0 \pi$  ( $r_B \sim 0.02$ ) etc.



$$\frac{d\Gamma_{B_s \rightarrow f}(t)}{e^{-\Gamma_s t}} \propto \left[ \cosh\left(\frac{\Delta\Gamma_s t}{2}\right) - D_f \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) + C \cos(\Delta m_s t) - S_f \sin(\Delta m_s t) \right]$$

$$\frac{d\Gamma_{\bar{B}_s \rightarrow f}(t)}{e^{-\Gamma_s t}} \propto \left[ \cosh\left(\frac{\Delta\Gamma_s t}{2}\right) - D_f \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) - C \cos(\Delta m_s t) + S_f \sin(\Delta m_s t) \right]$$

**Similar for  $\bar{f}$**

$$D_f = \frac{2r_{D_s K} \cos(\Delta(\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$

$$C = \frac{1 - r_{D_s K}^2}{1 + r_{D_s K}^2}$$

$$S_f = \frac{2r_{D_s K} \sin(\Delta(\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$

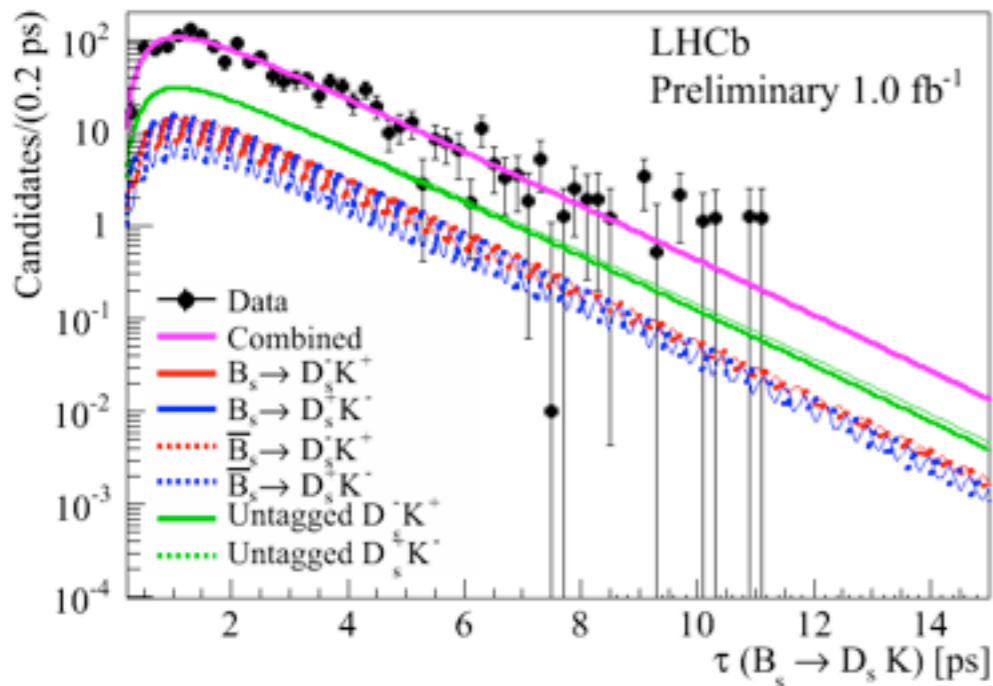
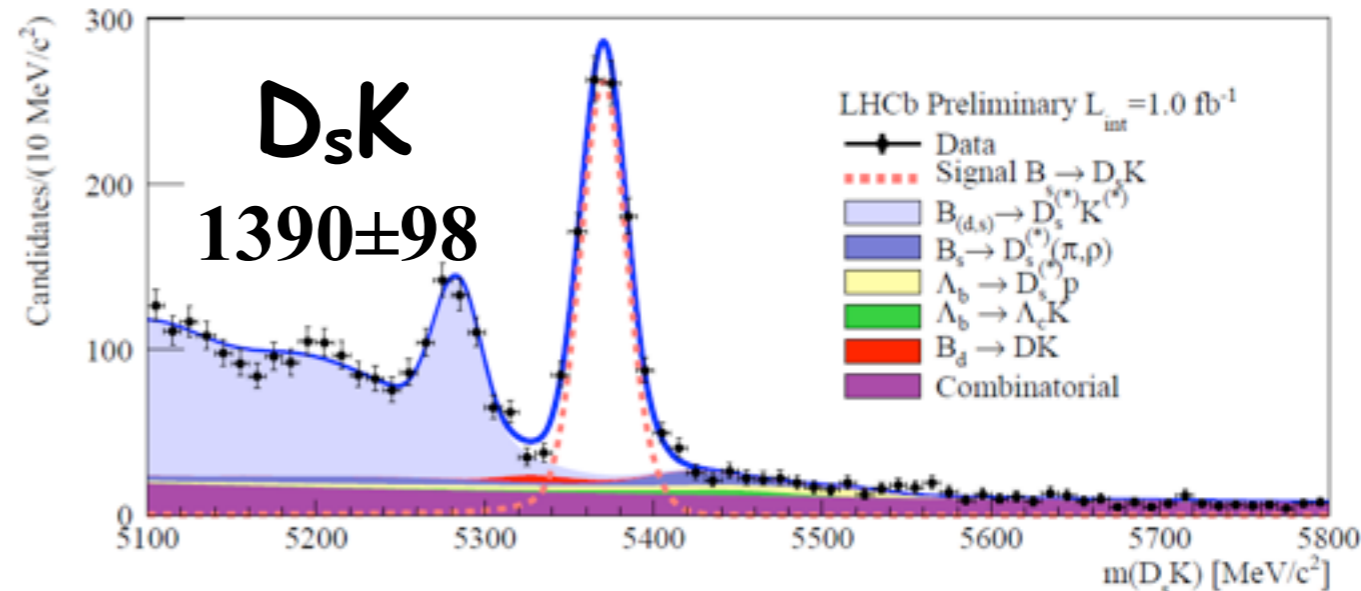
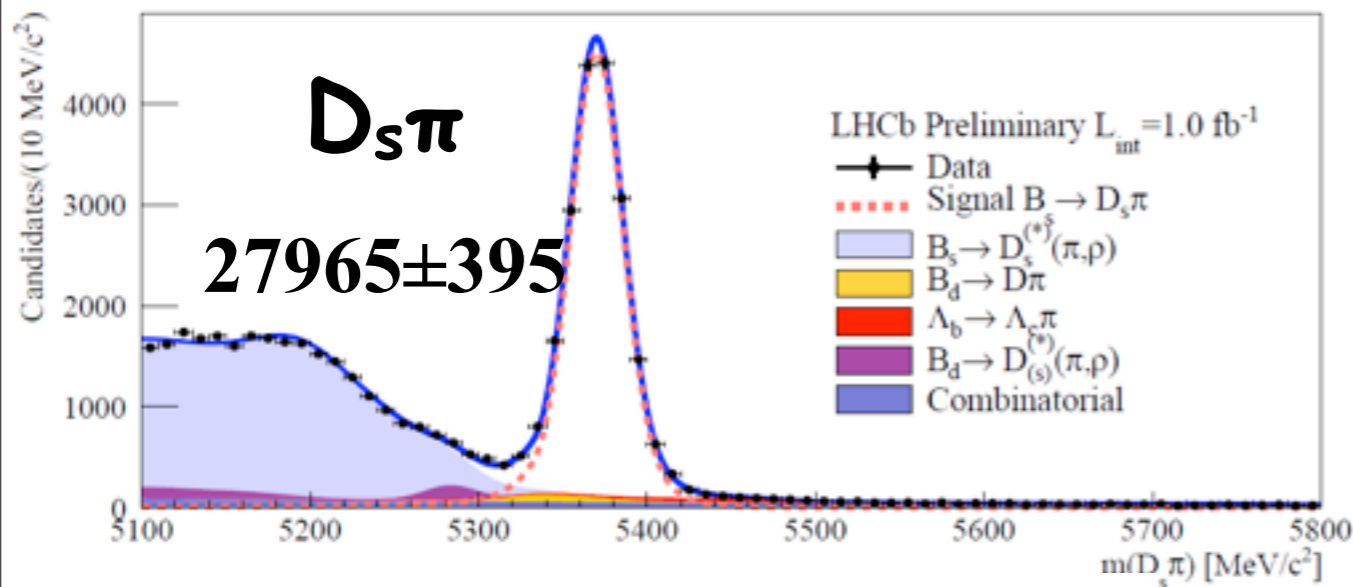
**$D_f$  can be measured due to non zero  $\Gamma_s$**   
**Independent of tagging**

**Tagging info. required**

**Change sign for  $\bar{f}$**



## ➤ Event Yields (with $D_s$ decays to $KK\pi$ , $K\pi\pi$ and $\pi\pi\pi$ )



**Stat. Sys.**

$$C = 1.01 \pm 0.50 \pm 0.23,$$

$$S_f = -1.25 \pm 0.56 \pm 0.24,$$

$$S_{\bar{f}} = 0.08 \pm 0.68 \pm 0.28,$$

$$D_f = -1.33 \pm 0.60 \pm 0.26,$$

$$D_{\bar{f}} = -0.81 \pm 0.56 \pm 0.26,$$

➤ Systematic uncertainties dominated by fixed parameters ( $\Delta m_s$ ,  $\Gamma_s$ ,  $\Delta \Gamma_s$ ), flavor tagging calibration, background description

➤  $\gamma$  extraction ongoing