

**Charm & bottom cross sections  
in pp,pp̄ collisions: data vs NNLO**

**Moriond QCD 2017**

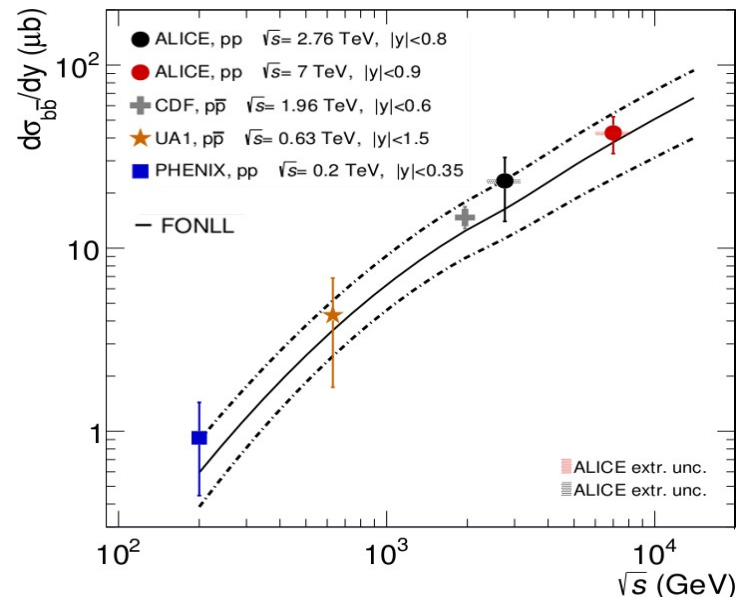
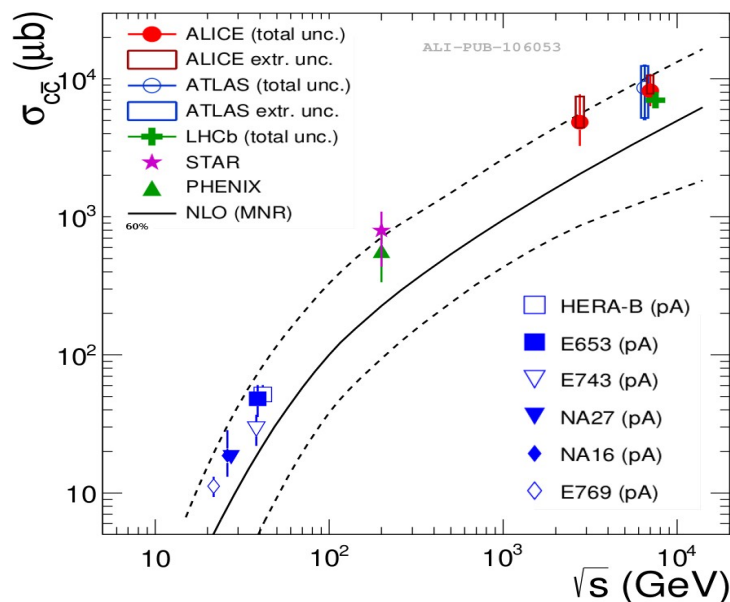
**La Thuile – 27<sup>th</sup> March 2017**

**David d'Enterria**

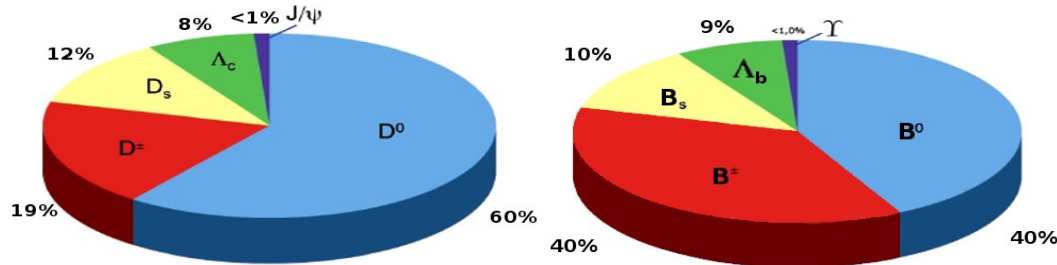
**CERN**

# Charm & bottom production in pp, p $\bar{p}$ colls.

- **Charm & bottom** cross sections in pp collisions increase significantly with c.m. energy. At the LHC, they represent  $\sim 20\%, \sim 1\%$  of  $\sigma_{inel}$ :



- **Experimentally**, one measures the c,b-quark fragmentation products (i.e. **D,B mesons,  $\Lambda$  baryons**) plus quarkonia bound states:



Most of total x-sections based on fraction of decay channels + model-dependent extrapolations over  $(p_T, y)$

# Calculation of heavy-Q x-sections in pp,p $\bar{p}$

- Charm/bottom/top production have **intrinsic hard scales** ( $m_Q \sim 1.7, 4.8, 173 \text{ GeV}$ ) that allow for application of **pQCD framework** to compute their cross sections.

- pQCD **factorization theorem**:

$$\sigma_{Q+X}[s, m_Q] \simeq \sum_{i,j} \int_0^1 dx_i \int_0^1 dx_j f_i^A(x_i, \mu_F) f_j^B(x_j, \mu_F) \tilde{\sigma}_{ij \rightarrow Q+X}[x_i, x_j, m_Q, \mu_F, \mu_R]$$

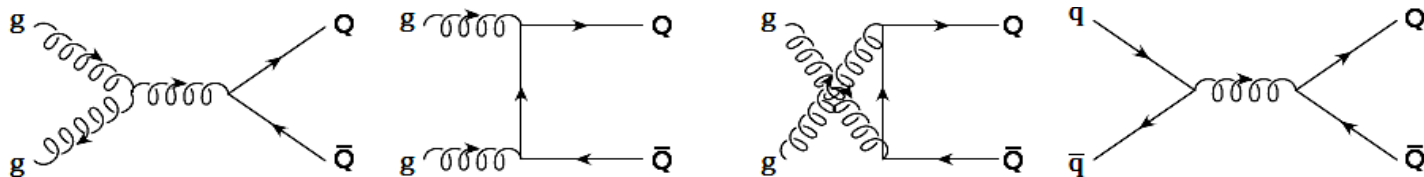
Sum over  
**active  
flavours**

**Parton densities** in proton:  
Evaluated at momentum  
fraction  $x$  & scale  $Q = \mu_F$

**Partonic subprocesses  
cross sections**, expanded  
in powers of  $\alpha_s$ :

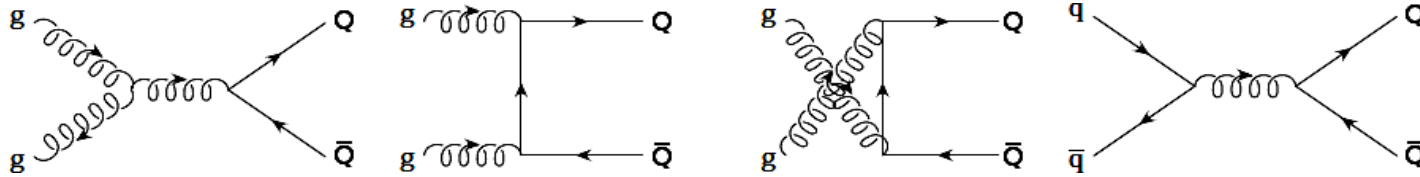
$$\tilde{\sigma}_{ij \rightarrow Q+X}[m_Q, \mu_F, \mu_R] = \frac{\alpha_s^2(\mu_R)}{m_Q^2} [\hat{\sigma}_{\text{LO}} + \alpha_s(\mu_R) \hat{\sigma}_{\text{NLO}} + \alpha_s^2(\mu_R) \hat{\sigma}_{\text{NNLO}} + \dots]$$

- Cross sections clearly dominated by **gluon-gluon fusion** processes

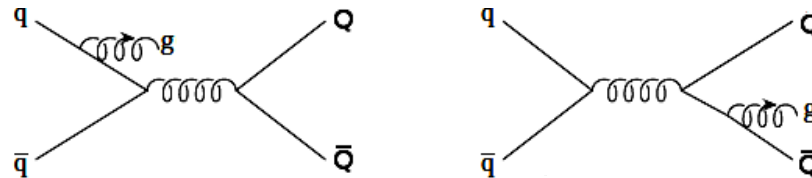


# Heavy-Quark production in $pp, p\bar{p}$ (LO, NLO)

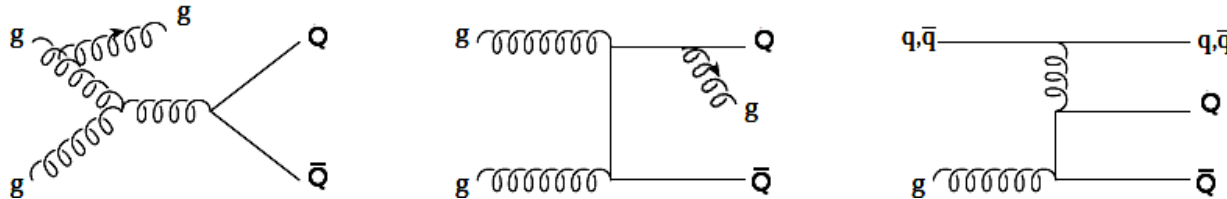
## Leading-order (LO) QCD processes:



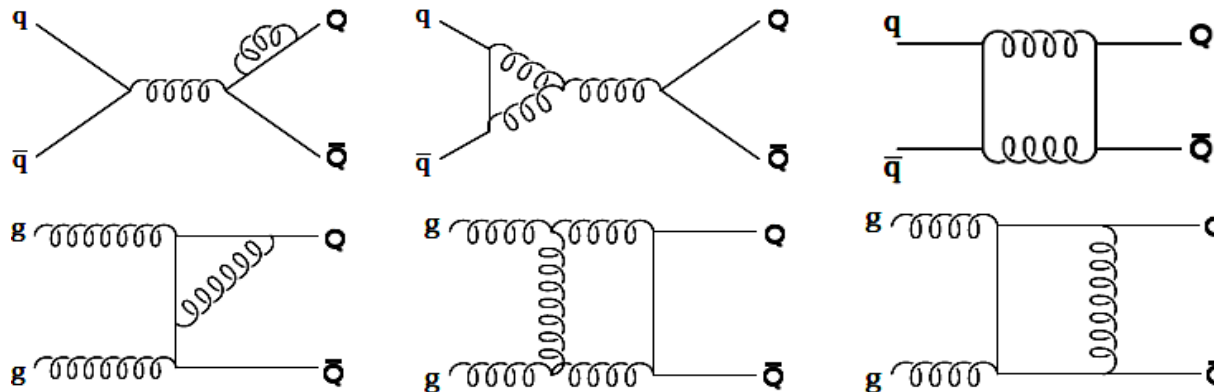
## Next-to-leading-order (NLO) QCD processes:



NLO real:



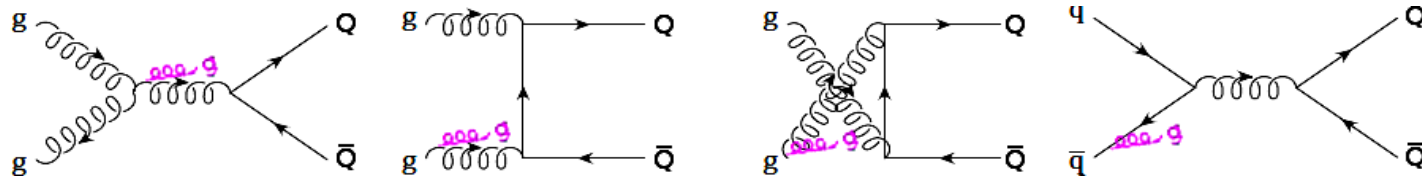
NLO virtual:



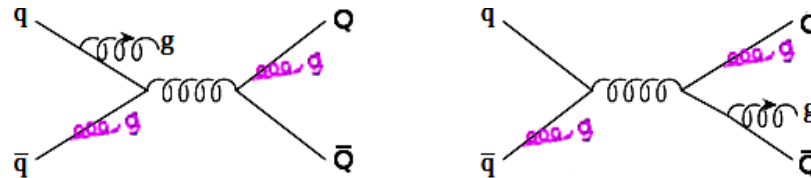
Mangano,  
Nason,  
Ridolfi,  
(MNR)  
...  
[1992]

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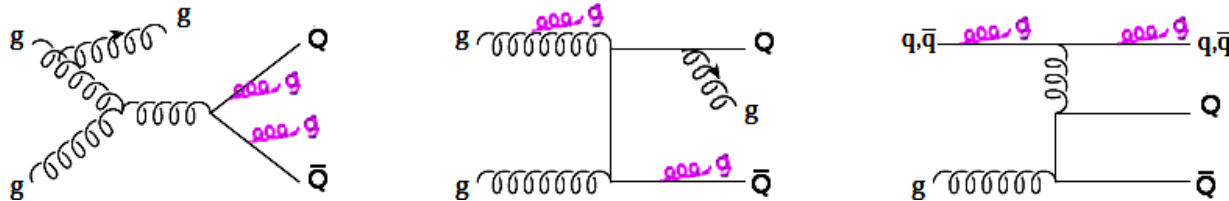
- LO + leading-log (LL) soft gluon resummation QCD processes:



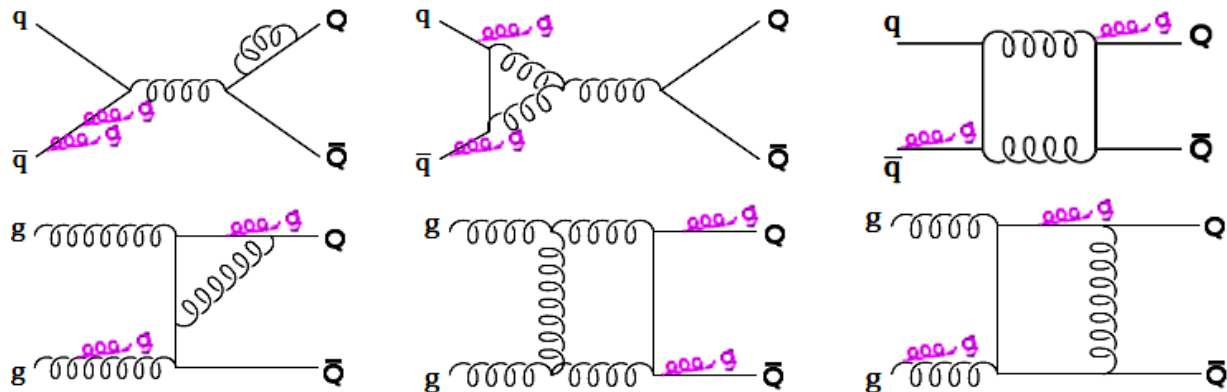
- NLO+ next-to-leading-log (NLL) soft gluon resummation QCD:



NLO real:



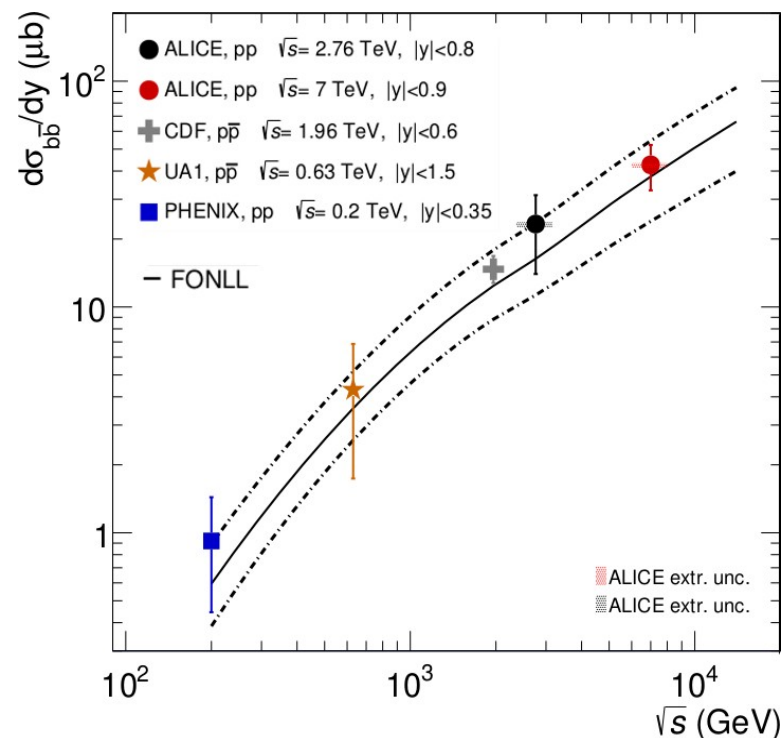
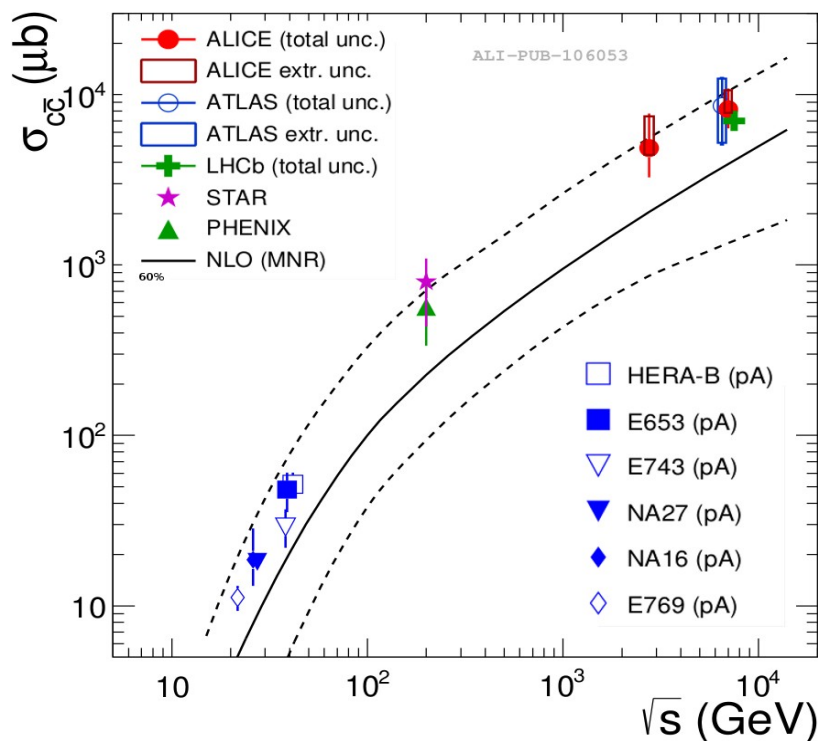
NLO virtual:



Mangano,  
Nason,  
Ridolfi  
Cacciari,  
**(FONLL)**  
Catani,  
Frixione,  
Mitov,  
Czakon,  
...  
[<2012]

# Charm & bottom in pp, p $\bar{p}$ : Data vs NLO+NLL

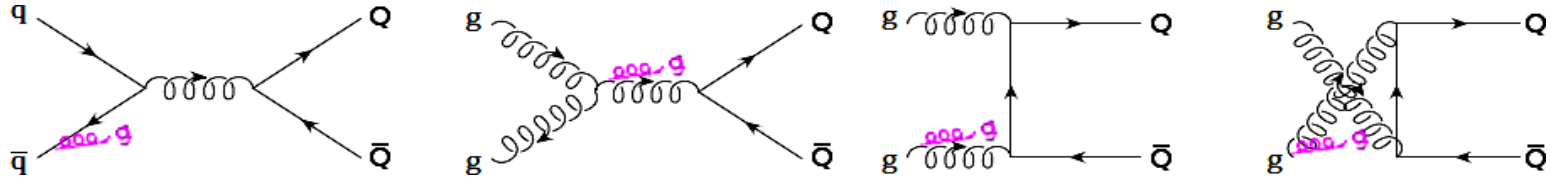
- pQCD predictions at NLO+NLL accuracy (MNR, FONLL) **globally reproduce the data. Better for bottom than for charm** (charm measurements are at upper uncertainty band of the predictions):



- pQCD predictions at **NLO+NLL** accuracy have still **very large scale uncertainties**:  $\sim 60\%$  for  $c\bar{c}$  (low  $m_c \sim 1.67$  GeV)  
 $\sim 35\%$  for  $b\bar{b}$  ( $m_b \sim 1.67$  GeV)

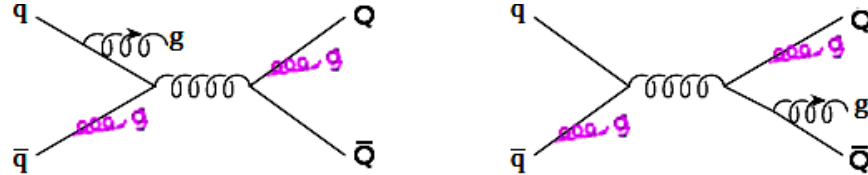
# Heavy-Quark production in $pp, p\bar{p}$ (NNLO)

- LO + leading-log (LL) soft gluon resummation QCD processes:

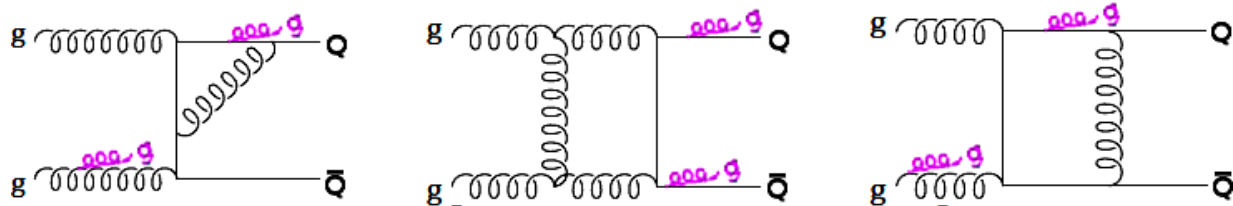


- NLO+ next-to-leading-log (NLL) soft gluon resummation QCD:

NLO real:

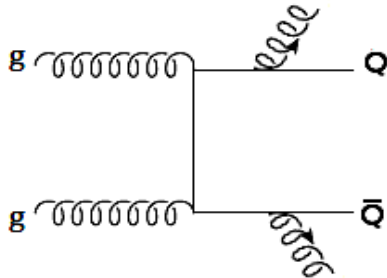


NLO virtual:

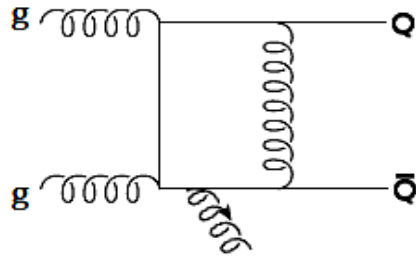


- NNLO+ next-to-leading-log (NLL) soft gluon resummation QCD:

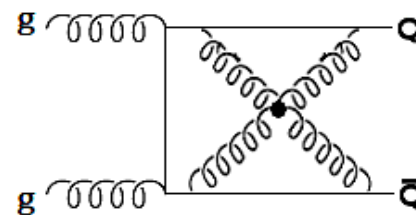
Real+Real:



Real+Virtual:



Virtual+Virtual:

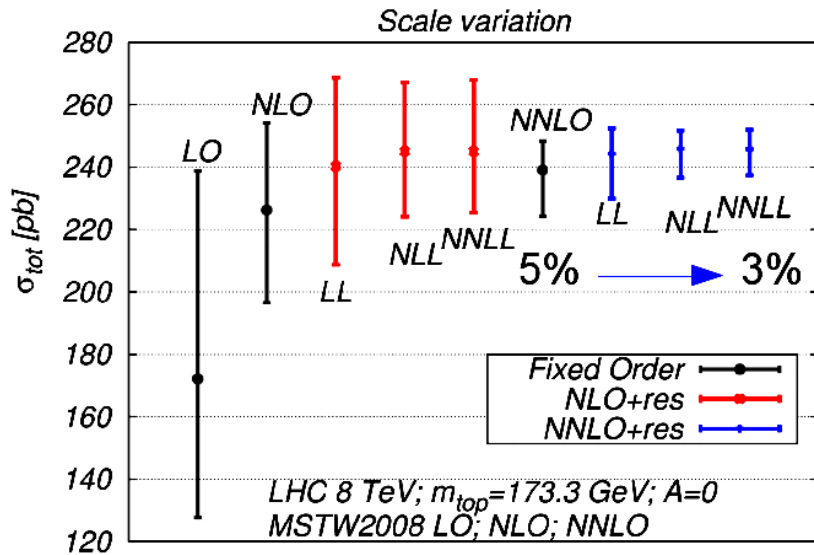


Mitov, Czakon  
(Top++)  
Moch et al.  
(HATHOR)

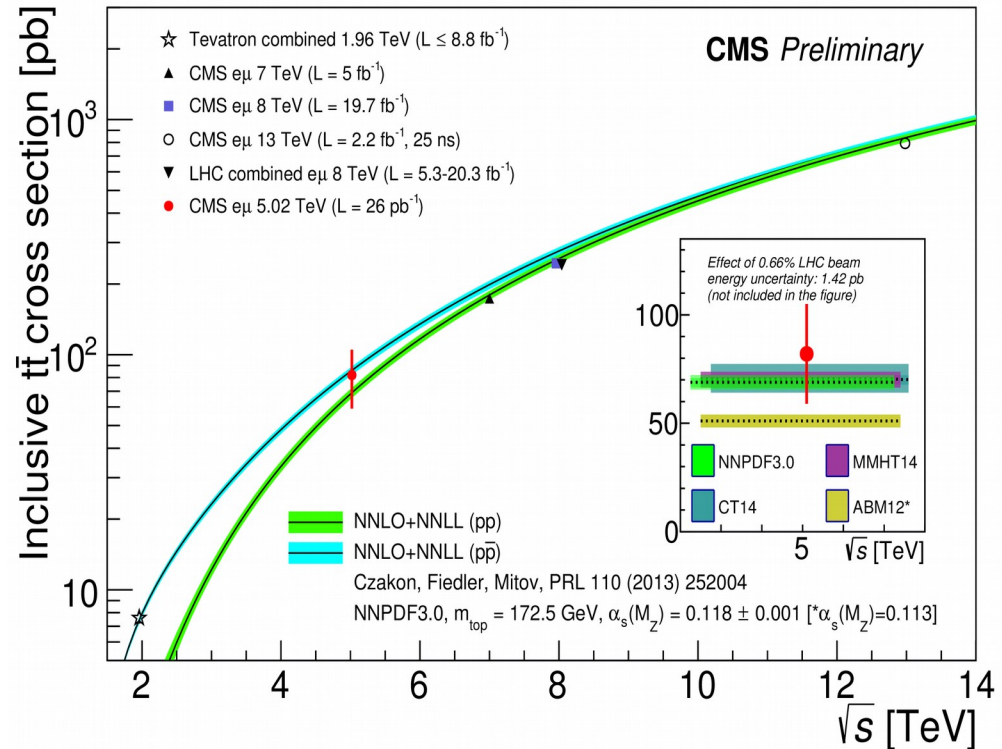
...  
[>2013]

# $t\bar{t}$ production in $pp, p\bar{p}$ : Data vs NNLO+NNLL

- Current state-of-the-art NNLO+NNLL calculations for  $t\bar{t}$  agree very well with data and have very small scale uncertainties: 5%  $\rightarrow$  3%



Mitov, Czakon et al. (Top++) 2013



- High precision of  $t\bar{t}$  data & theory allows for accurate extractions of high- $x$  gluon PDF and of the strong coupling  $\alpha_s$ .

- Use Top++ (NNLO+NNLL) to compute cc,bb total cross sections?



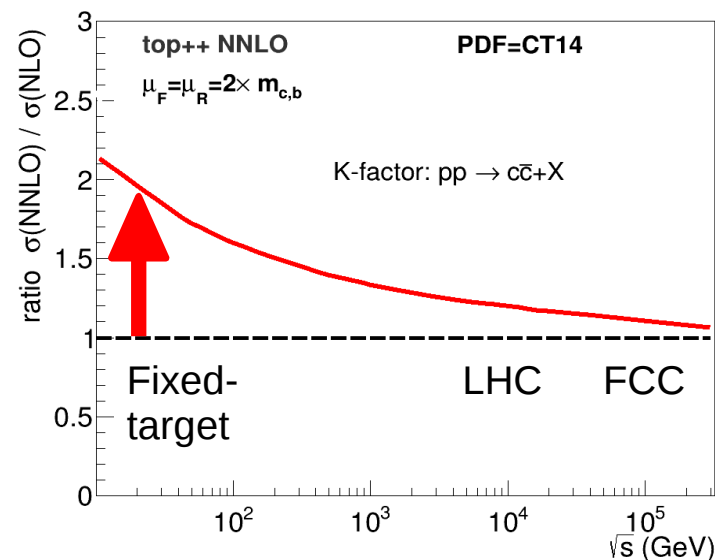
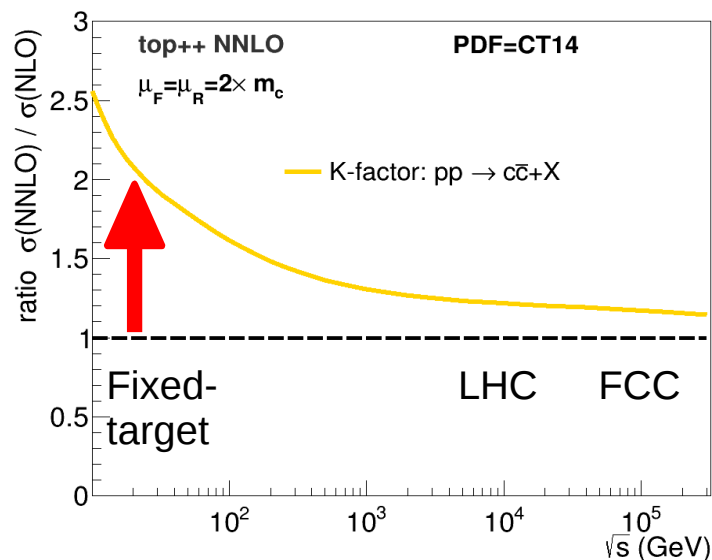
# $\sigma(c\bar{c}, b\bar{b})$ at NNLO. Theoretical setup

[Dd'E 2017, to be submitted]

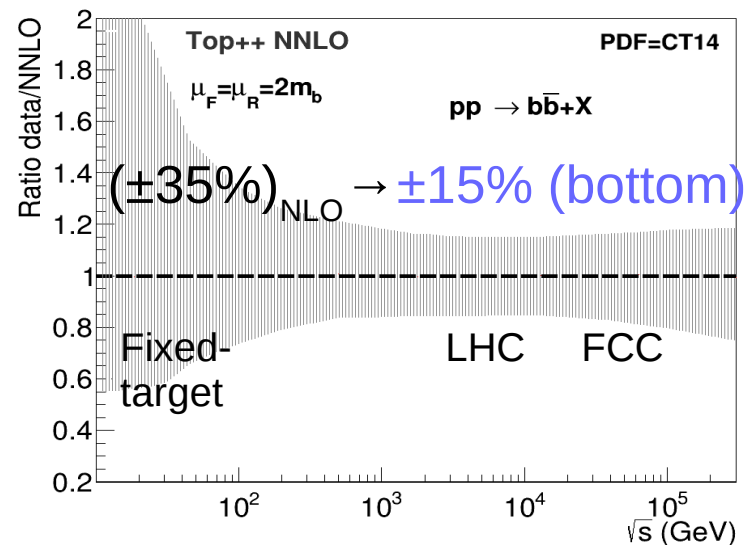
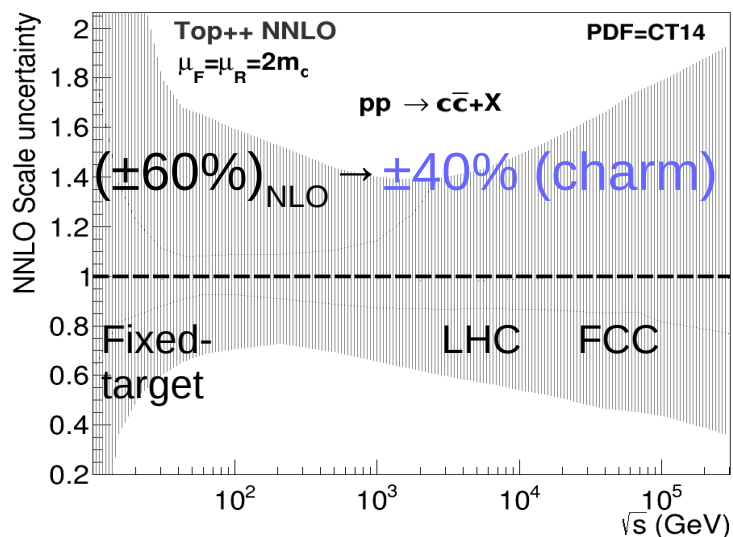
- Modified version of Top++:
  - Heavy-quark (pole) masses:  $m_c = 1.67$  GeV,  $m_b = 4.66$  GeV
  - Active number of flavours:  $N_f = 3$  (ccbar), 4 (bbbar)
- Model parameters:
  - Default scales:  $\mu_F = \mu_R = 2 \cdot m_{c,b}$  (Uncertainties:  $\mu_F, \mu_R = [1, 4] \times m_{c,b}$ )
  - QCD coupling (PDF default):  $\alpha_s = 0.118$
  - PDFs (3, 4 flavour scheme. Interfaced via LHAPDF v6.1.6):
    - CT14\_NNLO (90% CL, 56 eigenvector sets, asymmetric)
    - MMHT14\_NNLO (68% CL, 50 eigenvector sets, asymmetric)
    - ABMP16\_NNLO (68% CL, 28 eigenvector sets, symmetric)
    - NNPDF3.0\_NNLO (68% CL, 100 replicas, symmetric)
  - Pure NNLO. NNLL gluon **resummation not included** (yet)
- Modified Top++ run for  $\sqrt{s}$  of  $\sim 20$  existing experimental data sets:
  - Charm: 11 measurements from  $\sqrt{s} = 20$  GeV (fixed-target) to 13 TeV (LHC)
  - Bottom: 8 measurements from  $\sqrt{s} = 40$  GeV (fixed-target) to 13 TeV (LHC)

# $\sigma(c\bar{c}, b\bar{b})$ results: NLO vs NNLO

- Large charm & bottom K-factors :  $\sigma(\text{NNLO}/\text{NLO}) \sim 2$  (fixed-target) – 1.2 (LHC)



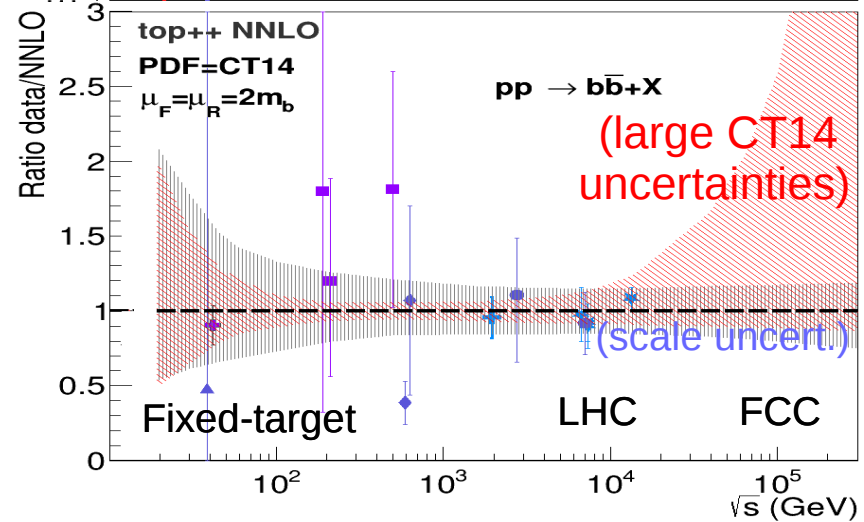
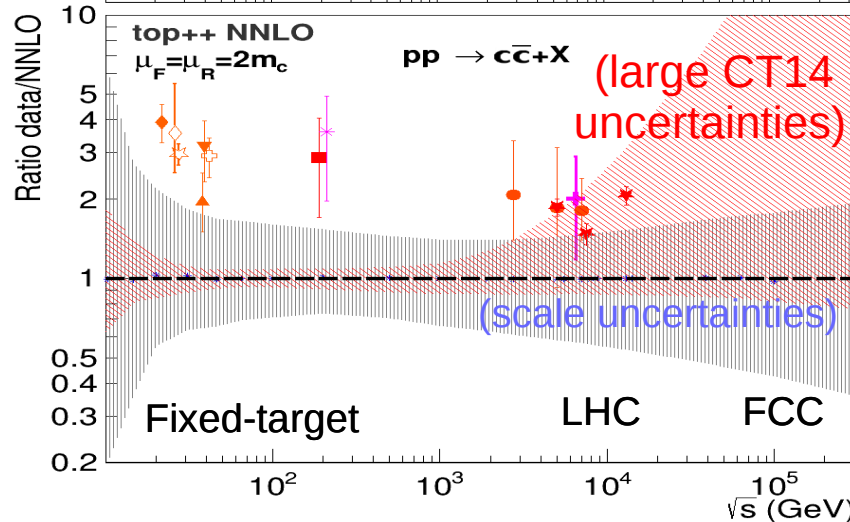
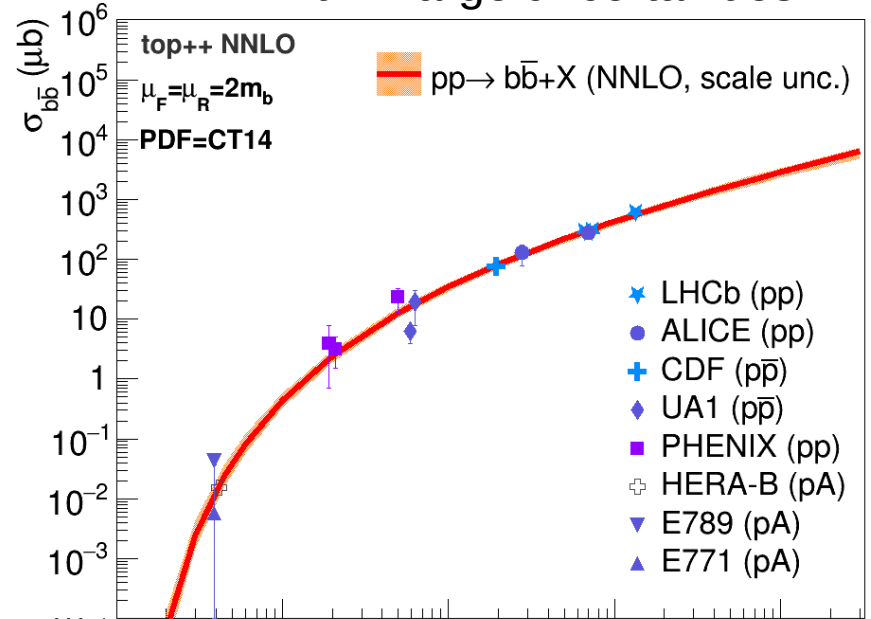
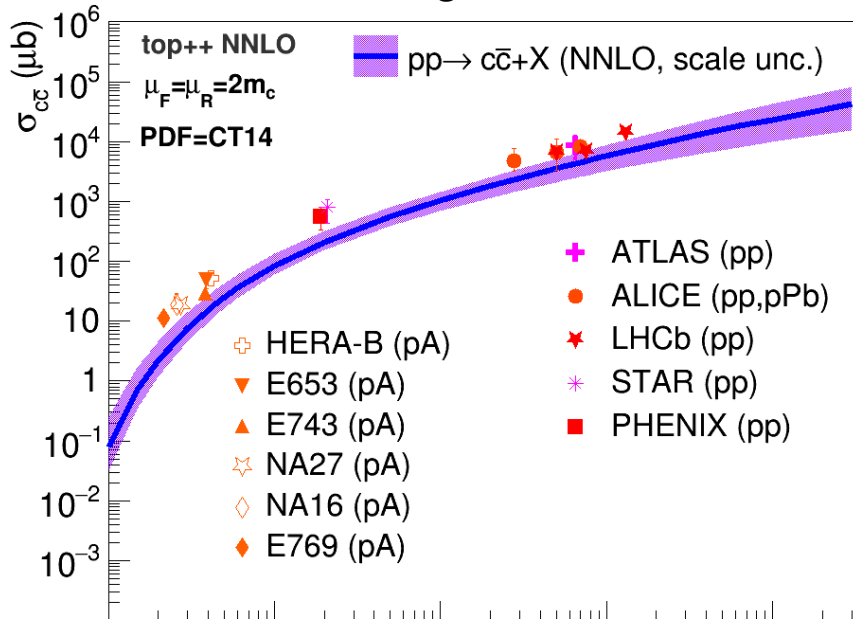
- Reduced NLO  $\rightarrow$  NNLO scale uncertainties:



# $\sigma(c\bar{c}, b\bar{b})$ : Data vs. NNLO (CT14 PDF)

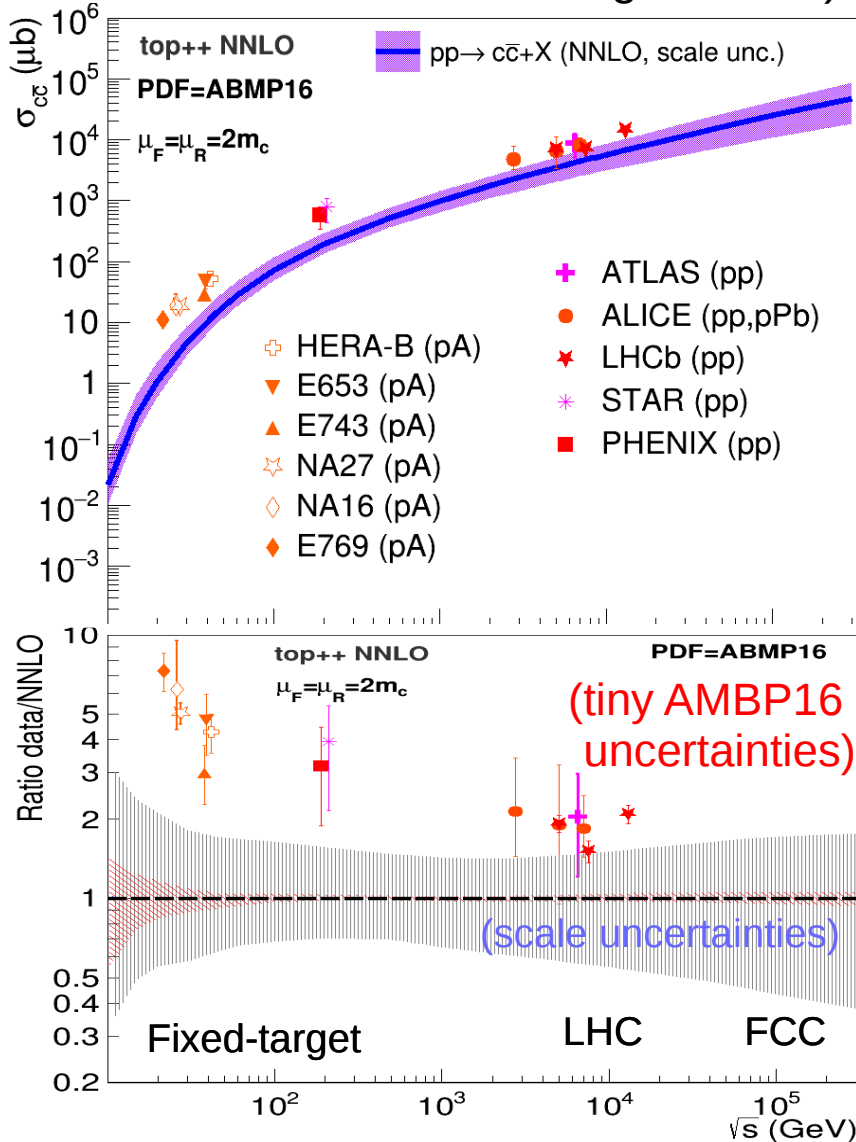
■ Charm: Data  $\times 2$  theory, but agreement within large uncertainties

■ Bottom: Very good agreement at all  $\sqrt{s}$  within large uncertainties

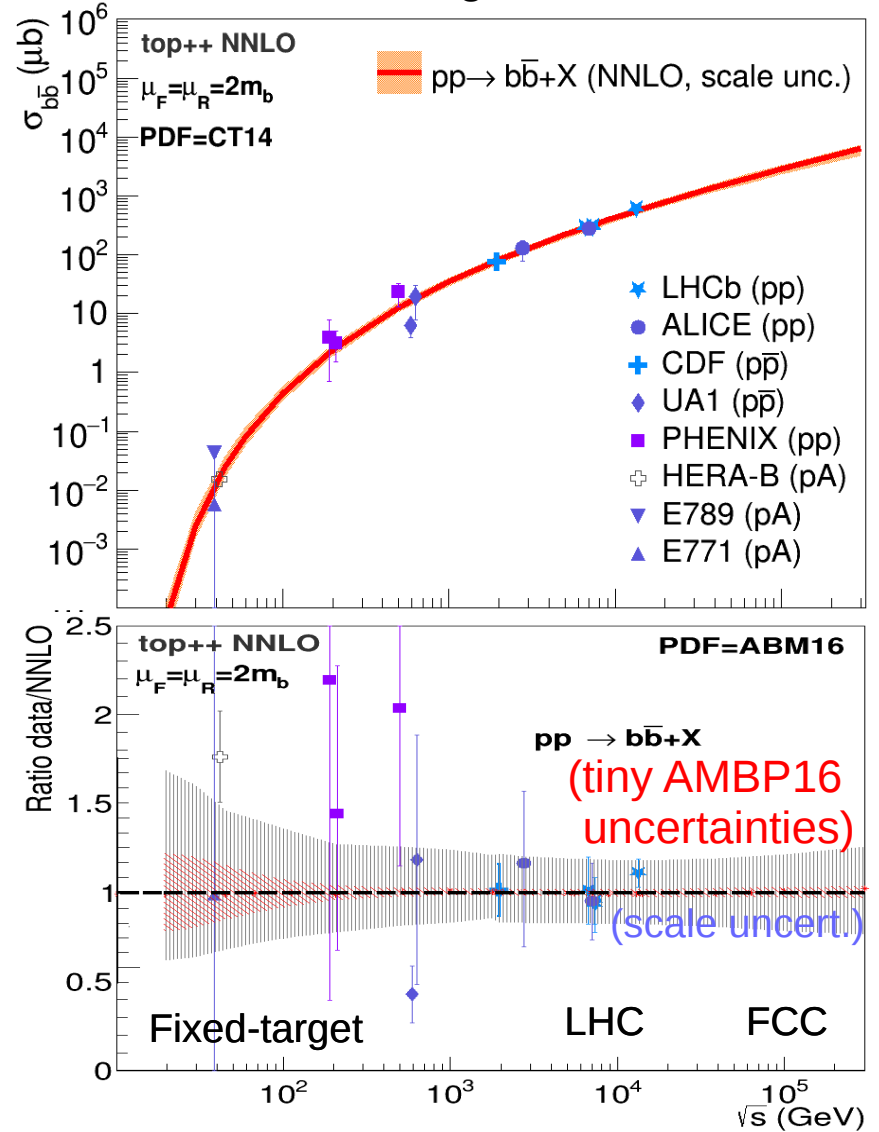


# $\sigma(c\bar{c}, b\bar{b})$ : Data vs. NNLO (ABMP16 PDF)

■ Charm: Data  $\times 2-5$  theory (agreement for LHC within large uncert.)

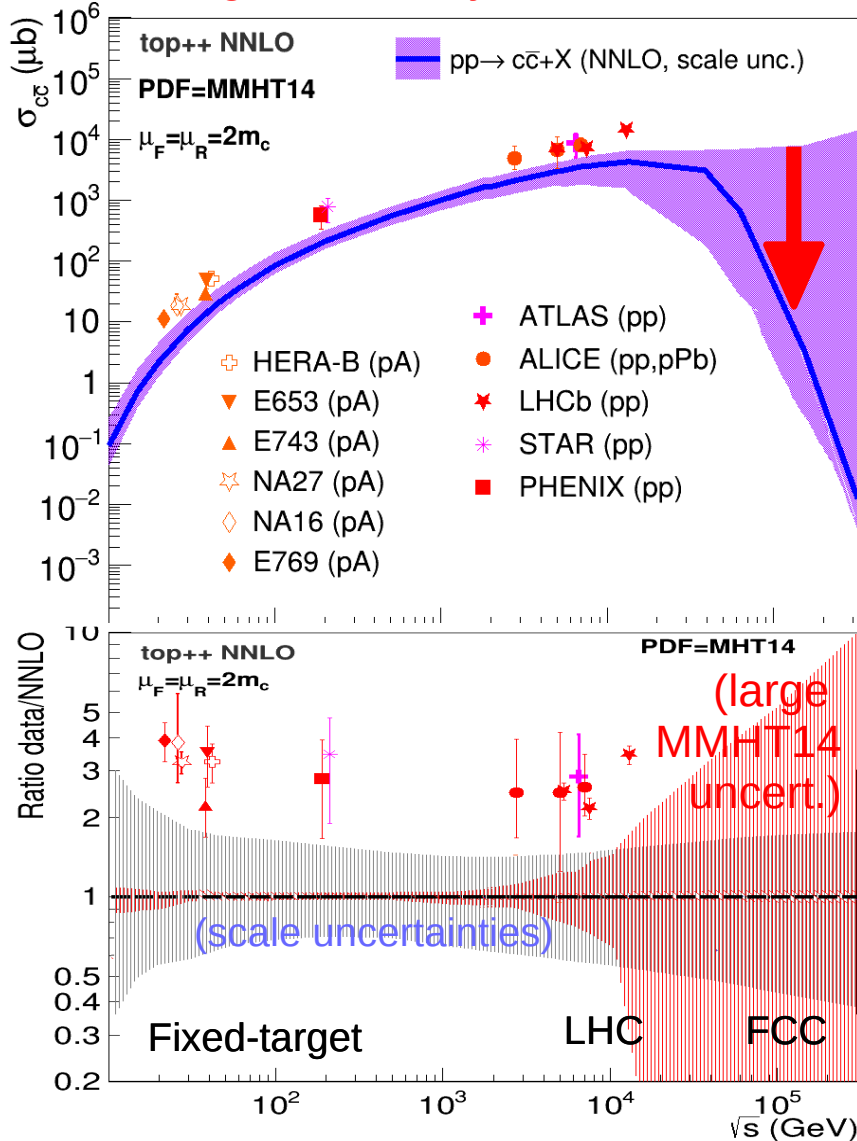


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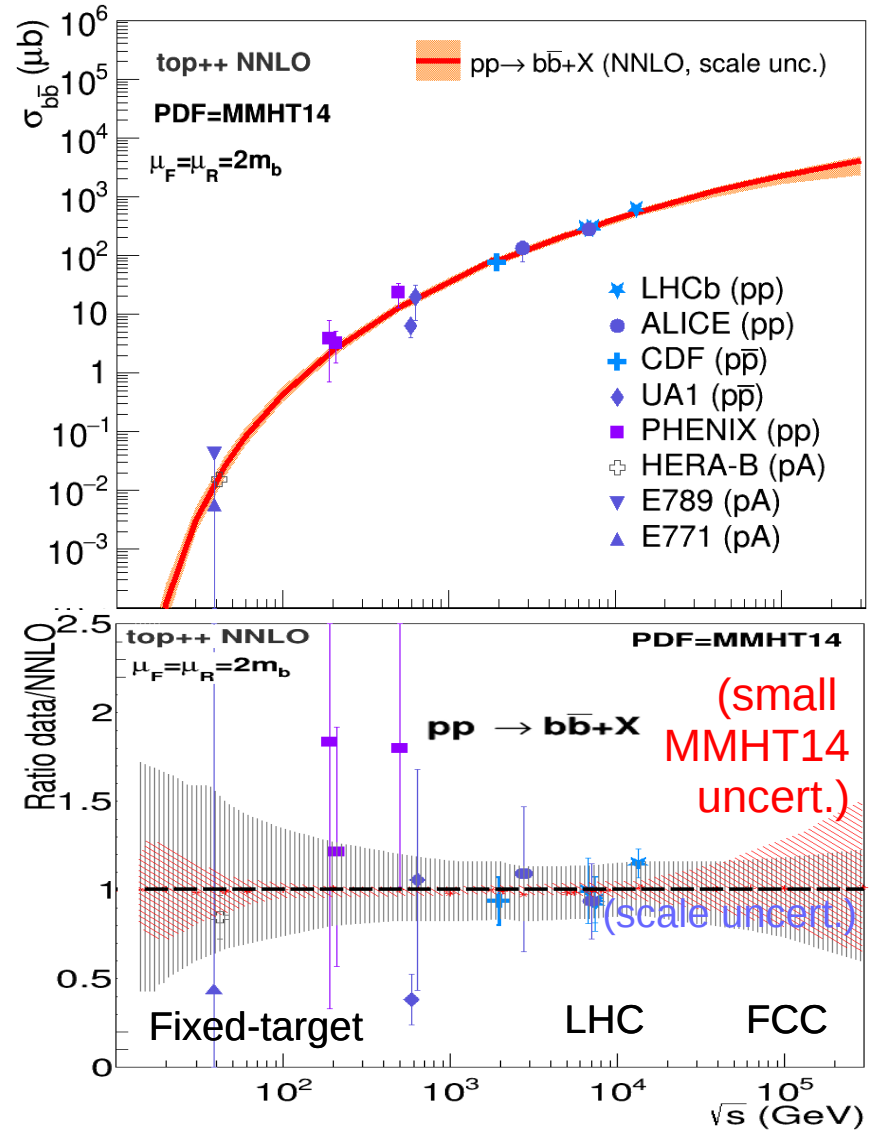


# $\sigma(c\bar{c}, b\bar{b})$ : Data vs. NNLO (MMHT14 PDF)

■ Charm: Data  $\times 2.5$  theory (negative gluon at very low  $x$ ,  $\sqrt{s} > 30$  TeV)

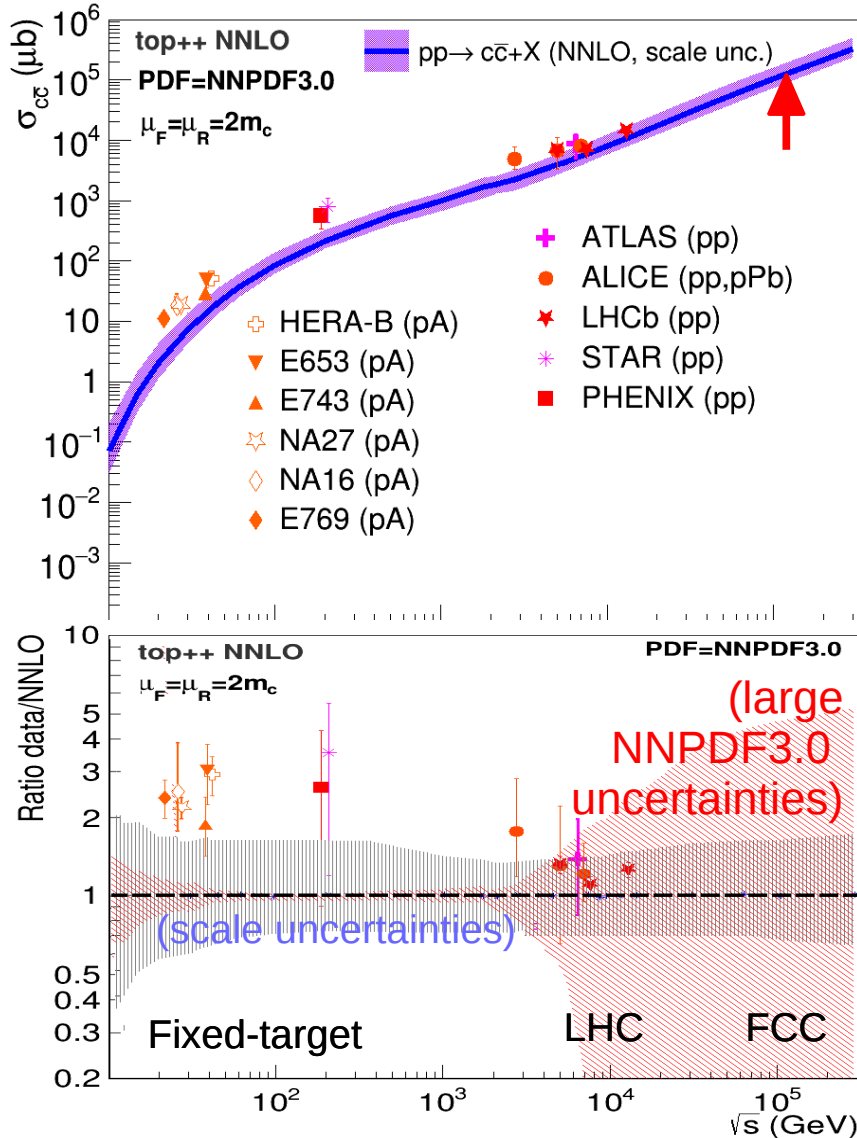


■ Bottom: Very good agreement at all  $\sqrt{s}$  within large uncertainties

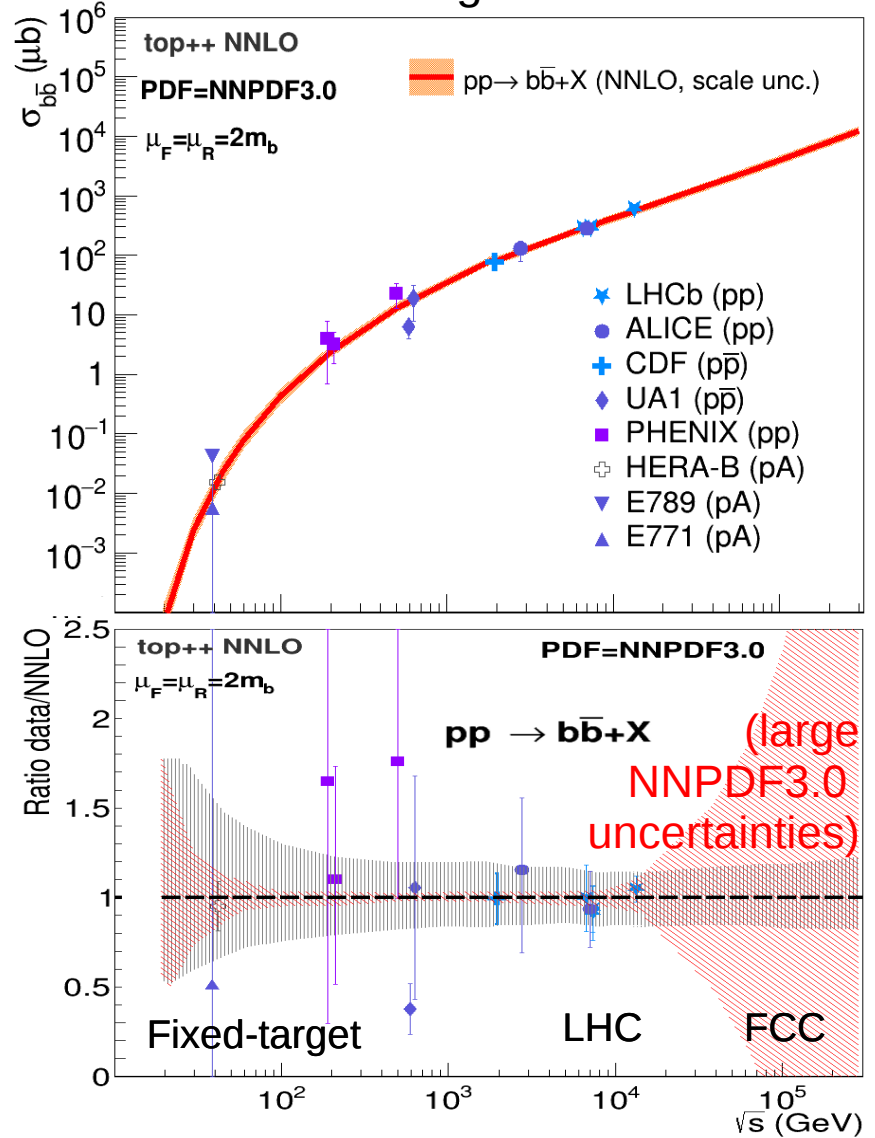


# $\sigma(c\bar{c}, b\bar{b})$ : Data vs. NNLO (NNPDF3.0 PDF)

■ Charm: Data  $\times 2$  theory (agreement within uncert. but “kink” at  $\sqrt{s} > 10$  TeV)



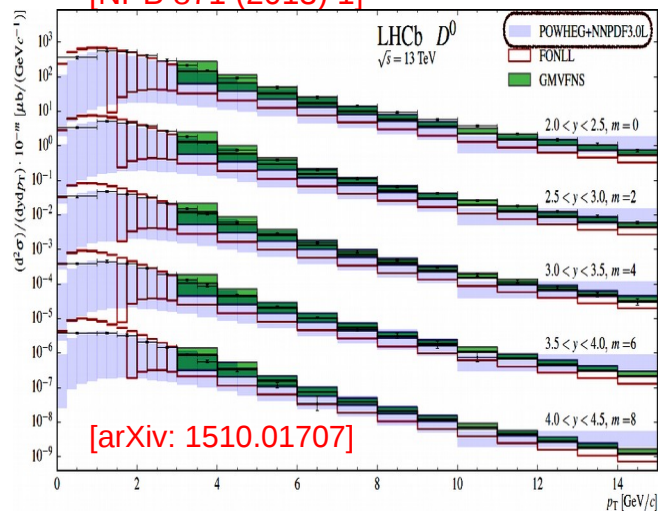
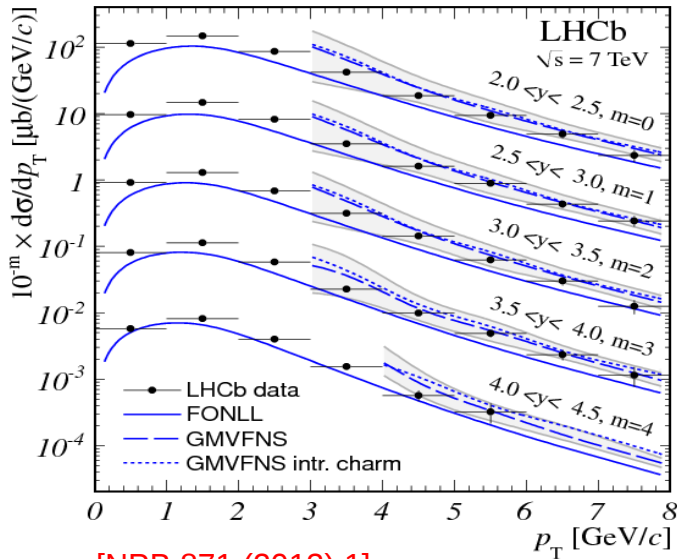
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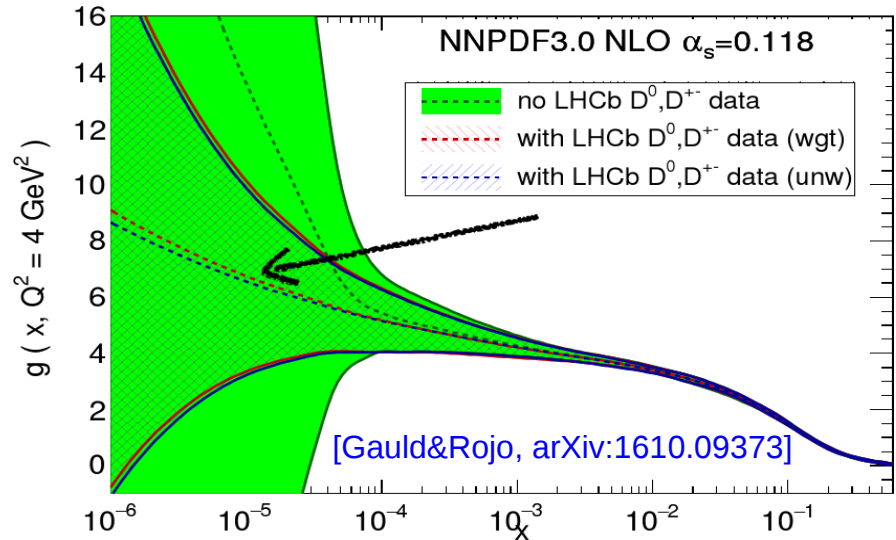
# Updated NNPDF3.0 (NLO) low-x gluon

- Forward D-mesons (LHCb) probe gluon down to  $x \sim 10^{-6}$ :

- 5,7,13 TeV D-meson data fitted with FONLL calculations (GM-VFN scheme):



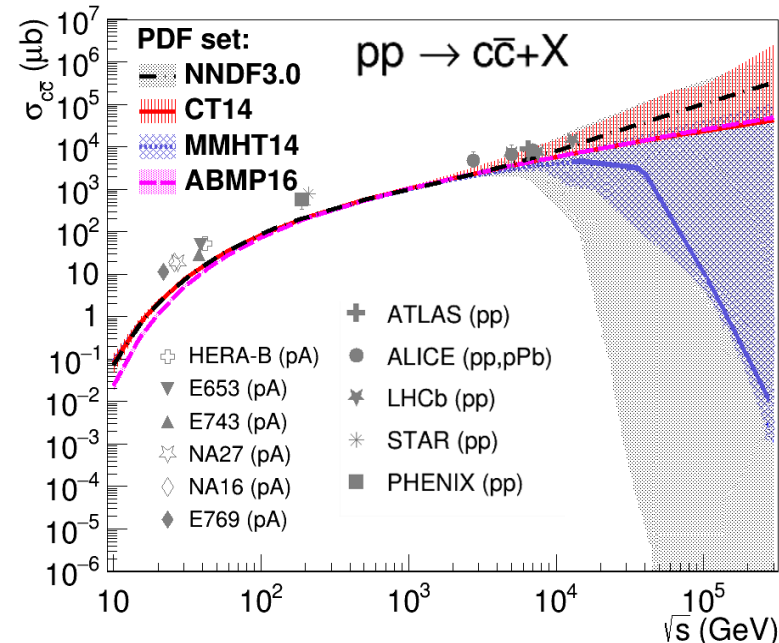
- Updated analysis based on normalized cross-sections at 5, 7 and 13 TeV and cross-section CoM energy ratios (avoiding double counting)
- Good description of all datasets, compatible pull on the small-x gluon except the R13/7 ratio
- The  $N^5+N^7+N^{13}$  combination leads to a reduction of the small-x gluon PDF errors by an order of magnitude!



- Future NNPDF low-x gluon will cure  $\sigma(cc)$  high- $\sqrt{s}$  "kink" & reduce uncertainties

# Summary

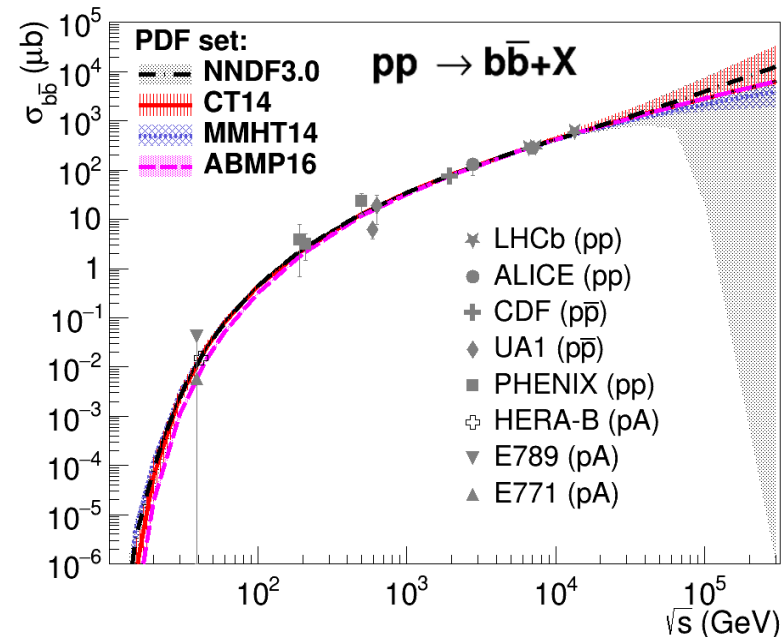
- **First-ever calculation of NNLO total charm and bottom cross sections** in hadronic collisions (using modified version of Top++):
  - ✓ **Large K-factors:**  $\sigma(\text{NNLO/NLO}) \sim 2(\text{fixed-target})\text{--}1.2(\text{LHC})$
  - ✓ **Reduced scale uncertainties:**  
 Charm:  $\pm(60\%)_{\text{NLO}} \rightarrow \pm(40\%)_{\text{NNLO}}$  Bottom:  $\pm(35\%)_{\text{NLO}} \rightarrow \pm(15\%)_{\text{NNLO}}$
- Agreement with data (20 measurements from 20 GeV to 10 TeV), within large (PDF & exp.) uncertainties, though **central exp. charm x-section still  $\times 2\text{--}3$  above theory.**
- **Very strong sensitivity to low-x gluon PDF (esp. charm). Predictions above LHC have uncontrolled behaviours and/or very large uncertainties:**
  - CT14 gluon seems best behaved overall
  - AMBP16 underestimates most low- $\sqrt{s}$  data.
  - MMHT14 gluon dives to zero above  $\sim 30$  TeV
  - NNPDF3.0 gluon best agreement w/ data (but unphysical slope change & huge uncertainties at  $\sim 10$  TeV)
- **At  $\sqrt{s} \sim 300$  TeV,  $\sigma_{cc} \sim \sigma_{\text{inel}}$ : Impact on  $\mu, \nu$  of most energetic cosmic-rays showers**





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- **Bottom x-sections well behaved** for all PDFs up to  $\sim 100$  TeV.



# Backup slides