

# Measurement of the running of the fine structure constant below 1GeV with the KLOE detector

V. De Leo on behalf of the KLOE-2 Collaboration

*veronica.deleo@roma2.infn.it*



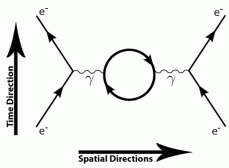
March 26<sup>th</sup>, 2017

# Overview

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- 3 Analysis
  - Event selection
  - Measured  $\mu^+\mu^-\gamma$  cross section
- 4 Measurement of the effective  $\alpha_{QED}$  coupling constant between 600 and 975 MeV
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- 6 Conclusions

# Physics Motivations

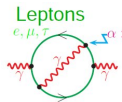
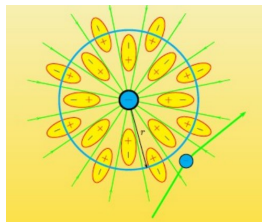
Knowledge of the QED coupling constant fundamental for testing the Standard Model



Modification of the QED coupling constant due to the Vacuum Polarization diagram:

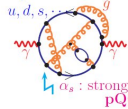
$$e^2 \rightarrow e^2(q^2) = \frac{e^2}{1 + (\Pi'_\gamma(q^2) - \Pi'_\gamma(0))};$$

$$\alpha(q^2) = \frac{\alpha(0)}{1 - \Delta\alpha(q^2)}$$



$\alpha$ : weak coupling pQED ✓

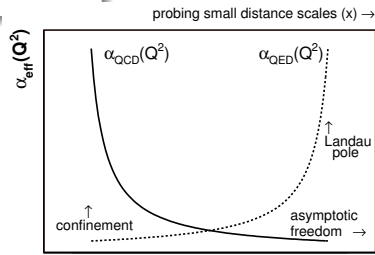
Quarks



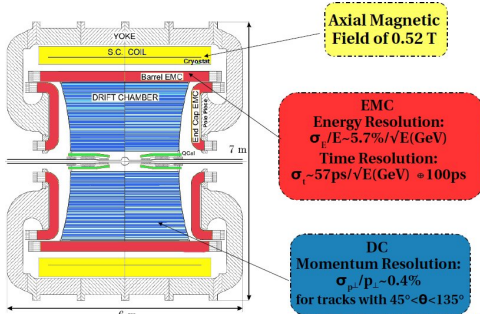
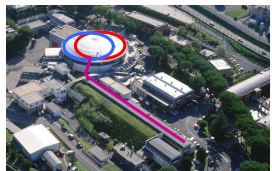
$\alpha_s$ : strong coupling pQCD

$$\Delta\alpha(q^2) = \Delta\alpha_{lep}(q^2) + \Delta\alpha_{had}(q^2)$$

No data in the low energy region



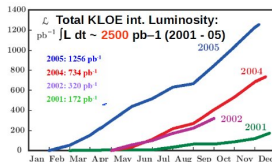
# The Frascati $\Phi$ Factory and the KLOE detector



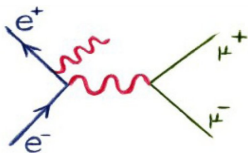
- EMC:**
- ◆ lead/scintillating fibers
  - ◆ 98% solid angle coverage
- DC:**
- ◆ Gas mixture: 90%He + 10% $C_4H_{10}$

## KLOE Data Set:

- On peak ( $\sqrt{s} \sim 1.02\text{GeV}$ ),  $2.5\text{fb}^{-1}$
- Off peak ( $\sqrt{s} = 1.0\text{GeV}$ ),  $250\text{pb}^{-1}$



## Analysis Method



where:

$$\frac{d\sigma^{ISR}}{dM_{\mu\mu}} = \frac{N_{obs} - N_{bkg}}{dM_{\mu\mu}} \frac{1}{\epsilon(\sqrt{s_\mu})L}$$

- $\theta_\gamma < 15^\circ$  ( $\theta_\gamma > 165^\circ$ )
- $0 < \theta_\mu < 180^\circ$

with FSR effects removed

$$\left| \frac{\alpha_{QED}(s)}{\alpha_{QED}(0)} \right|^2 = \frac{d\sigma^{ISR}}{dM_{\mu\mu}} \frac{d\sigma^{MC}}{dM_{\mu\mu}}$$

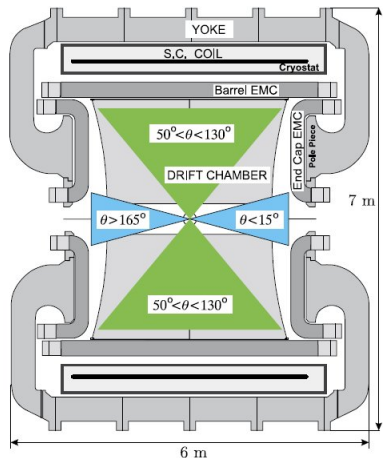
$\frac{d\sigma^{MC}}{dM_{\mu\mu}}$  obtained from PHOKARA gen.

with the following conditions:

- $\theta_\gamma < 15^\circ$  ( $\theta_\gamma > 165^\circ$ )
- $0 < \theta_\mu < 180^\circ$

Inclusive of the ISR and with the VP contribution removed

# Event selection: Small Angle (SA)



- Two tracks of opposite sign with

$$50^\circ < \theta < 130^\circ$$

- Photons (not detected) at small angles :

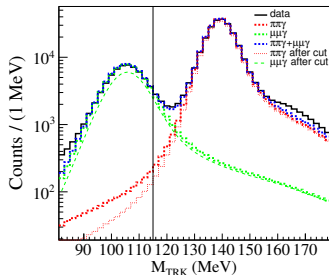
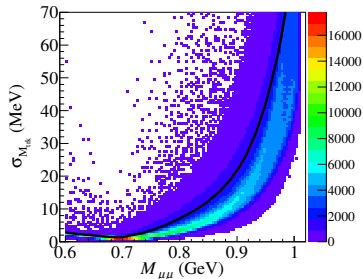
$$\theta < 15^\circ \text{ or } \theta > 165^\circ$$

- Photon momentum from kinematics:

$$\vec{p}_\gamma \simeq \vec{p}_{miss} = -(\vec{p}_+ + \vec{p}_-)$$

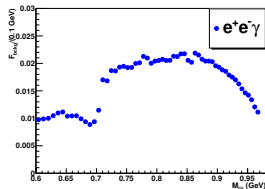
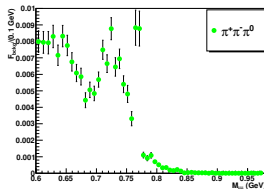
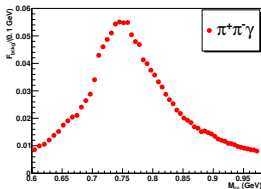
- High statistics for ISR photons
- Very small contribution from FSR
- Reduced background contamination

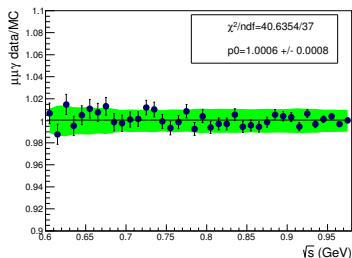
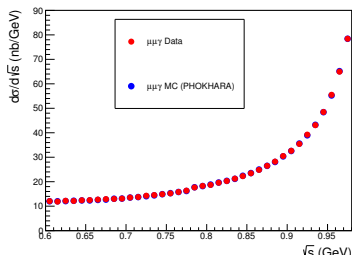
## Event selection



- $M_{TRK} < 115$  MeV for muons

$$M_{TRK} = (\sqrt{s} - \sqrt{|\vec{p}_+^-|^2 + M_{TRK}^2} - \sqrt{|\vec{p}_-^-|^2 + M_{TRK}^2})^2 - (\vec{p}_+^- + \vec{p}_-^-)^2 = 0$$



Measurement of the  $\mu^+\mu^-\gamma$  cross section

$$\frac{d\sigma}{dM_{\mu\mu}} = \frac{N_{obs} - N_{bkg}}{dM_{\mu\mu}} \frac{(1 - \delta_{FSR})}{\epsilon(\sqrt{s_\mu})L}$$

$$\frac{d\sigma_{\mu\mu\gamma}^{DATA}}{d\sigma_{\mu\mu\gamma}^{MC}} = 1.0006 \pm 0.0007$$

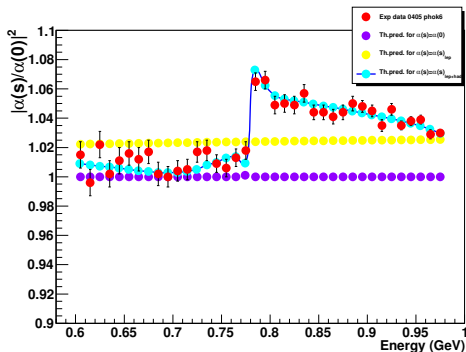
Excellent agreement with NLO theory (PHOKHARA MC) VP inside

H. Czyż, A. Grzelinska, J.H. Kühn, G. Rodrigo, Eur. Phys. J. C 39 (2005) 411.

Total systematic error  $\sim 1\%$ .



# Measurement of the effective $\alpha_{QED}$ coupling constant between 600 and 975 MeV



$$\left| \frac{\alpha_{QED}(s)}{\alpha_{QED}(0)} \right|^2 = \frac{\frac{d\sigma}{dM_{\mu\mu}}^{ISR}}{\frac{d\sigma}{dM_{\mu\mu}}^{MC}}$$

$\frac{d\sigma}{dM_{\mu\mu}}^{MC}$  with the VP contribution removed.

$$\left| \frac{\alpha(s)}{\alpha(0)} \right|^2 = |1/(1 - \Delta\alpha(s))|^2$$

$$\Delta\alpha(s) = \Delta\alpha_{lep}(s) + \Delta\alpha_{had}(s)$$

(we neglect the top contribution)

- ◆ “Theoretical prediction” (provided by the alphaQED package of F. Jegerlehner)  $\Delta\alpha_{lep}$  computed in QED with negligible error;  $\Delta\alpha_{had}$  obtained by a compilation of data in time-like region (with 0.1% accuracy).

$$\rightarrow \Delta\alpha_{had}(s) = -\left(\frac{\alpha s}{3\pi}\right) \text{Re} \int_{m_\pi^2}^{\infty} ds' \frac{R(s')}{s'(s'-s-i\epsilon)}$$

- ◆ The red points show the KLOE data with statistical error bars.

Extraction of Real and Imaginary part of  $\Delta\alpha(s)$ 

$$\text{Re } \Delta\alpha = 1 - \sqrt{|\alpha(0)/\alpha(s)|^2 - (\text{Im } \Delta\alpha)^2}$$

The Imaginary part of  $\Delta\alpha(s)$  can be related to the total cross section  $\sigma(e^+e^- \rightarrow \gamma^* \rightarrow \text{anything})$  (“anything” means any possible state).

$$\text{Im}\Delta\alpha = -\frac{\alpha}{3} R(s).$$

where:

$$R(s) = \sigma_{\text{tot}} / \frac{4\pi\alpha(s)^2}{3s}$$

- ◆  $R(s)$  take into account leptonic and hadronic contribution
- ◆  $R(s) = R_{lep}(s) + R_{had}(s)$ , where the leptonic part reads:

$$R_{lep}(s) = \sqrt{1 - \frac{4m_l^2}{s}} \left(1 + \frac{2m_l^2}{s}\right), \quad (l = e, \mu, \tau).$$

# Calculation of $R_{had}$

In the energy region around the  $\rho$  – meson we approximate the hadronic cross section to be given by the  $2\pi$  dominant contribution

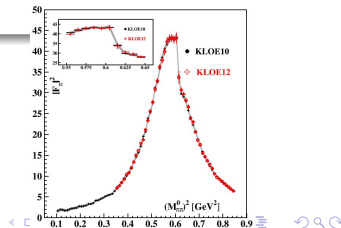
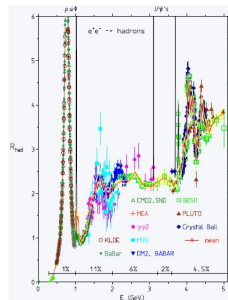
KLOE12 measurement of the pion form factor  $|F_\pi(s)|^2$  was used:

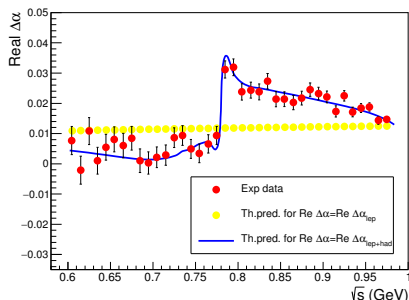
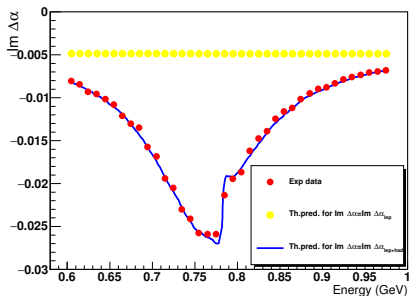
$$R_{had}(s) = \frac{1}{4} \left(1 - \frac{4m_\pi^2}{s}\right)^{\frac{3}{2}} |F_\pi^0(s)|^2$$

where:

$$|F_\pi^0(s)|^2 = |F_\pi(s)|^2 \left|\frac{\alpha(0)}{\alpha(s)}\right|^2.$$

Physics Letters B 720 (2013) 336–343



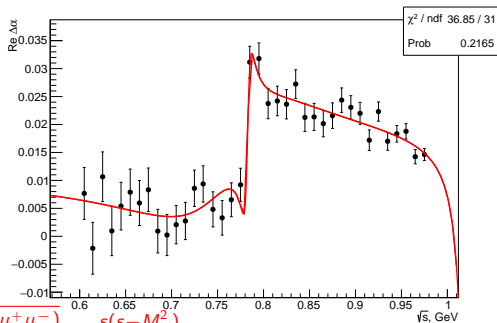
Imaginary part of  $\Delta\alpha$  only  $2\pi$  and Real part of  $\Delta\alpha$ 

$$\text{Re } \Delta\alpha = 1 - \sqrt{|\alpha/\alpha(s)|^2 - (\text{Im } \Delta\alpha)^2}$$

Excellent agreement with the "theoretical prediction"  
(data compilation)

Fit of the Real part of  $\Delta\alpha$ 

We fit  $\text{Re}\Delta\alpha$  by a sum of the leptonic and hadronic contributions, where the hadronic contribution is parametrized as a sum of  $\rho(770)$ ,  $\omega(782)$  and  $\phi(1020)$  resonances components and a non resonant term (param. with a pol1).



$$\text{Re } \Delta\alpha_{V=\omega,\phi} = \frac{3\sqrt{BR(V\rightarrow e^+e^-)\cdot BR(V\rightarrow\mu^+\mu^-)}}{\alpha M_V} \frac{s(s-M_V^2)}{(s-M_V^2)^2 + M_V^2\Gamma_V^2}$$

Gounaris-Sakurai parametrization for the  $\rho$ :

$$F_\pi(s) = BW_{\rho(s)}^{GS} = \frac{M_\rho^2(1+d\Gamma_\rho/M_\rho)}{M_\rho^2 - s + f(s) - iM_\rho\Gamma_\rho(s)}$$

(interference with the  $\omega$  and the higher excited states of the  $\rho$  neglected).

$\Gamma_\omega$ ,  $M_\phi$ ,  $\Gamma_\phi$ , and  $BR(\phi \rightarrow e^+e^-)BR(\phi \rightarrow \mu^+\mu^-)$  fixed to PDG values

K.A. Olive et al. (Particle Data Group), Chin. Phys. C, 38, 090001 (2014) and 2015 update.

Fit of the Real part of  $\Delta\alpha$ 

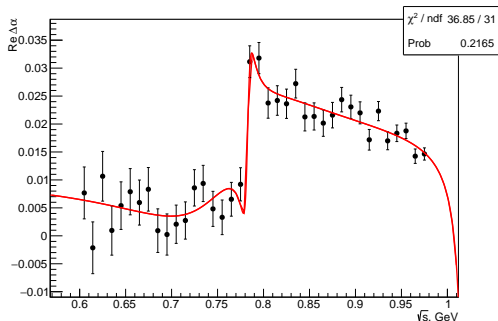
Assuming lepton universality and multiplying for the phase space correction:

$$\xi = \left(1 + 2 \frac{m_\mu^2}{m_\omega^2}\right) \left(1 - 4 \frac{m_\mu^2}{m_\omega^2}\right)^{1/2}$$



the  $BR(\omega \rightarrow \mu^+ \mu^-)$  results:

$(6.6 \pm 1.4_{stat} \pm 1.7_{syst}) \cdot 10^{-5}$   
 compared to  $(9.0 \pm 3.1) \cdot 10^{-5}$  from PDG.



Parameter	Result from the fit	Result from the fit with $\rho - \omega$ interf.	PDG
$M_\rho$ , MeV	$775 \pm 6$	$778 \pm 7$	$775.26 \pm 0.25$
$\Gamma_\rho$ , MeV	$146 \pm 9$	$147 \pm 10$	$147 \pm 0.9$
$M_\omega$ , MeV	$782.7 \pm 1.0$	$783.4 \pm 0.8$	$782.65 \pm 0.12$
$BR(\omega \rightarrow \mu^+ \mu^-) BR(\omega \rightarrow e^+ e^-)$	$(4.3 \pm 1.8) \cdot 10^{-9}$	$(4.4 \pm 1.8) \cdot 10^{-9}$	$(6.5 \pm 2.3) \cdot 10^{-9}$
$\chi^2 / ndf$	1.19	1.15	

# Conclusions

- The measurement of  $\alpha_{QED}$  running has been performed in the time-like region  $0.6 < \sqrt{s} < 0.975\text{GeV}$ .
- It represents the first measurement of the running of  $\alpha_{QED}$  in this region by a single experiment. It shows a significance of more than  $5\sigma$  of the hadronic contribution to the running of  $\alpha_{QED}$  with a spectacular evidence of  $\rho - \omega$  resonances contribution to the photon Vacuum Polarization
- For the first time also the real and imaginary part of  $\Delta\alpha$  have been extracted using the experimental data.
- The fit  $\text{Re}\Delta\alpha$  allows also to measure the the  $BR(\omega \rightarrow \mu^+ \mu^-)$ :  
 $(6.6 \pm 1.4_{stat} \pm 1.7_{syst}) \cdot 10^{-5}$
- Paper published in Phys.Lett.B  
(<https://dx.doi.org/10.1016/j.physletb.2016.12.016>).

THANK YOU!!!