



Precision Diboson Observables for the LHC

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based on arXiv:1510.08451 (accepted by JHEP)
with Chris Frye, Jakub Scholtz, Matt Strassler



Why precision? Why dibosons?

- entering the era of precision Higgs physics
- ...but not all EW physics easy to tie to Higgs measurements
 - ▶ BSM might not be easy to connect either
whither 750 GeV?
- non-Higgs precision measurements at the LHC are the next frontier

Why precision? Why dibosons?

- entering the era of precision Higgs physics
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whither 750 GeV?
- non-Higgs precision measurements at the LHC are the next frontier
- large part of this effort hinges on precision calculations
many talks here: D. Heymes, M. Worek, A. Huss, F. Dreyer, S. Kallweit ...
- but clever choices of observables can also help
cf. hadronic, Higgs decay ratios
- diboson rates related by $SU(2)_L \times U(1)_Y$ relations
 - ▶ broken at low energies, but restored above the EW scale
 - ▶ is there any way to take advantage of this?

Plan

- **Leading order**
 - ▶ Structure of partonic cross sections
 - ▶ Ratio observables
- Next-to-leading order
 - ▶ NLO corrections for $\sigma(\gamma\gamma)$, $\sigma(Z\gamma)$, $\sigma(ZZ)$
 - ▶ Photon isolation and gluon fusion
- Experimental benefits

(Nearly) massless gauge bosons at high \sqrt{s}

expand around unbroken $SU(2)_L \times U(1)_Y$ (gauge bosons: w^a, b)

- corrections at $(m_{W,Z}/E)^2$



$$bb_1 \equiv bb : |bb\rangle$$

$$wb_3 \equiv wb : \{|w^+b\rangle, |w^3b\rangle, |w^-b\rangle\}$$

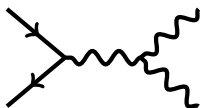
$$ww_1 : |w^-w^+\rangle + |w^-w^+\rangle - |w^3w^3\rangle$$

$$ww_3 : \{|w^+w^3\rangle - |w^3w^+\rangle, |w^+w^-\rangle - |w^-w^+\rangle, |w^3w^-\rangle - |w^-w^3\rangle\}$$

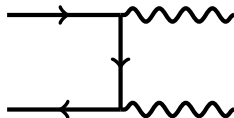
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(1)



(2)

Schematically define coupling-stripped amplitudes:

$$a_1 = (2), \quad a_3 = (1) + (2)$$

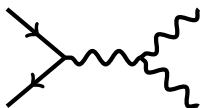
Matrix elements of interest:

$$\begin{aligned} a_1 &\sim \mathcal{M}(bb) && \sim \mathcal{M}(ww_1) && \propto t-, u\text{-channel} \\ a_3 &\sim \mathcal{M}(ww_3) && && \propto s-, t-, u\text{-channel} \end{aligned}$$

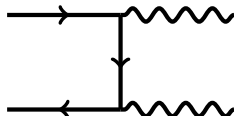
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$$a_1 \sim \mathcal{M}(bb) \sim \mathcal{M}(wb) \sim \mathcal{M}(ww_1)$$

$\propto t-, u\text{-channel}$

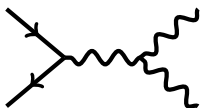
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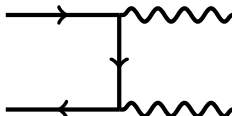
(Nearly) massless gauge bosons at high \sqrt{s}

expand around unbroken $SU(2)_L \times U(1)_Y$ (gauge bosons: w^a, b)

- corrections at $(m_{W,Z}/E)^2$
- need ϕ^a goldstones to unitarize



(1)



(2)



(3)

Schematically define coupling-stripped amplitudes:

$$a_1 = (2), \quad a_3 = (1) + (2), \quad a_L = (3)$$

Matrix elements of interest:

$$a_1 \sim \mathcal{M}(bb) \sim \mathcal{M}(wb) \sim \mathcal{M}(ww_1)$$

$$a_3 \sim \mathcal{M}(ww_3)$$

$$a_L \sim \mathcal{M}(\phi\phi)$$

$$\propto t\text{-, } u\text{-channel}$$

$$\propto s\text{-, } t\text{-, } u\text{-channel}$$

$$\propto s\text{-channel}$$

Amplitudes

at high energies

boson statistics fix amplitudes under $\hat{t} \leftrightarrow \hat{u}$

- a_1, a_L symmetric
- a_3 antisymmetric

$\Rightarrow a_3$ vanishes at threshold, $\text{Re}(a_1^\dagger a_3)$ vanishes in asymmetries

$$\begin{aligned} |a_1|^2 &= \frac{\hat{t}}{\hat{u}} + \frac{\hat{u}}{\hat{t}} \\ 2\text{Re}(a_1^\dagger a_3) &= \frac{\hat{t} - \hat{u}}{2\hat{s}} + \frac{1}{4} \left(\frac{\hat{t}}{\hat{u}} - \frac{\hat{u}}{\hat{t}} \right) \\ |a_3|^2 &= \frac{\hat{u}\hat{t}}{4\hat{s}^2} - \frac{1}{8} + \frac{1}{32} \left(\frac{\hat{t}}{\hat{u}} + \frac{\hat{u}}{\hat{t}} \right) \\ |a_L|^2 &= \frac{\hat{u}\hat{t}}{4\hat{s}^2} \end{aligned}$$

Amplitudes

with mass corrections

boson statistics fix amplitudes under $\hat{t} \leftrightarrow \hat{u}$

- a_1, a_L symmetric
- a_3 antisymmetric

$\Rightarrow a_3$ vanishes at threshold, $\text{Re}(a_1^\dagger a_3)$ vanishes in asymmetries

$$|A_1|^2 = (\hat{t}\hat{u} - m_1^2 m_2^2) \left(\frac{1}{\hat{t}^2} + \frac{1}{\hat{u}^2} \right) + \frac{2\hat{s}(m_1^2 + m_2^2)}{\hat{t}\hat{u}}$$

$$\begin{aligned} \text{Re}(A_1^\dagger A_3) &= P_s \left(\hat{t}\hat{u} - m_1^2 m_2^2 - \hat{s}(m_1^2 + m_2^2) \right) \left(\frac{1}{\hat{u}} - \frac{1}{\hat{t}} \right) \\ &\quad + \frac{1}{4} (\hat{t}\hat{u} - m_1^2 m_2^2) \left(\frac{1}{\hat{u}^2} - \frac{1}{\hat{t}^2} \right) \end{aligned}$$

$$|A_3|^2 = \dots$$

$$|A_L|^2 = P_s^2 \left(\hat{t}\hat{u} - m_1^2 m_2^2 + 2\hat{s}(m_1^2 + m_2^2) \right)$$

finite m effects have uniform structure

$\gamma\gamma, Z\gamma, ZZ$ at LO

$$\frac{d\hat{\sigma}_{q\bar{q}\rightarrow V_0^1 V_0^2}}{d\hat{t}} = \frac{C_{q\bar{q}\rightarrow V_0^1 V_0^2}}{\hat{s}^2} |A_1|^2$$

$$\gamma = c_W b + s_W w^3,$$

$$Z = c_W w^3 - s_W b$$

$$\gamma\gamma, Z\gamma, ZZ \propto bb, wb, ww_1$$

where

$$C_{q\bar{q}\rightarrow\gamma\gamma} = \frac{1}{2} \frac{\pi\alpha_2^2 s_W^4}{N_c} 2Q^4$$

$$C_{q\bar{q}\rightarrow Z\gamma} = \frac{\pi\alpha_2^2 s_W^2 c_W^2}{N_c} (L^2 Q^2 + R^2 Q^2)$$

$$C_{q\bar{q}\rightarrow ZZ} = \frac{1}{2} \frac{\pi\alpha_2^2 c_W^4}{N_c} (L^4 + R^4)$$

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$$L = T_3 - Y_L t_W^2, \quad R = -Y_R t_W^2$$

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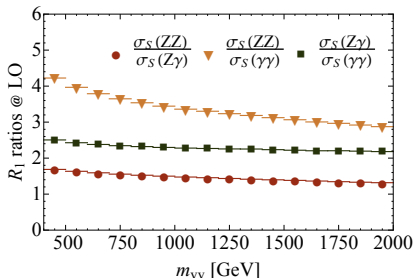
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where

$V_1^0 V_2^0$	$\mathcal{L}_{12}^u \cdot 10^5$	$\mathcal{L}_{12}^d \cdot 10^5$
$\gamma\gamma$	1.2	0.07
$Z\gamma$	2.2	0.7
ZZ	1.6	3.3



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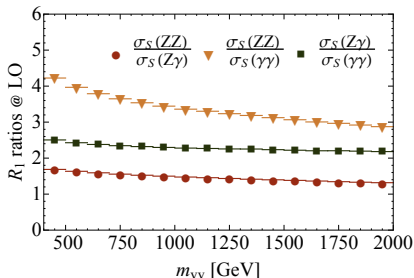
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PDFs mostly cancel – $u\bar{u}$ dominates



$W^\pm\gamma, W^\pm Z$ at LO

$W^\pm\gamma$ and $W^\pm Z$ built from wb and $ww_3 \implies$ Need A_1 and A_3 .

Need A_L for $\phi^\pm\phi^3$ component of $W^\pm Z$.

$$\frac{d\hat{\sigma}_{u\bar{d}\rightarrow W^\pm\gamma}}{d\hat{t}} = \frac{\pi|V_{ud}|^2\alpha_2^2 s_W^2}{N_c \hat{s}^2} \left(\frac{Y_L^2}{2} |A_1|^2 \pm 2Y_L \text{Re}(A_1^\dagger A_3) + |A_3|^2 \right)$$

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Numerically small

$\implies W\gamma/WZ \sim \tan^2\theta_W$

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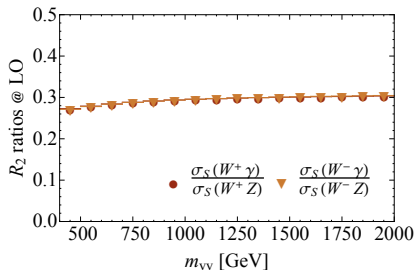
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Numerically small

$\implies W\gamma/WZ \sim \tan^2 \theta_W$

Radiation zero at threshold

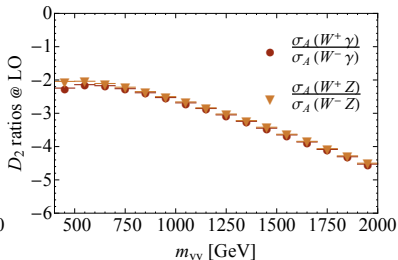
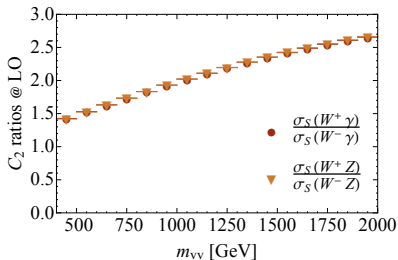
$\implies W\gamma/WZ \sim 0.19$



CP symmetry controls W^-V^0 rates:

$$d\hat{\sigma}_S(u\bar{d} \rightarrow W^+V^0) = d\hat{\sigma}_S(d\bar{u} \rightarrow W^-V^0)$$

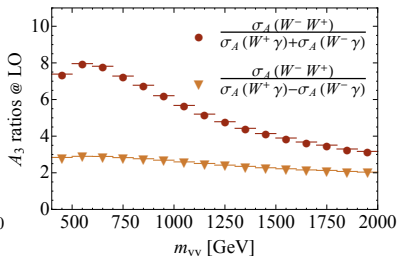
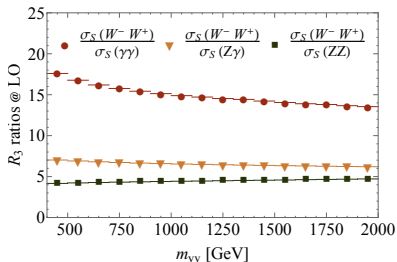
$$d\hat{\sigma}_A(u\bar{d} \rightarrow W^+V^0) = -d\hat{\sigma}_A(d\bar{u} \rightarrow W^-V^0)$$



W^+W^- built from $ww_1, ww_3, \phi^+\phi^-$

Very similar to $W^\pm\gamma$

$$\frac{\sigma_A(W^+W^-)}{a\sigma_A(W^+\gamma) + b\sigma_A(W^-\gamma)} \sim \frac{\mathcal{L}_{u\bar{u}}^A - \mathcal{L}_{d\bar{d}}^A}{4|V_{ud}|^2 s_W^2 Y_L (a\mathcal{L}_{ud}^A - b\mathcal{L}_{d\bar{u}}^A)}$$



Beyond leading order

- QCD cancellations?
 - ▶ how large are the shifts?
 - ▶ $SU(2)_L \times U(1)_Y$ relations help – where do they fail?
 - ▶ residual uncertainties?
- EW corrections?
- Big issue: the radiation zero
 - ▶ LO relations may receive large corrections where present
- Start with $V_1^0 V_2^0$
 - ▶ No radiation zero
 - ▶ Fully reconstructed (only $Z \rightarrow \ell^+ \ell^-$ here)
 - ▶ Good statistics (ZZ tougher)

NLO corrections to diboson production

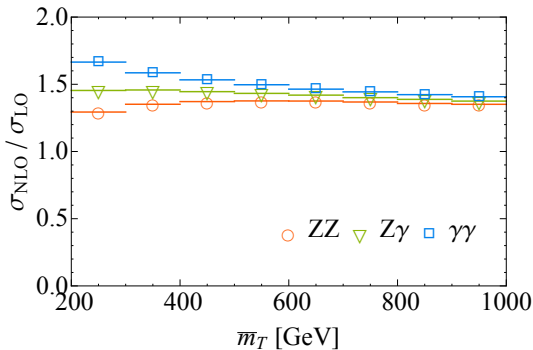
EW processes at LHC typically have large $O(\alpha_s)$ corrections

$qg \rightarrow V_1 V_2 q$ appears at $O(\alpha_s)$, and $f_g \gg f_{\bar{q}}$

Large uncertainties if distributions are “effectively LO” somewhere in PS

$$\bar{m}_T = \frac{1}{2}(m_{T1} + m_{T2}) = \min. E \text{ at } \theta_{CM} = \pi/2$$

Radiation can never reduce this variable



NLO corrections to diboson production

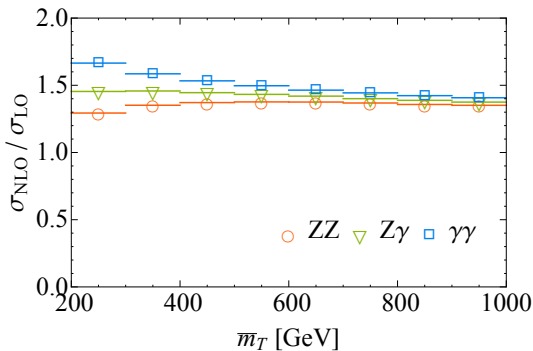
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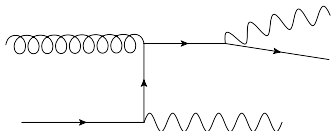
Choose cuts to avoid generating large logs anywhere in phase space

$$H_T < \frac{1}{2} p_{T,\min}^V, \quad p_{T,\min}^V > \frac{1}{2} p_{T,\max}^V$$

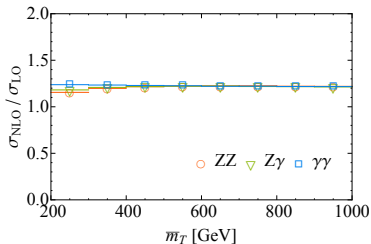
Fixed order calculation reliable



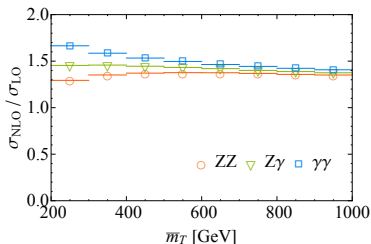
Complications in QCD corrects



divergence in qg process when $q\gamma$ are collinear
cut region out of phase space, or absorb into fragmentation function
large logarithm after regulation \implies need tight γ isolation

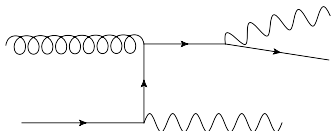


tight isolation



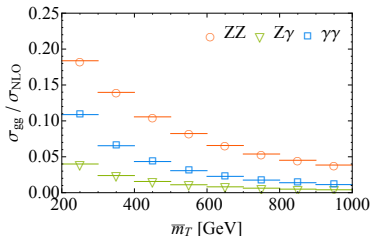
loose isolation

Complications in QCD corrects



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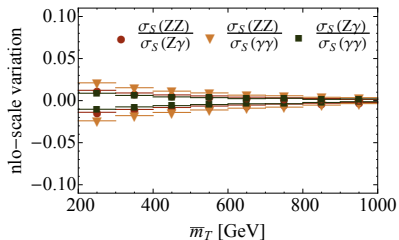
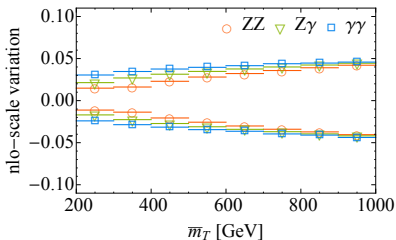
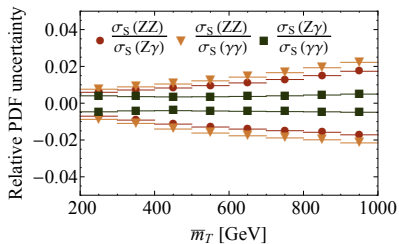
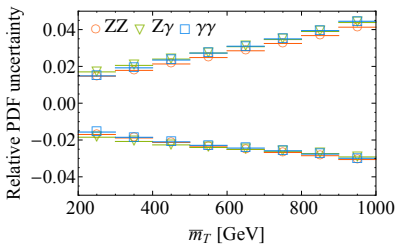
$gg \rightarrow V_1^0 V_2^0$
 \Rightarrow formally NNLO, numerically large



Both effects decrease in importance at high energy

Uncertainties: σ vs. R_{1i}

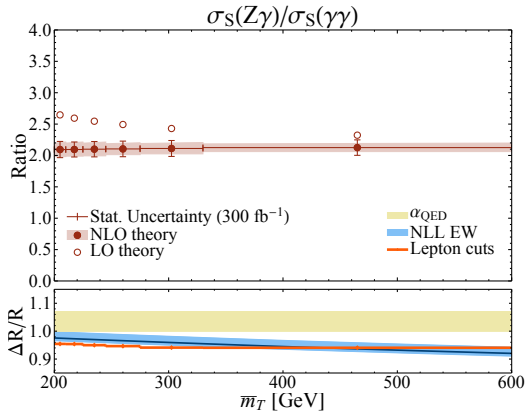
PDFs and scale choices



both PDF and scale uncertainties at the 1–2% level in ratios

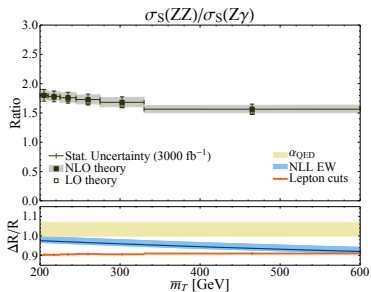
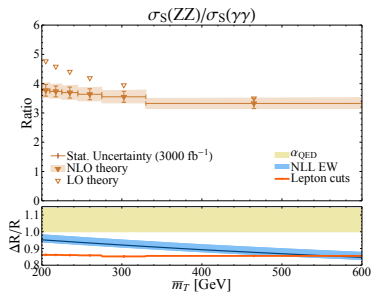
Predicted ratios

$Z\gamma/\gamma\gamma$ at 300 fb^{-1}



Predicted ratios

The other ratios at 3000 fb^{-1}



Summary & outlook

$SU(2)_L \times U(1)_Y$ structure of diboson rates at LO suggests points to studying certain observables

ratio observables based on this structure:

low uncertainties, small QCD corrections

candidates for (even) high(er)-precision calculation

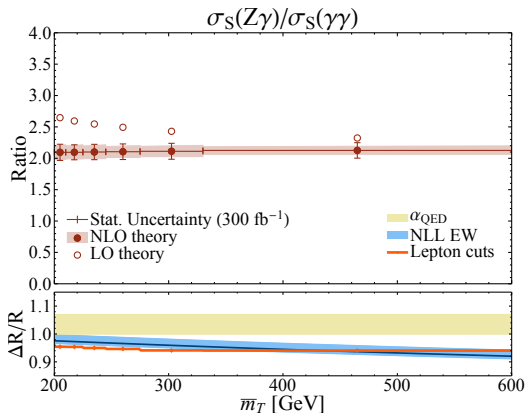
certainly useful for SM studies

need to see if sensitivity to new physics improved

reliable characterization of new resonances?

increased sensitivity to non-resonant effects?

Ratios for precision! Ratios for understanding!



Backup slides

Variable bin widths

Problem: very few Z decays to leptons

$V_1 V_2$	$N_f + N_b$	$N_f - N_b$
$\gamma\gamma$	12 000	0
$Z\gamma$	2000	0
ZZ	220	0
$W^+\gamma$	3300	-500
$W^-\gamma$	2100	220
W^+Z	790	33
W^-Z	520	-16
W^-W^+	9500	-430

Choose bin widths for 5% statistical uncertainty.

$R_{1a} = \sigma_S(Z\gamma)/\sigma_S(\gamma\gamma)$ not statistics limited with 300 fb^{-1}

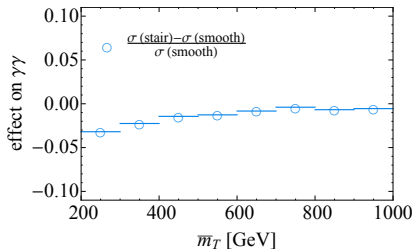
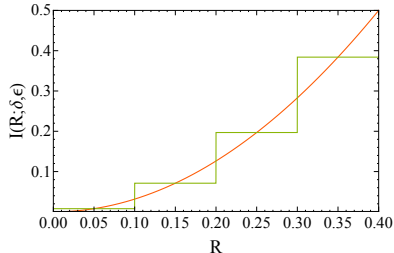
Others will have to wait until 3000 fb^{-1}

Staircase isolation

“Practical” smooth-cone isolation:

- stairs of width $\Delta R = 0.1$
- heights match smooth cone at midpoint
- never take heights below 25 GeV (pileup/resolution)

Minimize sensitivity to fragmentation functions, protect against large log at small cutoff. Experimentally viable.



Uncertainty budget

Effect	R_{1a} ($Z\gamma/\gamma\gamma$)	R_{1b} ($ZZ/\gamma\gamma$)	R_{1c} ($ZZ/Z\gamma$)	Comments
$qq \rightarrow VVqq$	2–3%	3–3.5%	1.5–2.5%	extrapolating $p_{T,\min}^j \rightarrow 0$
μ_R, μ_F (gg)	0.5–1%	1%	1–2%	uses NLO $gg \rightarrow \gamma\gamma$
μ_R, μ_F (NLO)	0.5–1%	1.5–2.5%	1–1.5%	varied independently
PDF	0.5%	1–1.5%	0.5–1%	MSTW2008 using MCFM
γ isolation	< 0.1%	< 0.1%	< 0.1%	Uncertainty in frag. fun.
α_{QED}	7%	14%	7%	Fully correlated
EW (LL)	+2% –1%	+3% –1%	+2% –1%	EFT scale uncertainty